

## CLINICAL PHARMACOKINETIC EQUATIONS AND CALCULATIONS

### 1- Intravenous Bolus Equation

$$C = (D/V)e^{-k_e t}$$

t = is the time after the intravenous bolus was given

C = is the concentration at time = t

V = is the volume of distribution

$k_e$  = is the elimination rate constant

$$t_{1/2} = 0.693/k_e$$

$C_0$  = concentration at time = 0

$$k_e = -(\ln C_1 - \ln C_2)/(t_1 - t_2)$$

$$V = D/C_0$$

$$C_0 = C/e^{-k_e t}$$

$C_0$  = concentration at time = 0

### 2-Continuous and Intermittent Intravenous Infusion Equations

$$C = (k_0/Cl)(1 - e^{-k_e t}) = [k_0/(k_e V)](1 - e^{-k_e t})$$

$k_0$  = the drug infusion rate (in amount per unit time, such as mg/h or  $\mu\text{g}/\text{min}$ ).

Cl = is the drug clearance.

[Since  $Cl = keV$ , this substitution was made in the second version of the equation]

$ke$  =is the eliminationrate constant

$t$  =is the time that the infusion has been running.

\*If the infusion is allowed to continue until steady state is achieved, the steady-state concentration ( $C_{ss}$ ) can be calculated easily:

$$C_{ss} = k_0 / Cl = k_0 / (keV).$$

\*If the infusion is stopped, post infusion serum concentrations ( $C_{postinfusion}$ ) can be computed

$$C_{postinfusion} = C_{end} e^{-ke t_{postinfusion}}$$

$$ke = -(\ln C_1 - \ln C_2) / (t_1 - t_2)$$

Where  $t_1$  and  $C_1$  are the first time/concentration pair and  $t_2$  and  $C_2$  are the second time/concentration pair;

$$V = \frac{k_0 (1 - e^{-ke t'})}{k_e [C_{max} - (C_{predose} e^{-ke t'})]}$$

- where  $k_0$  is the infusion rate
- $ke$  is the elimination rate constant
- $t'$  = infusion time
- $C_{max}$  is the maximum concentration at the end of infusion
- $C_{predose}$  is the predose concentration.

### 3- Extravascular Equation

$$C = \{(Fk_a D) / [V(k_a - k_e)]\} (e^{-k_e t} - e^{-k_a t})$$

Where  $t$  is the time after the extravascular dose was given ( $t = 0$  at the time the dose was administered)

$C$  =is the concentration at time =  $t$

$F$  =is the bioavailability fraction

$k_a$  =is the absorption rate constant

$D$  =is the dose

V= is the volume of distribution

$k_e$ = is the elimination rate constant.

\* When only postabsorption, postdistribution serum concentrations are obtained for a drug that is administered extravascularly, the equation simplifies to:

$$C = [(FD)/V]e^{-k_e t}$$

Where C is the concentration at any postabsorption, postdistribution time

F =is the bioavailability fraction

D= is the dose

V= is the volume of distribution

$k_e$ = is the elimination rate constant

t= is any postabsorption, postdistribution time.

$$k_e = - (\ln C_1 - \ln C_2) / (t_1 - t_2),$$

$$t_{1/2} = 0.693/k_e$$

$$C_0 = C/e^{-k_e t},$$

$$V/F = D/C_0$$

Where (V/F) volume of distribution/bioavailability constant

#### 4- Multiple-Dose and Steady-State Equations

In order to change a single dose equation to the multiple dose versions, it is necessary to multiply each exponential term in the equation by the multiple dosing factors:

$$(1 - e^{-nk_i\tau}) / (1 - e^{-k_i\tau})$$

Where n is the number of doses administered

$k_i$  =is the rate constant found in the exponential of the single dose equation

$\tau$  =is the dosage interval.

$$C = (D/V)[e^{-k_e t} / (1 - e^{-k_e \tau})]$$

Where C is the steady state concentration at any postdose time (t) after the dose (D) is given

V =is the volume of distribution

$k_e$ = is the elimination rate constant

$\tau$  =is the dosage interval.

