

Shom p. 46. ex. (3.7)

Two men m_1 and m_2 , and three women w_1, w_2 and w_3 are in a chess tournament. ^{play games.} those of the same sex have equal prob. of winning, but each man is twice as likely to win as any woman,

- (A) Find the prob. that a woman wins the tournament. ^{play game}
- (B) if m_1 and w_1 are married, find the prob. that one of them wins the tournament. ^{game}

set. $p(w_1) = p$

then $p(w_2) = p(w_3) = p$

and $p(m_1) = p(m_2) = 2p$.

این کار را می توانیم با این روش انجام دهیم.
فرض کنیم که احتمال برنده شدن هر یک از زنان w_1, w_2, w_3 برابر با p است.
چون هر مرد دو برابر از هر زن شانس برنده شدن دارد، پس احتمال برنده شدن هر یک از مردان m_1, m_2 برابر با $2p$ است.
(در اینجا یعنی لااقل به حدی که می توانیم).

and $p(m_1) = p(m_2) = 2p$.

next set the sum of the prob. of the five sample points equal to one.

$$p + p + p + 2p + 2p = 1 \quad \text{or} \quad p = \frac{1}{7}$$

we seek (A) $p\{(\omega_1, \omega_2, \omega_3)\}$

(B) $p(m_1, \omega_1)$

then by definition

(A) $p(\omega_1, \omega_2, \omega_3) = p(\omega_1) + p(\omega_2) + p(\omega_3)$

$$= \frac{1}{7} + \frac{1}{7} + \frac{1}{7}$$

$$= \boxed{\frac{3}{7}}$$

$$m = 2\omega$$

$$p(m) = 2p(\omega)$$

$$p(\omega) = p$$

$$p(m) = 2p$$

$$p(m) + p(\omega) = 1$$

$$p + 2p = 1$$

$$p = \frac{1}{3}$$

$$p(M_1, w_1)$$

then by definition

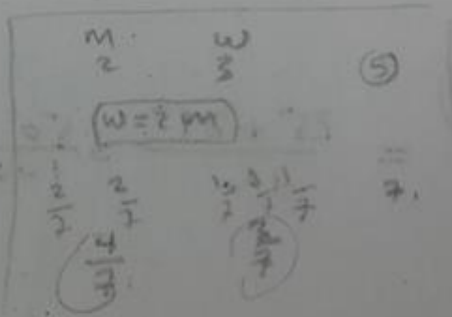
$$p(M) + p(W) = 1$$

$$p + 2p = 1$$

$$p = \boxed{\frac{1}{3}}$$

$$\begin{aligned} \textcircled{A} \quad p(w_1, w_2, w_3) &= p(w_1) + p(w_2) + p(w_3) \\ &= \frac{1}{7} + \frac{1}{7} + \frac{1}{7} \\ &= \boxed{\frac{3}{7}} \end{aligned}$$

$$p(M_1, w_1) = p(M_1) + p(w_1) = \frac{2}{7} + \frac{1}{7} = \boxed{\frac{3}{7}}$$



$$\frac{C_1^{26}}{C_1^{52}} + \frac{C_1^4}{C_1^{52}} = \boxed{\frac{30}{52}}$$

ex. 22

You will win 10 if the cards selected is either black or king.
what is the prob. of winning in the games.

A = the cards is black.

B = the card is king.

$$P(A \cup B) = P(A) + P(B) - P(A \cap B)$$

$$\frac{C_1^{26}}{C_1^{52}} + \frac{C_1^4}{C_1^{52}} - \frac{C_1^2}{C_1^{52}} = \boxed{\frac{26}{52}}$$

ex. 23

If a die is thrown once what is the prob. of getting

$$\frac{C_1^{26}}{C_1^{52}} + \frac{C_1^4}{C_1^{52}} \rightarrow \frac{C_1^6}{C_1^{52}} = \boxed{\frac{26}{52}}$$

ex. 23

If one dice is thrown once what is the prob. of getting either even or divisible by 3.

A = even

S = {1, ..., 6}

B = divi. by 2.

$$P(A \cup B) = P(A) + P(B) - P(AB)$$

$$= \frac{3}{6} + \frac{2}{6} - \frac{1}{6} = \boxed{\frac{4}{6}}$$

$$\text{or } P(C) = 1 - P(C^c) = 1 - 0.01 = \boxed{0.99}$$

⑥

⑤

ex. 25 if one dice is thrown what is the prob. of getting either 4 or 5

A = number 4 appears.

