## mixing

- Is defined as a process that tends to result in a randomization of dissimilar particles within a system.
- 2 types of mixing 1- solid 2-fluid mixing
- Fluid mixing
- Fluids may generally depend on shear rate and shear stress
- The flow characteristics and mixing behavior of fluids are governed by 3 primary laws 1- conservation of mass 2conservation of energy 3-classic laws of motion

# Mixing mechanisms of fluids

1-bulk transport 2-turbulent flow

3-laminar flow 4-molecular diffusion

#### 1-Bulk transport

The movement of a relatively large portion of the material being mixed from one location in the system to another constitutes bulk transport. A simple circulation of material does not necessarily result in efficient mixing.

# 2-Turbulent mixing

• The phenomenon of turbulent mixing is a direct result of turbulent fluid flow which is characterized by a random fluctuation of the fluid velocity at any given point within the system. The fluid velocity at a given instant may be expressed as the vector sum of its components in the x,y and z directions. In the case on turbulent flow in a pipe, the mean velocity in the direction of flow through the pipe is positive, and varies some what depending on the distance from the pipe wall. Turbulent flow can be conveniently visualized as a composite of eddies of various sizes.

# eddy

Is defined as a portion of fluid moving as a unit in a direction often contrary to that of the general flow. Large eddies tend to break up forming eddies of smaller and smaller size until they are no longer distinguishable.

# **3-laminar mixing**

Streamline or laminar flow is frequently encountered when

1- highly viscous fluid are being processed. It can also occur if

2-stirring is relatively gentle &

3- may exist adjacent to stationary surface in vessels in which the flow predominantly turbulent.

 When 2 dissimilar liquids are mixed through laminar flow, the shear that is generated stretches the interface between them. If the mixer employed folds the layers back upon themselves, the no. of lavers & e th interfacial area betwee them hcre exponentially with пе

• This relationship is observed because the rate of increase in interfacial area with time is proportional to the instantaneous interfacial area. Example . Consider the case where the mixer produces a folding effect & generates a complete fold every 10 seconds. Given an initial fluid layer thickness of 10 cm a thickness reduction by a factor of 10<sup>-8</sup> is necessary to attain layers 1 nm thick, which approximate molecular dimensions. Since a single fold results in a layer thickness reduction of one half, n folds are required where

#### (1\2)<sup>n</sup> =10<sup>-8</sup>

#### n= 26.6

#### 10 X26.6=266 sec or 4.43 min

Good mixing at the molecular level requires a significant contribution by molecular diffusion after the layers have been reduced to reasonable thickness by laminar flow.

# 4- molecular diffusion

 The primary mechanism responsible for mixing at the molecular level is diffusion resulting from the thermal motion of the molecules when it occurs in conjunction with laminar flow, molecular diffusion tends to reduce the sharp discontinuities at the interface between the fluid layers and if allowed to proceed for sufficient time result in complete mixing.

# The process described by Fick's 1<sup>st</sup> law of diffusion

 $Dm\dt = -DA dc\dx$ 

D depends on the viscosity and the size of the diffusing molecules.

Conc. Gradients at the boundaries is a decreasing function of time, approaching zero as mixing completion.

The concentration gradient at the original boundaries is a deceasing function of time, approaching zero as mixing approaches completion

**Scale & intensity of segregation** 

Danckwerts has suggested 2 criteria to describe degree of mixing (quality of randomness or goodness of mixing)

**1-scale of segregation** 

**2-intensity of segregation** 

Scale segregation is expressed in 2 ways

Linear or volume scale

Linear scale represent an average value of diameter of the lumps where the volume scale represent the average lump volume.

Intensity of segregation is a measure of the <u>variation</u> in composition among the various portions of the mixtures.

When mixing is complete, the intensity of segregation is zero.



#### Time of mixing

## Equipment

Batch mixing –when the material to be mixed is limited in volume to that which may be conveniently contained in a suitable mixer.

