## Chapter 11

## Isotonic solutions

Objectives
Upon successful completion of this chapter, the student will be able to:

1. Calculate the dissolution factor (i) of a chemical agent .
2. Calculate the sodium chlorid equivealnt ( E - valu) of a chemical agent
3. Perform calculation required in the preparation of isotonic solution.

## Lecture 3

When a solvent passes through a semipermeable membrane from a dilute solution into a more concentrated one, the concentrations become equalized and the phenomenon is known as osmosis.


Osmosis
The pressure responsible or this phenomenon is termed osmotic pressure and varies with the nature of the solute.
> If the solute is a nonelectrolyte, its solution contains only molecules and the osmotic pressure varies with the concentration o the solute.
$>$ If the solute is an electrolyte, its solution contains ions and the osmotic pressure varies with both the concentration of the solute and its degree o dissociation.

Thus, solutes that dissociate present a greater number of particles in solution and exert a greater osmotic pressure than undissociated molecules.

Two solutions that have the same osmotic pressure are termed isosmotic

Many solutions intended to be mixed with body fluids are designed to have the same osmotic pressure for greater patient comfort, efficacy, and safety.

A solution having the same osmotic pressure as a specific body fluid is termed isotonic (meaning of equal tone) with that specific body fluid.

Solutions of lower osmotic pressure than that of a body fluid are termed hypotonic.
A solution having a higher osmotic pressure than that of a body fluid are termed hypertonic.

Pharmaceutical dosage forms intended to be added directly to the blood or mixed with biological fluids of the eye, nose, and bowel are of principal concern to the pharmacist in their preparation and clinical application.


## Special Clinical Considerations of Tonicity

It is generally accepted that for ophthalmic and parenteral administration, isotonic solutions are better tolerated by the patient than those at the extremes of hypo- and hypertonicity.

With the administration of an isotonic solution, there is a homeostasis with the body's intracellular fluids. Thus, in most instances, preparations that are isotonic, or nearly so, are preferred.

However, there are exceptions, as in instances in which hypertonic solutions are used to "draw" fluids out of edematous tissues and into the administered solution.

Most ophthalmic preparations are:

1. Formulated to be isotonic, or approximately isotonic, to duplicate ophthalmic tears or the comfort of the patient.
2. These solutions are also prepared and buffered at an appropriate pH .

Both to reduce the likelihood of irritation to the eye's tissues and to maintain the stability o the preparations.

Injections that are not isotonic should be administered slowly and in small quantities to minimize tissue irritation, pain, and cell fluid imbalance.
$>$ The tonicity of small volume injections is generally unimportant when added to large-volume parenteral infusions because of the presence of tonic substances, such as sodium chloride or dextrose in the largevolume infusion, which serve to adjust the tonicity o the smaller added volume.

Intravenous infusions, which are hypotonic or hypertonic, can have profound adverse effects because they generally are administered in large volumes.
$>$ Large volumes of hypertonic infusions containing dextrose, or example, can result in hyperglycemia, osmotic diuresis, and excessive loss of electrolytes.
$>$ Excess infusions of hypotonic fluids can result in the osmotic hemolysis of red blood cells and surpass the upper limits of the body's capacity to safely absorb excessive fluids.
$>$ Isotonic fluids, when in used intravenously in excessive volumes or at excessive rates, can be deleterious due to an overload of fluids placed into the body's circulatory system.



## Physical/Chemical Considerations in the Preparation of Isotonic Solutions

The calculations involved in preparing isotonic solutions may be made in terms of data relating to the colligative properties of solutions.

Theoretically, any one of these properties may be used as a basis or determining tonicity. Practically and most conveniently, a comparison of freezing points is used or this purpose.

It is generally accepted that $-0.52^{\circ} \mathrm{C}$ is the freezing point of both blood serum and lacrimal fluid.

## Nonelectrolyte

When 1 g molecular weight of any nonelectrolyte, that is, a substance with negligible dissociation, such as boric acid, is dissolved in 1000 g of water, the freezing point of the solution is about $1.86^{\circ} \mathrm{C}$ below the freezing point of pure water.

