

(2)

(4) Inverse

$$1^{-1} = 1$$

$$\left(\frac{-1+i\sqrt{3}}{2}\right)^{-1} = \frac{-1-i\sqrt{3}}{2}$$

$$\left(\frac{-1-i\sqrt{3}}{2}\right)^{-1} = \frac{-1+i\sqrt{3}}{2}$$

$\therefore (G, \cdot)$  is group.

$$1 \cdot \frac{-1+i\sqrt{3}}{2} = \frac{-1+i\sqrt{3}}{2} \cdot 1$$

$\therefore a \cdot b = b \cdot a \quad \forall a, b \in G$

$\therefore (G, \cdot)$  is Comm. gp.

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Q/ state and prove cancellation laws theorem?

Solution: Let  $(G, \cdot)$  be a gp.  $\& a, b, c \in G$ :

① If  $a \cdot b = a \cdot c$ , then  $b = c$  (Left Canc. law)

② If  $b \cdot a = c \cdot a$ , then  $b = c$  (Right Canc. law)

Proof: ① Let  $a \cdot b = a \cdot c$

$\because a \in G$   $\& G$  is gp., so  $\exists a^{-1} \in G \exists$ .

$a \cdot a^{-1} = a^{-1} \cdot a = e$ . Thereby,

$$a^{-1} \cdot [a \cdot b = a \cdot c]$$

② By similar way.  $e \cdot b = e \cdot c \Rightarrow b = c$