

Showm p. 45, ex. 3.6

ex. 2.8

A coin is weighted so that heads is twice as likely to appear as tails, find $P(T)$ and $P(H)$.

$$P(H) = 2P(T).$$

$$\text{Let } P(T) = p \text{ then}$$

$$P(H) = 2p.$$

$$\text{we have } \sum_{i=1}^n P(X_i) = 1. \text{ then}$$

$$P(H) + P(T) = 1.$$

$$2p + p = 1$$

$$3p = 1$$

$$p = \frac{1}{3}$$

قطعة تعود تم استبدالها كخيار
فإذا ظهرت صورة واحدة H
فإنها تعادل كتابتين
احتمال الصورة واحتمال الكتابين

دائمًا (1) نفرض العلاقة

(2) نخطئ جميع الاحتمالات = 1

(3) الخفضية 10

(4) نفرض لايجاد الاحتمالات في العلاقة

$$P(H) = 2p.$$

we have $\sum_{i=1}^n P(X_i) = 1$. then

$$P(H) + P(T) = 1.$$

$$2p + p = 1$$

$$3p = 1$$

$$\boxed{p = \frac{1}{3}}$$

then $P(T) = \frac{1}{3}$

and $P(H) = \frac{2}{3}$.

دائماً (1) تفرض العلاقة

(2) يخطئ مجموع الاحتمالات = 1

(3) تخمينية p .

(4) لغرض لايجاد الاحتمالات في العلاقة

(11)

③ P. 41. ex. 3.6 - Show.

Ex. Three horses A, B and C are in a race, A is twice likely to win as B and B is twice likely to win as C. What are their respective prob. of winning. (means find $p(A)$, $p(B)$ and $p(C)$.)

we have $p(A) = 2p(B) \rightarrow p(B) = 2p(C)$ then.

$$\text{Let } p(C) = \boxed{p}$$

$$\text{then } p(B) = \boxed{2p}$$

$$\text{and } p(A) = 2p(B) = 2(2p) = \boxed{4p}$$

Know the sum of prob. must be 1. hence.

$$p(A) + p(B) + p(C) = 1.$$

$$\Rightarrow 4p + 2p + p = 1$$

$$7p = 1$$

$$\boxed{p = \frac{1}{7}}$$

then $p(B) = \frac{2}{7}$ and $p(A) = \frac{4}{7}$

$$7P = 1$$

$$\boxed{P = \frac{1}{7}}$$

⇒

$$\text{then } P(C) = \frac{1}{7}, \quad P(B) = \frac{2}{7} \quad \text{and} \quad P(A) = \frac{4}{7}.$$

Q.P.

What is the prob. that B or C wins, if B and C mutually exclusive events.

$$P(B \cup C) = P(B) + P(C) - P(BC).$$

$$= \frac{2}{7} + \frac{1}{7} - 0.$$

$$= \boxed{\frac{3}{7}}$$

The letters $bbkkm$ are arranged in a row. What is the probability of

- (a) two b's come together.
- (b) no two b's come together.
- (c) no two b's come together and the last letter b.

$$n(S) = \frac{8!}{3!3!2!} = \frac{8 \cdot 7 \cdot 6 \cdot 5 \cdot 4 \cdot 3 \cdot 2 \cdot 1}{3 \cdot 2 \cdot 1 \cdot 3 \cdot 2 \cdot 1 \cdot 2 \cdot 1} = \boxed{560}$$

عدد طرق ترتيب الحروف
من حيث

[a] Let A: The event that we get arrangements have two b's come together.

$$n(A) = \frac{7!}{2!3!2!} = 210.$$

1 + 1 = 2
 $\boxed{bb} kkk m$
 $\frac{2!}{2} \cdot \frac{3!}{3} \cdot \frac{2!}{2}$
 والعدد

$$n(A) = 210 = \boxed{0.375}$$

$$n(A) = \frac{4!}{2!3!2!} = 210.$$

$$\Rightarrow P(A) = \frac{n(A)}{n(S)} = \frac{210}{5760} = \boxed{0.375}.$$

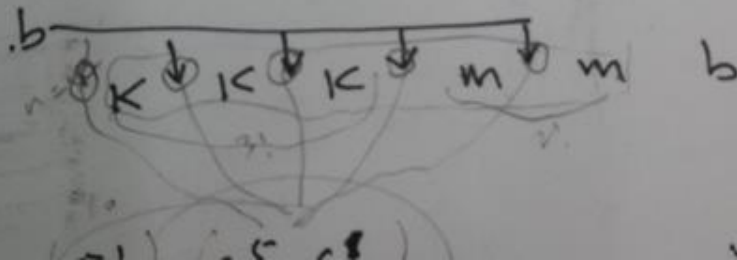
bb | b k k k m m
 2! | 3! | 2!
 2 | 6 | 2
 2 | 6 | 2
 والعدد

b)

[b] A^c is the complement of A .