By simple proportion, therefore, we can calculate the weight of any nonelectrolyte that should be dissolved in each 1000 g of water in the solution is to be isotonic with body fluids.

Boric acid, or example, has a molecular weight of 61.8 ; thus (in theory), 61.8 g in 1000 g of water should produce a freezing point of $-\mathbf{1 . 8 6}{ }^{\circ} \mathrm{C}$. There ore:

$$
\begin{aligned}
\frac{1.86\left({ }^{\circ} \mathrm{C}\right)}{0.52\left({ }^{\circ} \mathrm{C}\right)} & =\frac{61.8(\mathrm{~g})}{\mathrm{x}(\mathrm{~g})} \\
\mathrm{x} & =17.3 \mathrm{~g}
\end{aligned}
$$

In short, 17.3 g of boric acid in 1000 g o water, having a weight-in-volume strength o approximately $1.73 \%$, should make a solution isotonic with lacrimal fluid.

## Electrolyte

With electrolytes, because osmotic pressure depends more on the number of particles, substances that dissociate have a tonic effect that increases with the degree of dissociation; the greater the dissociation, the smaller the quantity required to produce any given osmotic pressure.

If we assume that sodium chloride in weak solutions is about $\mathbf{8 0 \%}$ dissociated, then each 100 molecules yields 180 particles, or 1.8 times as many particles as are yielded by 100 molecules of a nonelectrolyte

- This dissociation factor, commonly symbolized by the letter $\boldsymbol{i}$, must be included in the proportion when we seek to determine the strength of an isotonic solution of sodium chloride (m.w. 58.5):

$$
\begin{aligned}
\frac{1.86\left({ }^{\circ} \mathrm{C}\right) \times 1.8}{0.52\left({ }^{\circ} \mathrm{C}\right)} & =\frac{58.5(\mathrm{~g})}{\mathrm{x}(\mathrm{~g})} \\
\mathrm{x} & =9.09 \mathrm{~g}
\end{aligned}
$$

Hence, 9.09 g of sodium chloride in 1000 g of water should make a solution isotonic with blood or lacrimal fluid.

In practice, a $0.9 \% \mathrm{w} / \mathrm{v}$ sodium chloride solution is considered isotonic with body fluids.

Simple isotonic solutions may then be calculated by using this formula:

$$
\frac{0.52 \times \text { molecular weight }}{1.86 \times \text { dissociation }(i)}=\mathrm{g} \text { of solute per } 1000 \mathrm{~g} \text { of water }
$$

The value of $\boldsymbol{i}$ for many medicinal salts has not been experimentally determined. Some salts are exceptional (such as zinc sulfate, with only $40 \%$ dissociation and an $i$ value therefore of 1.4), but most medicinal salts approximate the dissociation of sodium chloride in weak solutions.

If the number of ions is known, we may use the following values, lacking better information:
$\checkmark$ Nonelectrolytes and substances of slight dissociation: 1.0
$\checkmark$ Substances that dissociate into 2 ions: 1.8
$\checkmark$ Substances that dissociate into 3 ions: 2.6
$\checkmark$ Substances that dissociate into 4 ions: 3.4
$\checkmark$ Substances that dissociate into 5 ions: 4.2

## Example Calculations of the $i$ Factor

Zinc sulfate is a 2-ion electrolyte, dissociating 40\% in a certain concentration. Calculate its dissociation (i) factor.

On the basis of $40 \%$ dissociation, 100 particles of zinc sulfate will yield:
40 zinc ions
40 sulfate ions
60 undissociated particles
or 140 particles
Because 140 particles represent 1.4 times as many particles as were present before dissociation, the dissociation (i) factor is 1.4

Zinc chloride is a 3-ion electrolyte, dissociating 80\% in a certain concentration. Calculate its dissociation (i) factor.

On the basis of $80 \%$ dissociation, 100 particles of zinc chloride will yield:
80 zinc ions
80 chloride ions
80 chloride ions
20 undissociated particles
or 260 particles
Because 260 particles represents 2.6 times as many particles as were present before dissociation, the dissociation (i) factor is 2.6.

