

Series and parallel resistors :

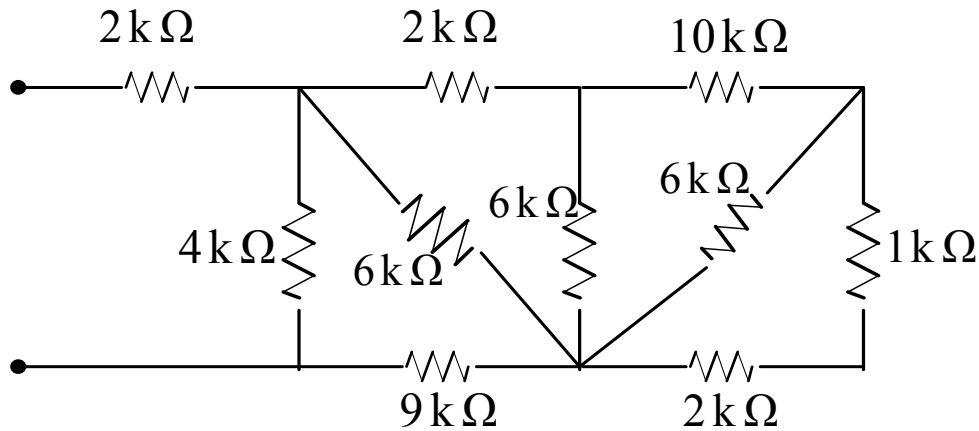
Series : $R = R_1 + R_2 + \dots + R_N \quad \Rightarrow R_s = \sum_{k=1}^N R_k$

Parallel

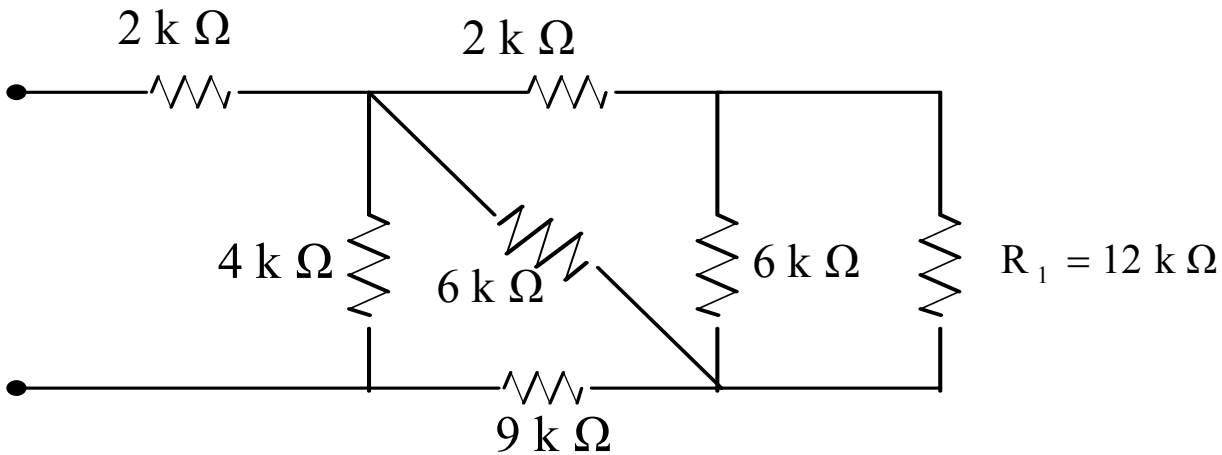
$$\frac{1}{R_p} = \frac{1}{R_1} + \frac{1}{R_2} + \dots + \frac{1}{R_N}$$
$$\frac{1}{R_p} = \sum_{k=1}^N \frac{1}{R_k}$$

Example :