B = number 5 appears.

$$P(A \cup B) = P(A) + P(B) - P(AB)$$

$$= \frac{1}{6} + \frac{1}{6} - 0 = \boxed{\frac{2}{6}}$$

at least one

at least two

$$P(1) + P(2) + P(3) + \dots + P(100) = 0.05$$

$$P(2) + P(3) + \dots + P(100) = 0.01$$

P(1)

$$= 0.04$$

either 4 or 5

↓

ex. 26

we have 4-pearson Mr (a, b, c, d), we selecte two from their

A = Mr a is to be receive apriase. *جائزہ*

B = either Mr a or Mr d but not both, *ایک لیا ہوگا*

S = {ab, ac, ad, bc, bd, cd} , n(S) = 6 or S = C₂⁴ = 6

A = {ab, ac, ad} , n(A) = 3 or P(A) = C₁³ / C₂⁴ = 3/6

P(A) = n(A) / n = 3/6

B = {(a,b), (a,c), (b,d), (c,d)} , n(B) = 4

P(B) = n(B) / n = 4/6 or P(B) = (C₁² · C₁²) / C₂⁴ = (C₁² · C₁² + C₁¹ · C₁³) / C₂⁴

P(B) = C₁² · C₁² + C₁¹ · C₁³

P(B) = (C₁² · C₁² + C₁¹ · C₁³) / C₂⁴ = 2/6

6
ex. 27.

We have (2, 5, 4) number and want to form it as 3-digit number
(i) What is the probability that the 3-digit number is even.

(ii) What is the prob. that the 3-digit number is divisible by 2.
odd.

(iii)

اذا اردنا ترتيبهم بشكل عشوائي

$n! = 3! = 6$

$S = \{245, 425, 452, 254, 524, 542\}$, $n(S) = 6$.

- A: the 3-digit number is even.
- B: the 3-digit number is divisible by 2
- C: the 3-digit number is odd.
- $A = \{254, 524, 452, 542\} \Rightarrow n(A) = 4$.

2	1	2
---	---	---

16

ex. 27.

We have (2, 5, 4) number and want to form it as

3-digit number (i) What is the probability that the 3-digit number is even.

(ii) what is the prob. that the 3-digit number is divisible by 2.

(iii)

اذا اردنا ترتيبهم بشكل عشوائي

→ $n! = 3! = 6$

$S = \{245, 425, 452, 254, 524, 542\}$, $n(S) = 6$.

A: the 3-digit number is even.

B: the 3-digit number is divisible by 2

C: the 3-digit number is odd.

$A = \{254, 542, 452, 524\} \Rightarrow n(A) = 4$

2	1	7
---	---	---

$$\therefore S = \{245, 425, 452, 524, \dots\}$$

A: the 3-digit number is even.

B: the 3-digit number is divisible by 2.

C: the 3-digit number is odd.

$$A = \{254, 524, 452, 524\} \Rightarrow n(A) = 4$$

2	1	2
---	---	---

$$2 \times 1 \times 2$$

$$P_2 \cdot P_2$$

$$\therefore P(A) = \frac{n(A)}{n(S)} = \frac{P_2 \cdot P_2}{3!}$$

$$= \frac{2! \cdot 2!}{3!} = \frac{4}{6}$$

$$\therefore \text{or } P(A) = \frac{n(A)}{n} = \frac{4}{6}$$

2	1	2
---	---	---

$$B = \{254, 524, 452, 524\}, n(B) = 4$$

$$P(B) = \frac{n(B)}{n} = \frac{4}{6}$$

3:

د) $P(A) = \frac{n(A)}{n} = \frac{4}{6}$

$B = \{254, 542, 452, 524\}$, $n(B) = 4$

$P(B) = \frac{n(B)}{n} = \frac{4}{6}$

$C = \{425, 245\}$, $n(C) = 2$

$P(C) = \frac{n(C)}{n} = \frac{2}{6}$

$n(C) = \frac{2}{6}$

①
د) $\begin{array}{|c|c|c|} \hline 2 & 1 & 1 \\ \hline \end{array}$
 $P_2 \cdot P_1$
 $2 \times 1 \times 1 = 2$