## Lecture 4

## Sodium chloride equivalent

A special problem arises when a prescription directs us to make a solution isotonic by adding the proper amount of a tonicity agent (such as sodium chloride or boric acid) to the solution containing the active ingredient.
$>$ Given a $0.5 \% \mathrm{w} / \mathrm{v}$ solution of sodium chloride, we may easily calculate that :
$0.9 \mathrm{~g}-0.5 \mathrm{~g}=0.4 \mathrm{~g}$ of additional sodium chloride that should be contained in each 100 mL if the solution is to be made isotonic with a body fluid.

But how much sodium chloride should be used in preparing 100 mL of a $1 \% \mathrm{w} / \mathrm{v}$ solution of atropine sulfate, which is to be made isotonic with lacrimal fluid?

The answer depends on how much sodium chloride is in effect represented by the atropine sulfate.

The relative tonic effect of two substances that is, the quantity of one that is equivalent in tonic effects to a given quantity of the other may be calculated if the quantity of one having a certain effect in a specified quantity of solvent is divided by the quantity of the other having the same effect in the same quantity of solvent

For example, we calculated that 17.3 g of boric acid per 1000 g of water and 9.09 g of sodium chloride per 1000 g of water are both instrumental in making an aqueous solution isotonic with lacrimal fluid.
If, however, 17.3 g of boric acid are equivalent in tonicity to 9.09 g of sodium chloride, then 1 g of boric acid must be the equivalent of
$17.3 \mathrm{~g} \quad 9.09 \mathrm{~g}$
1 g
x
$\mathrm{X}=9.09 \mathrm{~g} \div 17.3 \mathrm{~g}$ or 0.52 g of sodium chloride.

Similarly, 1 g of sodium chloride must be the "tonicic equivalent" of $17.3 \mathrm{~g} \div 9.09 \mathrm{~g}$ or 1.9 g of boric acid.

We have seen that one quantity of any substance should in theory have a constant tonic effect if dissolved in 1000 g of water: $\mathbf{1} \mathbf{g}$ molecular weight of the substance divided by its $\boldsymbol{i}$ or dissociation value.

Hence, the relative quantity of sodium chloride that is the tonicic equivalent of a quantity of boric acid may be calculated by these ratios:

$$
\frac{58.5 \div 1.8}{61.8 \div 1.0} \text { or } \frac{58.5 \times 1.0}{61.8 \times 1.8}
$$

and we can formulate a convenient rule: quantities of two substances that are tonicic equivalents are proportional to the molecular weights of each multiplied by the i value of the other.

To return to the problem involving 1 g of atropine sulfate in 100 mL of solution:
Molecular weight of sodium chloride $=58.5 ; i=1.8$
Molecular weight of atropine sulfate $=695 ; i=2.6$

$$
\begin{aligned}
\frac{695 \times 1.8}{58.5 \times 2.6} & =\frac{1(\mathrm{~g})}{\mathrm{x}(\mathrm{~g})} \\
\mathrm{x} & =0.12 \mathrm{~g} \text { of sodium chloride represented by } \\
& 1 \mathrm{~g} \text { of atropine sulfate }
\end{aligned}
$$

Therefore, the sodium chloride equivalent, or $E$-value, of atropine sulfate is 0.12 .

Because a solution isotonic with lacrimal fluid should contain the equivalent of 0.9 g of sodium chloride in each 100 mL of solution, the difference to be added must be
$0.9 \mathrm{~g}-0.12 \mathrm{~g}=0.78 \mathrm{~g}$ of sodium chloride.