System for batch mixing consist of 2 primary components:

1-tank which is suitable to hold the material being mixed

2-a means of supplying energy to the system

Power may be supplied to the fluid mass by means of an impellers ,air stream or liquid jet. Besides supplying power also are used to serve & direct flow

## 1- impellers

The distinction between impeller types is made on the basis of type of flow pattern they produce or on the basis of the shape and pitch of the blades. 3 basic types of flow may produced: radial, axial & tangential. These may occur singly or in various combinations.



FIG. 1-2. A and B, Diagrammatic representation of cylindric tanks in which tangential and radial flow occur, respectively. C, Side view of a similar tank in which axial flow occurs. These diagrams represent systems in which only one type of flow occurs, in contrast to the usual situation in which two or more of these flow patterns occur simultaneously.



FIG. 1-3. Impeller blade types (only one blade shown), top and side views. A and B, Radial flow design: C and D, mixed radial-axial flow design. For axial pumping, the blade must be set at an incline to the axis of the shaft.

# **Propeller**s: screw with blades (3 blades design)-blades pitch equal to the daimeter

Turbines are usually distinguished from propellers in that the blades of the latter do not have a constant pitch throughout their length. When radial-tangential flow is desired, turbines with

Paddles also are employed as impellers and are normally operated at low speeds, 50 rpm or less. Their blades have a large surface area in relation to the tank in which they are employed, a feature that permits them to pass close to the tank walls and effectively mix viscous liquids or semisolids, which tend to cling to these surfaces. Circulation is primarily tangential, and consequently, concentration gradients in the axial and radial directions may persist in this type of mixer even after prolonged operation. Operating procedures should take these characteristics into account so as to minimize their

# 2-Air jet

 Subsurface jets of air or less commonly of some other gas, are effective mixing devices for certain liquids. The liquids must be of low viscosity, non foaming, unreactive with the gas employed & reasonably non volatile. the jets are arranged so that the buoyancy of the bubbles lifts liquid from the bottom to the top of the mixing vessel brings fluid from all parts of the tank to the region of the jet. This is accomplished with a draft tubes. These serve to confine the expanding hubbles and



FIG. 1-4. Vertical tank with centrally located air jet and draft tube. Bubbles confined within the draft tube rise, inducing an upward fluid flow in the tube. This flow tends to circulate fluid in the tank, bringing it into the turbulent region in the vicinity of the jet.

## 3-Fluid jets

When liquids are to be pumped into a tank for mixing .

The fluids are pumped through nozzles arranged to permit good circulation of material throughout the tank, like propellers, they generate turbulent flow in the direction of their axes.

## 4- Baffles

For bulk fluid flow to be most effective ,an intermingling must occur between material from remote regions in the mixer. To accomplish this , it is frequently necessary to install auxiliary devices for directing the flow of the fluid, usually baffles plates.

# **Continuous mixing**

- The process of continuous mixing produces an uninterrupted supply of freshly mixed material & is often desirable when very large volumes of material are to be handled. It can be accomplished in 2 ways
- 1-in a tube or pipe through which the material flows & in which there is a little back flow or recirculation
- 2- in chamber in which a considerable amount of holdup & recirculation.
- to ensure good mixing efficiency, such



**FIG. 1-5.** Continuous fluids mixing devices. A, Baffled pipe mixer; B, mixing chamber with flow induced recirculation. Both types induce turbulence in the fluid; however, recirculation is desirable when overall fluctuations occur in the material fed to the mixer, since these fluctuations will not be eliminated by simple transverse mixing in a pipe.

### **Mixer selection---equipment selection**

Factors that must be taken into consideration include

- 1-the physical properties of the materials to be mixed such as the density, viscosity and miscibility
- 2-Economic considerations regarding processing ex. time required for mixing and the power expenditure necessary.3- cost of the equipment and its maintenance.