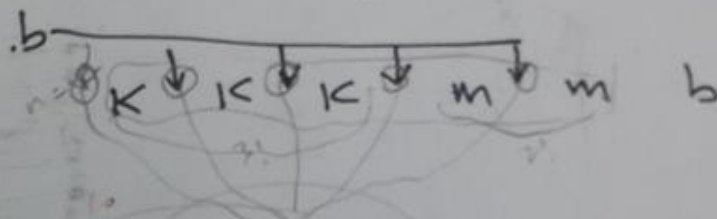
$$P(A^c) = 1 - P(A) = 1 - 0.375 = \boxed{0.625}$$

[c] Let B : the event that we get arrangements have two b's come together and the last letter



ب لا يكون سويم
 معناه يكون بي
 ك، ك، ك، م، م
 م، م
 ام عندهم لانه فان

ⓐ Let B : the event that we get arrangements have no two b 's come together and the last letter is b .



$$n(B) = \frac{5!}{3!2!} \cdot C_2^5 \cdot C_1^2 = 100.$$

$$\Rightarrow P(B) = \frac{100}{560}$$

$$\frac{5!}{3!2!} = \frac{5 \times 4 \times 3 \times 2 \times 1}{2 \times 2 \times 1 \times 1} = 10$$

ط لا يكون سوياً
معناه يكون بين
ك، ك، ك، م، م، م
أو م، م، م، ك، ك، ك
فدبت ط. C_1^2

وتمار من مسطرة 2 لتوزع مقيماً C_2^5

وعدد طرق توزع (السيارة) هو $\frac{n!}{n_1! n_2!}$

↓
 1 k k k m m
 k m m k k
 k k m m k
 m m k k k
 وهكذا...

The letters k h m m m j j are arranged in a row. What is the probability of $\frac{1}{3}$:

- (a) no two m's come together.
- (b) no two m's come together and the last letter is m.
- (c) two m's come together.

k h m m m j j

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$$\text{p.m.w} = \frac{9!}{4! 2! 2!} = \frac{3!}{2! 2! 2!} = \boxed{210}$$

(a) Let A: No two m's come together

⊕ h ⊕ h ⊕ j ⊕ m ⊕ m ⊕

$$n(A) = C_5^3 = \frac{5!}{2! 2!} = \frac{5 \cdot 4 \cdot 3 \cdot 2 \cdot 1}{2 \cdot 1 \cdot 2 \cdot 1} = \boxed{15}$$

$$P(A) = \frac{n(A)}{n} = \frac{15}{210} = \frac{1}{14}$$

a) Let A: No two m's come together

h h j j m

$$n(A) = \binom{5}{3} = \frac{5!}{3!2!} = \frac{5 \cdot 4 \cdot 3!}{3! \cdot 2 \cdot 1} = 10$$

$$\therefore P(A) = \frac{n(A)}{n(S)} = \frac{10}{210} = \frac{1}{21}$$

b) Let B: No two m's come together and the last letter

h h j j m

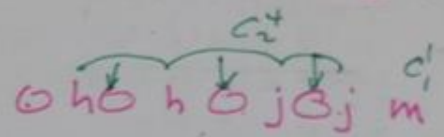
$$n(B) = \binom{4}{2} \cdot \binom{1}{1} = \frac{4!}{2!2!} = 6$$

$$P(B) = \frac{6}{210}$$

$$n(B) = \frac{4!}{2!2!} \cdot \binom{4}{2} \cdot \binom{1}{1} = 6 \cdot 6 = 36$$

ای
 ز ز ج ج
 ترکیبها به صورت
 h h j j
 j j h h
 h j h j

Can't be: No two m's come together and the last letter is m



$$n(B) = \frac{C_2^4 \cdot C_1^1}{2! \cdot 2!} \cdot \frac{4!}{2! \cdot 2!} = 36$$

$$P(B) = \frac{36}{210}$$

$$n(B) = \frac{4!}{2! \cdot 2!} \cdot C_2^4 \cdot C_1^1 = 6 \cdot 6 = 36$$

ترتيب الحروف

$$P(B) = \frac{36}{210}$$

- ترتيب
- h h z z
 - z z h h
 - h z z h
 - z h z h
 - h z h z
 - h z h z
- و ترتيب الحروف

C

$$n(C) = 2! \cdot 2! \cdot 2! = 2 \cdot 2 \cdot 2 = 8$$

$$n(C) = \frac{6!}{2! \cdot 2! \cdot 2!} = \frac{720}{8} = 90$$

$$P(C) = \frac{n(C)}{n(S)} = \frac{90}{210}$$

$$\frac{C_2^4 \cdot C_1^1}{2! \cdot 2!} \cdot C_2^4 \cdot C_1^1$$

$$\frac{4!}{2! \cdot 2!} \cdot C_2^4 \cdot C_1^1$$

و ترتيب الحروف