Rearranging the information for calculating the $E$-value of boric acid or atropine sulfate, the following equation can be used to calculate the sodium chloride equivalent of any substance:

| $\frac{\text { Molecular weight of sodium chloride }}{i \text { Factor of sodium chloride }}$ | $\times \frac{i \text { factor of the substance }}{\text { Molecular weight of the substance }}$ |
| ---: | :--- |
|  | $=$ Sodium chloride equivalent |


| Substance | molecular Weight | Ions | Sodium Chloride equivalent <br> $(\text { e-value })^{\text {a }}$ |
| :--- | :---: | :---: | :---: |
| Antipyrine | 188 | 1 | 0.17 |
| Atropine sulfate $\cdot \mathrm{H}_{2} \mathrm{O}$ | 695 | 3 | 0.12 |
| Benoxinate hydrochloride | 345 | 2 | 0.17 |
| Benzalkonium chloride | 360 | 2 | 0.16 |
| Benzyl alcohol | 108 | 1 | 0.17 |
| Boric acid | 61.8 | 1 | 0.52 |
| Brimonidine tartrate | 442 | 2 | 0.13 |
| Chlorobutanol | 177 | 1 | 0.24 |
| Cocaine hydrochloride | 340 | 2 | 0.17 |
| Cromolyn sodium | 512 | 2 | 0.14 |
| Cyclopentolate hydrochloride | 328 | 2 | 0.18 |
| Demecarium bromide | 717 | 3 | 0.12 |
| Dextrose (anhydrous) | 180 | 1 | 0.18 |
| Dextrose $\cdot \mathrm{H}_{2} \mathrm{O}$ | 198 | 1 | 0.16 |
| Ephedrine hydrochloride | 202 | 2 | 0.29 |
| Ephedrine sulfate | 429 | 3 | 0.2 |
| Epinephrine bitartrate | 333 | 2 | 0.18 |
| Fluorescein sodium | 376 | 3 | 0.31 |

Table 11.1 gives the sodium chloride equivalents ( E values) of each of the substances listed. These values were calculated according to the rule stated previously.

If the number of grams of a substance included in a prescription is multiplied by its sodium chloride equivalent, the amount of sodium chloride represented by that substance is determined.

## Example Calculations of the Sodium Chloride Equivalent (E-values)

Papaverine hydrochloride (m.w. 376) is a 2-ion electrolyte, dissociating 80\% in a given concentration. Calculate its sodium chloride equivalent.

Because papaverine hydrochloride is a 2-ion electrolyte, dissociating $80 \%$, its $i$ factor is 1.8.

$$
\begin{aligned}
\frac{\text { Molecular weight of sodium chloride }}{i \text { Factor of sodium chloride }} & \times \frac{i \text { factor of the substance }}{\text { Molecular weight of the substance }} \\
& =\text { Sodium chloride equivalent }
\end{aligned}
$$

$$
\frac{58.5}{1.8} \times \frac{1.8}{376}=0.16
$$

Calculate the sodium chloride equivalent for glycerin, a nonelectrolyte with a molecular weight of 92.
Glycerin, $i$ factor $=1.0$

$$
\frac{58.5}{1.8} \times \frac{1.0}{92}=0.35
$$

Calculate the sodium chloride equivalent or timolol maleate (TIMOPTIC), which dissociates into two ions and has a molecular weight of 432.

Timolol maleate, $i$ factor $=1.8$

$$
\frac{58.5}{1.8} \times \frac{1.8}{432}=0.14
$$

Calculate the sodium chloride equivalent or fuorescein sodium, which dissociates into three ions and has a molecular weight of 376 .

Fluorescein sodium, $i$ factor $=2.6$

$$
\frac{58.5}{1.8} \times \frac{2.6}{376}=0.22
$$

Note that the calculated value differs from the value in Table 11.1 ( 0.31 ). This is most likely due to using the general dissociation factor of 2.6 rather than the specific dissociation factor or fluorescein sodium. The value reported in Table 11.1 is an experimentally determined value.

The agent brimonidine tartrate (ALPHAGAN P) has a molecular weight of 442 and dissociates into two ions when in solution. It is used as a $0.1 \%$ ophthalmic solution in the treatment of glaucoma. Calculate
(a) the sodium chloride equivalent of brimonidine tartrate
(b) whether, without additional formulation agents, a $0.1 \%$ solution would be isotonic, hypotonic, or hypertonic with tears.

$$
\text { (a) } \frac{58.5}{1.8} \times \frac{1.8}{442}=\mathbf{0 . 1 3} \text { sodium chloride equivalent }
$$

(b) Arbitrarily select a volume of solution as a basis or the calculation.