TABLE 2-1 Single-Dose, Multiple-Dose, and Steady-State One-Compartment Model Equations

ROUTE OF ADMINISTRATION	SINGLE DOSE	MULTIPLE DOSE	STEADY STATE
Intravenous bolus	$C = (D/V)e^{-k_e t}$	$C = (D/V)e^{-k_e t} [(1 - e^{-nk_e \tau}) / (1 - e^{-k_e \tau})]$	$C = (D/V)[e^{-k_e t} / (1 - e^{-k_e \tau})]$
Continuous intravenous infusion	$C = [k_0 / (k_e V)](1 - e^{-k_e t})$	N/A	$C_{ss} = k_0 / Cl = k_0 / (k_e V)$
Intermittent intravenous infusion	$C = [k_0 / (k_e V)](1 - e^{-k_e t})$	$C = [k_0 / (k_e V)](1 - e^{-k_e t}) [(1 - e^{-nk_e \tau}) / (1 - e^{-k_e \tau})]$	$C = [k_0 / (k_e V)](1 - e^{-k_e t}) / (1 - e^{-k_e \tau})$
Extravascular (postabsorption, postdistribution)	$C = [(FD)/V]e^{-k_e t}$	$C = [(FD)/V]e^{-k_e t} [(1 - e^{-nk_e \tau}) / (1 - e^{-k_e \tau})]$	$C = (FD/V)[e^{-k_e t} / (1 - e^{-k_e \tau})]$
Average steady-state concentration (any route of administration)	N/A	N/A	$C_{ss} = [F(D/\tau)] / Cl$

Symbol key: C is drug serum concentration at time = t, D is dose, V is volume of distribution,  $k_e$  is the elimination rate constant, n is the number of administered doses,  $\tau$  is the dosage interval,  $k_0$  is the infusion rate, Cl is clearance,  $t'$  is infusion time, N/A is not applicable.

TABLE 2-2 Single-Dose, Multiple-Dose, and Steady-State Pharmacokinetic Constant Computations Utilizing a One Compartment Model

ROUTE OF ADMINISTRATION	SINGLE DOSE	MULTIPLE DOSE	STEADY STATE
Intravenous bolus	$k_e = -(\ln C_1 - \ln C_2) / (t_1 - t_2)$ $t_{1/2} = 0.693/k_e$ $V = D/C_0$ $Cl = k_e V$	$k_e = -(\ln C_1 - \ln C_2) / (t_1 - t_2)$ $t_{1/2} = 0.693/k_e$ $V = D / (C_0 - C_{pre-dose})$ $Cl = k_e V$	$k_e = -(\ln C_1 - \ln C_2) / (t_1 - t_2)$ $t_{1/2} = 0.693/k_e$ $V = D / (C_0 - C_{pre-dose})$ $Cl = k_e V$
Continuous intravenous infusion	N/A	N/A	$Cl = k_0 / C_{ss}$
Intermittent intravenous infusion	$k_e = -(\ln C_1 - \ln C_2) / (t_1 - t_2)$ $t_{1/2} = 0.693/k_e$ $V = [k_0(1 - e^{-k_e t'})] / [k_e[C_{max} - (C_{pre-dose}e^{-k_e t'})]]$ $Cl = k_e V$	$k_e = -(\ln C_1 - \ln C_2) / (t_1 - t_2)$ $t_{1/2} = 0.693/k_e$ $V = [k_0(1 - e^{-k_e t'})] / [k_e[C_{max} - (C_{pre-dose}e^{-k_e t'})]]$ $Cl = k_e V$	$k_e = -(\ln C_1 - \ln C_2) / (t_1 - t_2)$ $t_{1/2} = 0.693/k_e$ $V = [k_0(1 - e^{-k_e t'})] / [k_e[C_{max} - (C_{pre-dose}e^{-k_e t'})]]$ $Cl = k_e V$
Extravascular (postabsorption, postdistribution)	$k_e = -(\ln C_1 - \ln C_2) / (t_1 - t_2)$ $t_{1/2} = 0.693/k_e$ $V/F = D/C_0$ $Cl/F = k_e(V/F)$	$k_e = -(\ln C_1 - \ln C_2) / (t_1 - t_2)$ $t_{1/2} = 0.693/k_e$ $V/F = D / (C_0 - C_{pre-dose})$ $Cl/F = k_e(V/F)$	$k_e = -(\ln C_1 - \ln C_2) / (t_1 - t_2)$ $t_{1/2} = 0.693/k_e$ $V/F = D / (C_0 - C_{pre-dose})$ $Cl/F = k_e(V/F)$
Average steady-state concentration (any route of administration)	N/A	N/A	$Cl/F = (D/\tau) / C_{ss}$