# Mixer selection---equipment selection

 1- monophase system : fluids of relatively low viscosity are best mixed by method that generate a high degree of turbulence & at the same time circulate the entire mass of material. These requirements are satisfied by air jets, fluid jets & the various high speed impellers. A viscosity of approximately 10 poise may be considered as a practical upper limit for the application of these devices.

Thick creams & ointments & pastes are of such high viscosity that is difficult if not impossible to generate turbulence within their bulk & laminar. Mixing may be done with a turbine of

# 2-poly phase system

- The mixing of 2 immiscible liquids requires the subdivision of one of these phases into globules, then distributed throughout the bulk of the fluid. These globules are successively broken down into smaller one. 2 primary forces play here: 1-the interfacial tension of the globules in the surrounding liquid and 2- forces of shear within the fluid mass. The first force tends to resist the distortion of globule shape fragmentation to small globule where the opposite with the 2<sup>nd</sup> force.
- The selection of equipment depends upon the viscosity of the liquids and this is made according to the mechanism by which intense shearing

Highly viscous fluids such as are approximatered in the

Highly viscous fluids such as are encountered in the production of ointments, are efficiently dispersed by the shearing action of 2 surfaces in close proximity and moving at different velocities with respect to each other. This is achieved in paddle mixers in which the blades clear out the walls. These mixers generate shear to reduce globule size and induce sufficient circulation of materials to ensure efficient mixing.

- the mixing of finely divided solids with a liquid of low viscosity in the production of a suspension depends on the separation of aggregates & distribution of these particles in the fluid. This process occurs in a single mixing operation provided that shear forces of sufficient to disrupt aggregates.
- As the % of solids is increased or if highly viscous fluids are employed, the solid – liquid system takes on the consistency of a paste or dough. The choice of mixer is either knead or mull the materials. Kneaders operate by pushing of the material by squeezing & deforming them at the same time. Such mixers take several forms.
- Usually have counter rotating blades or heavy arms that work the plastic mass. Shear forces are generated

# Sigma blade mixer with overlapping blades



FIG. 1-8. Schematic drawing of a top-loading sigma-blade mixer with overlapping blades. The top view shows the relationship of the counter rotating blades to the overall geometry of the mixer.

- Mulling mixer are efficient in deaggregation of solids, but are inefficient in distributing the particles uniformly through the entire mass. Previously mixed material of uniform composition, but containing aggregates of solid particles. In the events of segregation during mulling, a final remixing may be necessary.
- The 3 roll type are preferred.
- In operation rollers composed of a hard abrasion resistant material & arranged to come into close proximity to each other are rotated at different rates of speed. Material

# 3-roll mill

 The material passes from the hopper A between rolls B & C & is reduced in size in the process. The gap between rolls C & D which is less than that between B & C, further crushes & smooths the mixture which adheres to roll C. A scraper E is arranged to continuously remove the mixed material from roller D.



**FIG. 1-9.** Cross section of a three-roll mill showing hopper (A), rolls (B,C,D), and scraper (E). Directions of roller rotation are indicated. Speed of rotation of the rollers increases from B to D. Material placed in the hopper passes between rolls B and C and then C and D in succession and is finally collected on the scraper.

# Solid – liquid mixing

• In which a small volume of liquid is to be mixed with a large quantity of solids. This process is one of coating the solid particles with liquid & of the transfer of liquid from one particle to another. The liquid is added slowly to reduce the tendency of the particles to lump. But when the particles tend to stick together because of surface tension of the coating liquids, the equipment used is the same as that for pastes. If the solids remain essentially free **Particulate Solids Variables.** Particle size and particle size distribution are important since they largely determine the magnitude of forces, gravitational and inertial, that can cause interparticulate movement relative to surface forces, which resist such motion. As a consequence of high interparticulate forces, as compared with gravitational forces, few powders of less than 100 microns mean particle size are free-flowing. Most powders, including those encountered in pharmaceutical systems, have a wide range in particle size with the actual distribution determined to some extent by the method of preparaParticle density, elasticity, surface roughness, and shape also exert their influence on the bulk properties of powders. Of these, particle shape is perhaps the most difficult variable to describe and is commonly expressed by scalar quantities known as shape factors. When applied to solids mixing, shape factors provide a number index to which mixing rate, flow rate, segregation rate, angle of repose, and other static or dynamic characteristics can be related. However, the limitations as well as the attributes of shape factors should be understood.