The commercial product is available in $\mathbf{1 0} \mathbf{- m L}$ containers, so that volume would be a good choice.
For isotonicity, a $10-\mathrm{mL}$ volume would require the following amount of sodium chloride or its equivalent:
$10 \mathrm{~mL} \times 0.9 \% \mathrm{w} / \mathrm{v}=0.09 \mathrm{~g}$ sodium chloride or its equivalent
A $10-\mathrm{mL}$ volume of a $0.1 \% \mathrm{w} / \mathrm{v}$ solution of brimonidine tartrate would contain $10 \mathrm{~mL} \times 0.1 \% \mathrm{w} / \mathrm{v}=0.01 \mathrm{~g}$ brimonidine tartrate
Applying the sodium chloride equivalent (0.13):
0.01 g brimonidine tartrate $\times 0.13=0.0013 \mathrm{~g}$ of sodium chloride equivalence

Thus, this solution would be hypotonic.

If 1 g of epinephrine bitartrate, when dissolved in water, prepares 20 mL of an isotonic solution, calculate its sodium chloride equivalent.

20 mL of an isotonic sodium chloride solution would be calculated by
$20 \mathrm{~mL} \times 0.9 \% \mathrm{w} / \mathrm{v}=0.18 \mathrm{~g}$ sodium chloride (in 20 mL of solution)
Therefore, 1 g of epinephrine bitartrate is equal in tonic effect to 0.18 g sodium chloride, and thus, its sodium chloride equivalent is 0.18 .

The procedure for the calculation of isotonic solutions with sodium chloride equivalents may be outlined as follows:

Step 1. Calculate the amount of sodium chloride represented by each ingredient in a prescription by multiplying the amount of each ingredient by its sodium chloride equivalent.

Step 2. Calculate the amount of sodium chloride, alone, that would be contained in an isotonic solution of the volume specified in the prescription, namely, the amount of sodium chloride in a $0.9 \%$ solution of the specified volume.

Step 3. Subtract the amount of sodium chloride represented by the ingredients in the prescription (Step 1) from the amount of sodium chloride, alone, that would be represented in the specific volume of an isotonic solution (Step 2). T he answer represents the amount of sodium chloride to be added to make the solution isotonic.

Step 4. If an agent other than sodium chloride, such as boric acid, dextrose, or mannitol, is to be used to make a solution isotonic, divide the amount of sodium chloride (Step 3) by the sodium chloride equivalent of the other substance.

## Example Calculations of Tonicic Agent Required

How many grams of sodium chloride should be used in compounding the following prescription?
R Homatropine hydrobromide 0.6 g
Sodium chloride qs
Purif ed water ad $\quad 30 \mathrm{~mL}$
Make isoton. sol.
Sig. for the eye
Step $1 \quad 0.6 \mathrm{~g} \times \frac{1000 \mathrm{mg}}{1 \mathrm{~g}} \times 0.17$ (from Table 11.1)
$=102 \mathrm{mg}$ of sodium chloride represented by the homatromine HBr
Step 2
$30 \mathrm{~mL} \times \frac{0.9 \mathrm{~g}}{100 \mathrm{~mL}} \times \frac{1000 \mathrm{mg}}{1 \mathrm{~g}}$
$=270 \mathrm{mg}$ of sodium chloride in 30 mL of an isotonic sodium chloride solution
Step 3
$270 \mathrm{mg}($ from Step 2) - $102 \mathrm{mg}($ from Step 1) $=\mathbf{1 6 8} \mathbf{~ m g}$ of sodium chloride to be used

## How many grams of boric acid should be used in compounding the following prescription?

Rx Proparacaine hydrochloride $0.5 \%$
Pilocarpine hydrochloride $\quad 2 \%$
Boric acid
qs
Purif ed water ad
60 mL
Make isoton. sol.
Sig. one drop in each eye
Step 1 Proparacaine HCl :

$$
\frac{0.5 \mathrm{~g}}{100 \mathrm{~mL}} \times \frac{1000 \mathrm{mg}}{1 \mathrm{~g}} \times 60 \mathrm{~mL}=300 \mathrm{mg} \times 0.15=\underset{\text { chloride represented }}{45 \mathrm{mg} \text { of sodium }}
$$