Symbol key:  $C_1$  is drug serum concentration at time =  $t_1$ ,  $C_2$  is drug serum concentration at time =  $t_2$ ,  $k_e$  is the elimination rate constant,  $t_{1/2}$  is the half-life, V is the volume of distribution,  $k_0$  is the continuous infusion rate,  $t'$  is the infusion time, V/F is the hybrid constant volume of distribution/bioavailability fraction, D is dose,  $C_0$  is the concentration at time = 0, Cl is drug clearance, Cl/F is the hybrid constant clearance/bioavailability fraction,  $C_{pre-dose}$  is the predose concentration,  $C_{ss}$  is the steady-state concentration, N/A is not applicable.

### 5- Average Steady-State Concentration Equation

$$C_{ss} = [F(D/\tau)] / Cl$$

Where F is the bioavailability fraction

D = is the dose

$\tau$  = is the dosage interval

Cl = is the drug clearance

$$Cl/F = (D/\tau)/C_{ss}$$

Where D is dose and  $\tau$  is the dosage interval

## 6- DESIGNING INDIVIDUALIZED DOSAGE REGIMENS USING ONE COMPARTMENT MODEL EQUATIONS

**TABLE 2-3** Equations to Compute Individualized Dosage Regimens for Various Routes of Administration

ROUTE OF ADMINISTRATION	DOSAGE INTERVAL ( $\tau$ ), MAINTENANCE DOSE (D OR $k_0$ ), AND LOADING DOSE (LD) EQUATIONS
Intravenous bolus	$\tau = (\ln C_{ss_{max}} - \ln C_{ss_{min}})/k_e$ $D = C_{ss_{max}} V(1 - e^{-k_e\tau})$ $LD = C_{ss_{max}} V$
Continuous intravenous infusion	$k_0 = C_{ss} Cl = C_{ss} k_e V$ $LD = C_{ss} V$
Intermittent intravenous infusion	$\tau = [(\ln C_{ss_{max}} - \ln C_{ss_{min}})/k_e] + t'$ $k_0 = C_{ss_{max}} k_e V[(1 - e^{-k_e\tau})/(1 - e^{-k_e t'})]$ $LD = k_0/(1 - e^{-k_e\tau})$
Extravascular (postabsorption, postdistribution)	$\tau = [(\ln C_{ss_{max}} - \ln C_{ss_{min}})/k_e] + T_{max}$ $D = [(C_{ss_{max}} V)/F][(1 - e^{-k_e\tau})/e^{-k_e T_{max}}]$ $LD = (C_{ss_{max}} V)/F$
Average steady-state concentration (any route of administration)	$D = (C_{ss} Cl \tau)/F = (C_{ss} k_e V \tau)/F$ $LD = (C_{ss} V)/F$

Symbol key:  $C_{ss_{max}}$  and  $C_{ss_{min}}$  are the maximum and minimum steady-state concentrations,  $k_e$  is the elimination rate constant, V is the volume of distribution,  $C_{ss}$  is the steady-state concentration,  $k_0$  is the continuous infusion rate,  $t'$  is the infusion time,  $T_{max}$  is the time that  $C_{ss_{max}}$  occurs, F is the bioavailability fraction.

## 7- MULTICOMPARTMENT MODELS

The equation that describes a two compartment model after an intravenous bolus is:

$$[V_1(\alpha - \beta)]\{e^{-\alpha t} + \{[D(k_{21} - \beta)] / [V_1(\alpha - \beta)]\}e^{-\beta t}$$

Where C is the drug serum concentration,

D is the intravenous bolus dose

$k_{21}$  is the rate constant that describes the transfer of drug from compartment 2 to compartment 1

$\alpha$  is the distribution rate constant

$\beta$  is the elimination rate constant

$V_1$  is the volume of distribution for compartment 1

t is the time after the dose was administered.

**8-MICHAELIS-MENTEN EQUATIONS FOR SATURABLE PHARMACOKINETICS**

$$D = (V_{\max} \cdot C_{ss}) / (K_m + C_{ss})$$

Where D is the dose

$C_{ss}$  is the steady-state drug concentration

$V_{\max}$  is the maximum rate of drug metabolism

$K_m$  is the concentration where the rate of metabolism equals  $V_{\max}/2$ .

$$D = V_{\max} - [K_m(D/C_{ss})]$$

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