As scalar quantities, shape factors serve as proportionality constants between mean particle diameters and particle surface area and volume. They also serve to relate results of experimental particle size measurements by different methods. In spite of their utility in these ways, shape factors do not describe the shape of the particles they characterize. Thus, a single factor can in no
way be considered a unique indication of shape. For example, one cannot differentiate between rods and flat discs by the use of a single shape factor. This limitation somewhat complicates correlations and interpretations of particulate shape effects on mixing.

A large number of shape factors have been defined and used in studies of multiparticulate solids systems. A typical example is that of a surface shape factor,  $\alpha_s$ , defined by the expression:

$$\alpha_{\rm s} = \frac{\rm s}{\Sigma n_{\rm i} {\rm d_i}^2} \tag{11}$$

The total surface area of the powder is s, having  $n_i$  particles of projected diameter  $d_i$ . Powders whose particles are highly irregular in shape generally exhibit large values of  $\alpha_s$ .

*Example.* To calculate a value of  $\alpha_s$  that is useful for purposes of comparison with other materials, consider a system of monodisperse spheres of diameter 2r. The surface shape factor  $\alpha_s$  will be independent of sample size, so that for simplicity, a single particle will be taken as the sample. In this case, equation (11) takes the form.

$$\alpha_{\rm s} = \frac{4\pi r^2}{(2r)^2} = \pi$$

Had the idealized particles been perfect cubes, having edges of length d, then equation (11) would become:

$$\alpha_{\rm s} = \frac{6d^2}{d^2} = 6$$

The value for  $\alpha_s$  can be seen to increase substantially as the particles become more angular and deviate from a spherical shape.

Forces Acting in Multiparticulate Solids **Systems.** As pointed out previously, forces that operate at a particulate level during the mixing process are essentially of two types: (1) those that tend to result in movement of two adjacent particles or groups of particles relative to each other and (2) those that tend to hold neighboring particles in a fixed relative position. This division is arbitrary, and often a clear distinction cannot be made, for reasons that will become evident.

In the first category are forces of acceleration produced by the translational and rotational movements of single particles or groups of particles. Such motion can result either from contact with the mixer surfaces or from contact with other particles. In either case, the efficiency of momentum transfer is highly dependent on the

elasticity of the collisions.

Gravitational forces also operate and, of course, act on all particles at all times in proportion to their mass.

Included in the second category of forces, namely those that resist particulate movement, are interparticulate interactions associated with the size, shape, and surface characteristics of the particles themselves. Powders that have high "cohesive" forces due to interaction of their surfaces can be expected to be more resistant to intimate mixing than those whose surfaces do not interact strongly. Factors that influence this type of interaction are surface polarity, surface charge, and adsorbed substances such as moisture.

In moving from one location to another, relative to its neighbors, a particle must surmount certain potential energy barriers. These arise from forces resisting movement insofar as neighboring particles must be displaced. This effect is a function of both particle size and shape and is most pronounced when high packing densities occur. Particle shape is important because as the shape of a particle deviates more significantly from a spherical form, the free movement it experiences along its major axes also diverges.

### solid -solid mixing mechanisms

 1-convective mixing is an analogous to bulk transport. This mixing can occur by an inversion of the powder bed by means of 1blades or paddles, 2- revolving screw or by any method of moving a relatively large mass of material from one part of the powder bed to another.

# 2-shear mixing

 As a result of forces within the particulate mass, slip planes are set up and this give rise to laminar flow. When shear occurs between regions of different composition & parallel to their interface, it reduces the scale of segregation by thinning the dissimilar layers.