Pilocarpine HCl :

$$
\frac{2 \mathrm{~g}}{100 \mathrm{~mL}} \times \frac{1000 \mathrm{mg}}{1 \mathrm{~g}} \times 60 \mathrm{~mL}=1200 \mathrm{mg} \times 0.24=\begin{gathered}
288 \mathrm{mg} \text { of sodium } \\
\text { chloride represented }
\end{gathered}
$$

Total: $45 \mathrm{mg}+288 \mathrm{mg}=333 \mathrm{mg}$ of sodium chloride represented by both ingredients

Step $2 \quad \frac{0.9 \mathrm{~g}}{100 \mathrm{~mL}} \times \frac{1000 \mathrm{mg}}{1 \mathrm{~g}} \times 60 \mathrm{~mL}$
$=540 \mathrm{mg}$ of sodium chloride in 60 mL of an isotonic sodium chloride solution
Step $3 \quad 540 \mathrm{mg}($ from Step 2) $-333 \mathrm{mg}($ from Step 1$)=207 \mathrm{mg}$ of sodium chloride required to make the solution isotonic

But because the prescription calls or boric acid:

Step $4 \quad 4.207 \mathrm{mg} \div 0.52=\mathbf{3 9 8 . 0 8} \mathbf{~ m g}$ of boric acid to be used

How many grams of potassium nitrate should be used to make the following prescription isotonic?
$\mathbb{R}^{2}$
Sol. silver nitrate
$1: 500 \mathrm{w} / \mathrm{v}$
Make isoton. sol.
Sig. for eye use

Step 1

$$
\begin{aligned}
\frac{1 \mathrm{~g}}{500 \mathrm{~mL}} \times \frac{1000 \mathrm{mg}}{1 \mathrm{~g}} \times 60 \mathrm{~mL} & =120 \mathrm{mg} \text { silver nitrate } \times 0.33 \\
& =39.6 \mathrm{mg} \text { of sodium chloride represented }
\end{aligned}
$$

Step 2
$\frac{0.9 \mathrm{~g}}{100 \mathrm{~mL}} \times \frac{1000 \mathrm{mg}}{1 \mathrm{~g}} \times 60 \mathrm{~mL}$
$=540 \mathrm{mg}$ of sodium chloride in 60 mL of an isotonic sodium chloride solution
Step 3
$540 \mathrm{mg}($ from Step 2$)-39.6 \mathrm{mg}($ from Step 1$)=500.4 \mathrm{mg}$ of sodium chloride required to make solution isotonic

Because, in this solution, sodium chloride is incompatible with silver nitrate, the tonicity agent of choice is potassium nitrate. Therefore,

Step 4
$500.4 \mathrm{mg} \div 0.58($ sodium chloride equivalent of potassium nitrate $)=\mathbf{8 6 2 . 7 6} \mathbf{~ m g}$ of potassium nitrate to be used

How many grams of sodium chloride should be used in compounding the following prescription?

```
B Ingredient X 0.5 g
Sodium chloride qS
Purif ed water ad }50\textrm{mL
Make isoton. sol.
Sig. eyedrops
```

Let us assume that ingredient X is a new substance or which no sodium chloride equivalent is to be found in Table 11.1 and that its molecular weight is 295 and its $i$ factor is 2.4. The sodium chloride equivalent of ingredient X may be calculated as follows:

$$
\frac{58.5}{1.8} \times \frac{2.4}{295}=0.26, \text { the sodium chloride equivalent for ingredient } \mathrm{X}
$$

Step $1 \quad 0.5 \mathrm{~g} \times \frac{1000 \mathrm{mg}}{1 \mathrm{~g}} \times 0.26=\begin{gathered}130 \mathrm{mg} \text { of sodium chloride represented by } \\ \text { ingredient } X\end{gathered}$

