

$$\textcircled{b} \quad \lim_{n \rightarrow \infty} (ka_n) = ka.$$

proof :- let  $\epsilon > 0$  be given  
 since  $\lim_{n \rightarrow \infty} a_n = a \Rightarrow \exists$  positive integer  $N$

$$\exists |a_n - a| < \frac{\epsilon}{|k|} \quad \forall n \geq N, k \neq 0.$$

$$\therefore |ka_n - ka| = |k(a_n - a)| = |k| \cdot |a_n - a| \\ < |k| \cdot \frac{\epsilon}{|k|} = \epsilon.$$

$$\therefore |ka_n - ka| < \epsilon.$$

proof  $\lim_{n \rightarrow \infty} (a + ka_n) = a + ka$

let  $\epsilon > 0$  be given

since  $\lim_{n \rightarrow \infty} a_n = a \Rightarrow \exists$  positive integer  $N$

$$\exists |a_n - a| < \epsilon \quad \forall n \geq N.$$

$$\Rightarrow |(a_n + ka) - (a + ka)| = |a_n + ka - a - ka| = |a_n - a| < \epsilon \\ \forall n \geq N.$$

$$\therefore |(a_n + ka) - (a + ka)| < \epsilon$$

$$\therefore \lim_{n \rightarrow \infty} (a + ka_n) = a + ka.$$