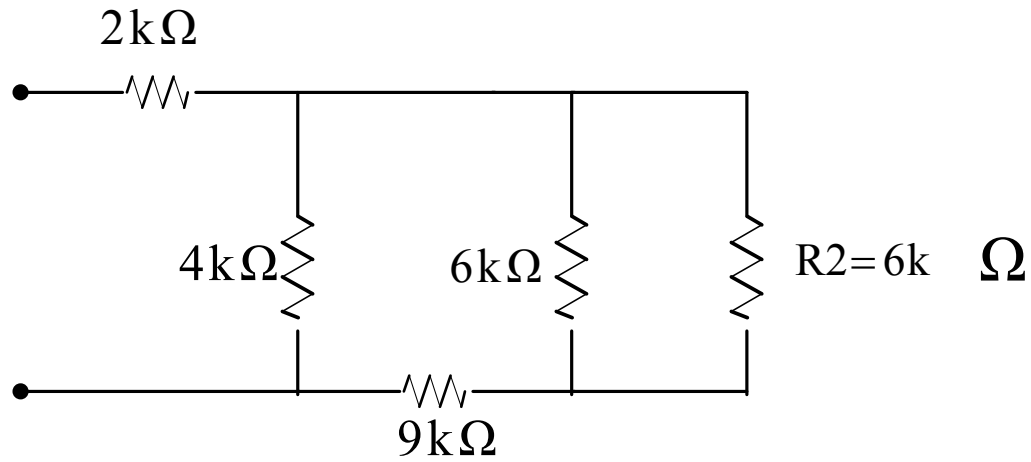
Find equivalent resistance



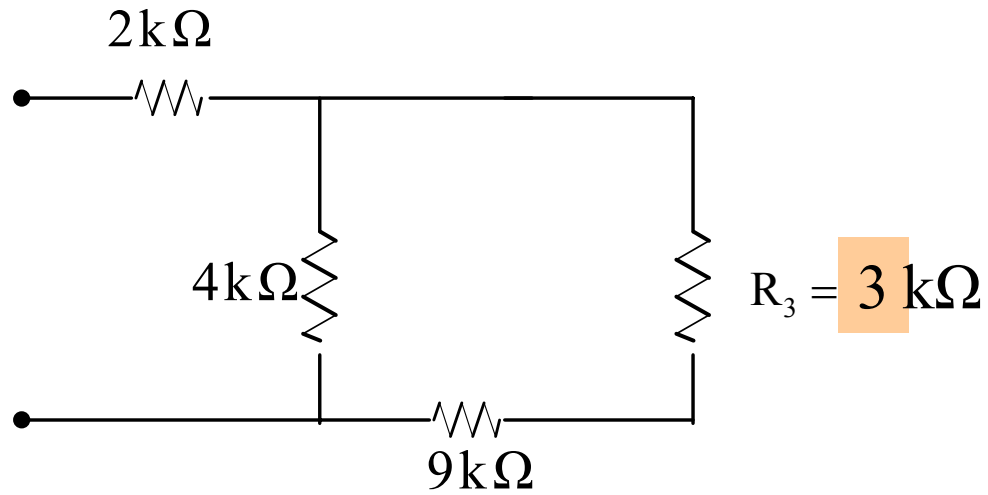
$$R_1 = \{[(1\text{ k}\Omega) + (2\text{ k}\Omega)] \parallel 6\text{ k}\Omega\} + 10\text{ k}\Omega$$



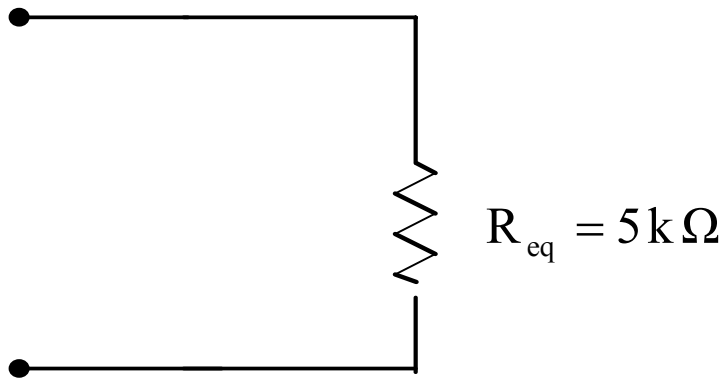
$$R_2 = [12\text{ k} // 6\text{ k}] + 2\text{ k} = 6\text{ k}$$