Step $2 \frac{0.9 \mathrm{~g}}{100 \mathrm{~mL}} \times \frac{1000 \mathrm{mg}}{1 \mathrm{~g}} \times 50 \mathrm{~mL}$
$=450 \mathrm{mg}$ of sodium chloride in 50 mL of an isotonic sodium chloride solution

Step 3
$450 \mathrm{mg}($ from Step 2) - $130 \mathrm{mg}($ from Step 1) $=\mathbf{3 2 0} \mathbf{~ m g}$ of sodium chloride to be used

## Use of Freezing Point Data in Isotonicity Calculations

Freezing point data (DT ) can be used in isotonicity calculations when the agent has a tonicic effect and does not penetrate the biologic membranes in question (e.g., red blood cells).

As stated previously, the freezing point o both blood and lacrimal fluid is $-0.52^{\circ} \mathrm{C}$. Thus, a pharmaceutical solution that has a freezing point of $-0.52^{\circ} \mathrm{C}$ is considered isotonic.

Representative data on freezing point depression by medicinal and pharmaceutical substances are presented in Table 11.3.

## Table 11.3 - freezIng poIn TdaTa for SeleCT agen TS

| a gent | f reezing point depression, $1 \%$ Solutions ( $\mathrm{DT}_{\mathrm{f}}{ }^{1 \% 9}$ ) |
| :--- | :---: |
| Atropine sulfate | 0.07 |
| Boric acid | 0.29 |
| Chlorobutanol | 0.14 |
| Dextrose | 0.09 |
| Ephedrine sulfate | 0.13 |
| Epinephrine bitartrate | 0.10 |
| Glycerin | 0.20 |
| Homatropine hydrobromide | 0.11 |
| Lidocaine hydrochloride | 0.063 |
| Lincomycin | 0.09 |
| Morphine sulfate | 0.08 |
| Naphazoline hydrochloride | 0.16 |
| Physostigmine salicylate | 0.09 |
| Sodium bisulfite | 0.36 |
| Sodium chloride | 0.58 |
| Sulfacetamide sodium | 0.14 |
| Zinc sulfate | 0.09 |

Although these data are or solution strengths o 1\% (DT \% ) f1, data or other solution strengths and or many additional agents may be found in physical pharmacy textbooks and in the literature.

## Example Calculations Using Freezing Point Data

How many milligrams each of sodium chloride and lidocaine hydrochloride are required to prepare 30 mL of a $1 \%$ solution of lidocaine hydrochloride isotonic with tears?

To make this solution isotonic, the freezing point must be lowered to $-0.52^{\circ} \mathrm{C}$.
From Table 11.3, it is determined that a $1 \%$ solution o lidocaine hydrochloride has a freezing point lowering o $0.063^{\circ} \mathrm{C}$. Thus, sufficient sodium chloride must be added to lower the freezing point an additional $0.457^{\circ} \mathrm{C}$ $\left(0.52^{\circ} \mathrm{C}-0.063^{\circ} \mathrm{C}\right)$.

Also rom Table 11.3, it is determined that a $1 \%$ solution o sodium chloride lowers the freezing point by $0.58^{\circ} \mathrm{C}$. By proportion:

$$
\frac{1 \% \mathrm{NaCl}}{\mathrm{x} \% \mathrm{NaCl}}=\frac{0.58^{\circ} \mathrm{C}}{0.457^{\circ} \mathrm{C}}
$$

$x=0.79 \%$ sodium chloride needed to lower the freezing point by $0.457^{\circ} \mathrm{C}$ and, there-
fore, required to make the solution isotonic

Thus, to make 30 mL of solution,
$30 \mathrm{~mL} \times 1 \%=0.3 \mathrm{~g}=\mathbf{3 0 0} \mathbf{~ m g}$ lidocaine hydrochloride, and
$30 \mathrm{~mL} \times 0.79 \%=0.24 \mathrm{~g}=\mathbf{2 3 6 . 6 8} \mathbf{~ m g}$ sodium chloride

NOTE: Should a prescription call for more than one medicinal and/or pharmaceutic ingredient, the sum of the freezing points is subtracted from the required value in determining the additional lowering required by the agent used to provide isotonicity.