# 3-Diffusive mixing by diffusion

 When random motion of particles within a powder bed causes them to change position relative to one another. Such an exchange of positions by single particles result in a reduction of the intensity of segregation. Diffusive mixing occurs at the interfaces of dissimilar regions that are undergoing shear & therefore results from shear mixing.

The mixing of particles whose surfaces are nonconducting (electrically) often results in the generation of surface charges, as evidenced by a tendency of the powder to clump following a period of agitation. Surface charging of particles during mixing is undesirable, for it tends to decrease the process of interparticulate "diffusion." Charging of powder beds and the undesirable effects it produces can be prevented or reduced in many cases by surface treatment, which is usually accomplished by adding small amounts of surfactants to the powder, thereby increasing the conductivity of the surface. The problem can also be solved in some cases by mixing under conditions of increased humidity (above 40%).

# Segregation mechanisms

- The requirements for segregation
- 1-differences in mixture components mobilities can result from differences in particle sizes, shape, density, & surface characteristics.
- 2-segregation can be met by the earth's gravitational field or by centrifugal .electrical, magnetic field generated in the course of processing.

 Particulate solids tend to segregate by virtue of differences in the size, density, shape & other properties of particles. The process of segregation occurs during mixing & during subsequent handling of the completed mix, & it is pronounced with free flowing powders. Powders that are not free flowing or exhibit high forces of cohesion or adhesion between particles of similar or dissimilar composition are difficult to mix owing to agglomeration.

 The clumps of particles can be broken down by the use of 1- mixers that generate high shear forces or 2- subject the powder to impact.

### Equipment ---batch mixing

- Common type of mixer consists of a container of one of several geometric forms which is mounted so that it can be rotated about an axis. The resulting tumbling motion accentuated by means of baffles or simply by virtue of the shape of the container.
- The popular twin shell blender is of this type & takes the form of a cylinder that has been cut in half. At approximately a 45- degree angle with its long axis & then joined to form a V shape. This is retated so that the material is

In the bottom of the V is inverted. This is effective because the bulk transport & shear which occur in tumbling mixers .

Other mixers take the form of cylinders , cubes or hexagonal cylinders & may be rotated about almost any axis .

### 1- tumbler



**FIG. 1-11.** Three types of tumbling mixers shown mounted on a common shaft: A, twin-shell; B, cubic; C, cylindric. In operation, the asymmetric geometry results in a sideways movement of material in addition to the tumbling action of the mixers. Of the three types, the twinshell is the most popular.

The efficiency of tumbling mixers is highly dependent on the speed of rotation .

#### Rotation is too slow

• Does not produce the desired intense tumbling or cascading motion.

#### Rotation is too rapid

 Tends to produce centrifugal force sufficient to hold the powder to the sides of mixers & thereby reduce the efficiency.

- The optimum rate of rotation depends on the size & shape of the tumbler & also on the type of material being mixed but is commonly in the range of 30 to 100 rpm.
- 2<sup>nd</sup> class of mixers employs a stationary container to hold the material & brings about mixing by means of moving screws, paddles or blades.

### Stationary mixers

Does not depend on gravity

It is useful in mixing solids that have been wetted

The high shear forces are effective in breaking up lumps or aggregates.

### Well known mixers are

- 1-the ribbon blender consists of horizontal cylindric tank usually opening at the top & fitted with helical blades which mounted on a shaft through the long axis of the tank & are often of both sided right & left hand twist.
- 2- in the helical flight mixer powders are lifted by a centrally located vertical screw & allowed to cascade to the bottom of the tank.

### Ribbon blender



FIG. 1-12. Side view of a top-loading ribbon blender. The blades are mounted on the horizontal axle by struts (not shown) and are rotated to circulate the material to be mixed. The spiral blades are wound (in most cases) in opposite directions to provide for movement of material in both directions along the axis of the tank. These mixers may be emptied either through ports in the bottom or by inverting them.