## Isotonisity

$\checkmark$ To calculate the "equivalent tonic effect" to sodium chloride represented by an ingredient in a preparation, multiply its weight by its E-value:

## $g \times E$ - value equivalent tonic effect $=g$, to sodium chloride

$\checkmark$ To make a solution isotonic, calculate and ensure the quantity of sodium chloride and/ or the equivalent tonic effect of all other ingredients to total $0.9 \% \mathrm{w} / \mathrm{v}$ in the preparation:

$$
\frac{\mathrm{g}(\mathrm{NaCl}) \times \mathrm{g}(\mathrm{NaCl} \text { tonic equivelant })}{\mathrm{mL} \text { (preparation) }} \times 100=0.9 \%
$$

$\checkmark$ To make an isotonic solution from a drug substance, add sufficient water by the equation:

$$
\frac{\mathrm{g}(\text { drug substance }) \times \mathrm{E}-\text { value (drug substance) }}{0.009}=\mathrm{mL} \text { water }
$$

This solution may then be made to any volume with isotonic sodium chloride solutionto maintain its isotonicity.

The E-value can be derived from the same equation, given the grams of drug substance and the milliliters of water required to make an isotonic solution.

CaSe In poIn T 11.1 $1^{\text {a }}$ A local ophthalmologist is treating one of his patients for a post-LAs iK eye infection that is not responding to topical ciprofloxacin. t hese infections, although rare, can occur after laser in situ keratomileusis (LAs iK) surgery for vision correction.
topical amikacin sulfate has been shown to be effective for the treatment of eye infections due to ciprofloxacin-resistant Pseudomonas, ${ }^{5,6}$ Burkholderia ambifaria, ${ }^{7}$ Mycobacterium chelonae, and Mycobacterium fortuitum. ${ }^{8-10}$
the ophthalmologist prescribes 60 mL of a $2.5 \%$ amikacin sulfate isotonic solution, two drops in the affected eye every 2 hours.

Amikacin sulfate Us $\mathrm{P}\left(\mathrm{c}_{22} \mathrm{H}_{43} \mathrm{~N}_{5} \mathrm{O}_{13} \cdot 2 \mathrm{H}_{2} \mathrm{SO}_{2}\right)$, m.w., 781.76 , is an aminoglyco-side-type antibiotic containing three ions.
(a) Determine the weight in grams of amikacin sulfate needed to prepare the solution.
(b) calculate the sodium chloride equivalent (E-value) for amikacin sulfate.
(c) calculate the amount of sodium chloride needed to make the prepared solution isotonic.
(d) How many milliliters of $23.5 \%$ sodium chloride injection should be used to obtain the needed sodium chloride?
${ }^{\text {a }}$ c ase in Point courtesy of W. beach, Athens, GA.
(a) $60 \mathrm{~mL} \times 2.5 \% \mathrm{w} / \mathrm{v}=1.5 \mathrm{~g}$ amikacin
(b) NaCl m.w. $=58.5$

Amikacin m.wt. $=781.76$
$i=2.6$
$\frac{58.5}{1.8} \times \frac{2.6}{781.76}=E$
$E=0.108$
(c) $60 \mathrm{~mL} \times 0.9 \% \mathrm{w} / \mathrm{v}=0.54 \mathrm{~g} \mathrm{NaCl}$
(d) 1.5 g (amikacin sulfate $) \times 0.108(\mathrm{NaCl}$ equivelant $)=0.162 \mathrm{~g}$ $0.54 \mathrm{~g}-0.162 \mathrm{~g}=0.378 \mathrm{NaCl}$ required for isotonicity
$\frac{23.5 \mathrm{~g}}{100 \mathrm{~mL}}=\frac{0.378 \mathrm{~g}}{\mathrm{x} \mathrm{mL}}$
$\mathrm{x}=1.61 \mathrm{~mL} \mathrm{NaCl}$ injection