$$R_3 = (6\text{ k} // 6\text{ k}) = 3\text{ k}\ \Omega$$

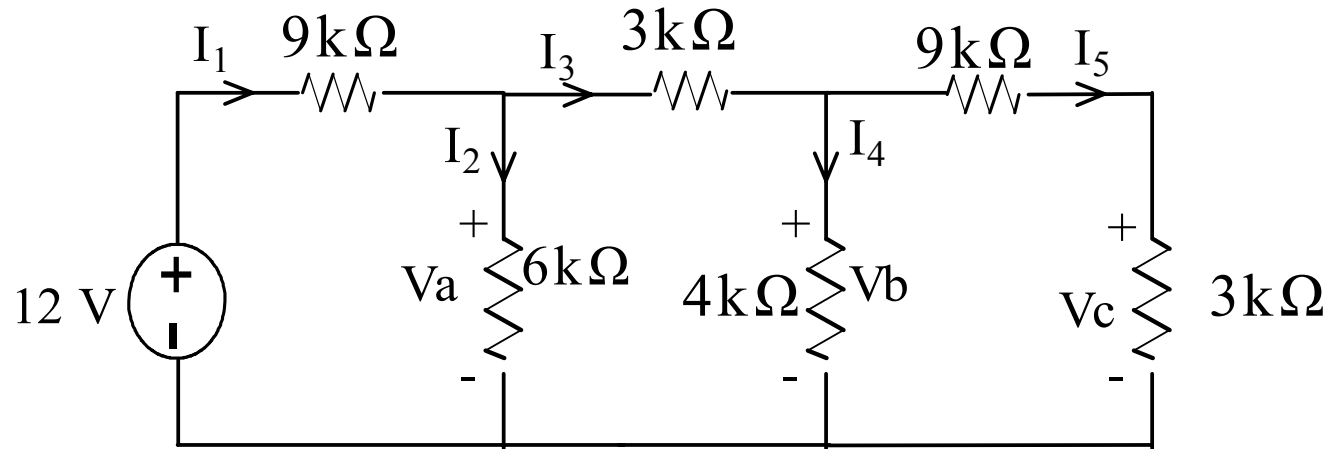


$$R_{\text{eq}} = (12\text{k} \parallel 4\text{k}) + 2\text{k} = 5\text{k}$$

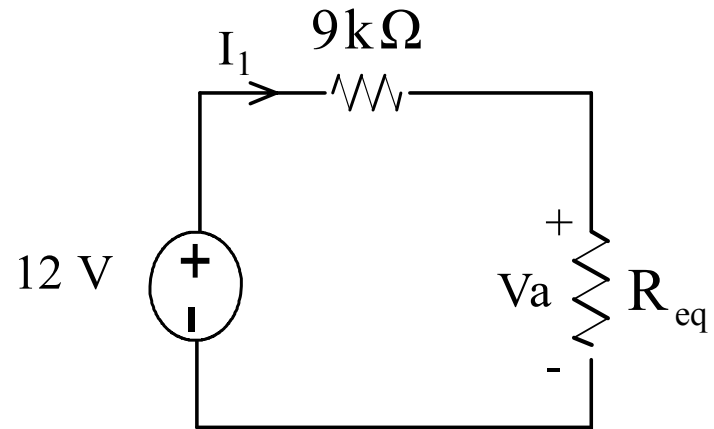


Example :

Find all currents and voltages



The equivalent circuit is :



$$\begin{aligned} R_{\text{eq}} &= \left[\left[(3\text{k} + 9\text{k}) // 4\text{k} \right] + 3\text{k} \right] // 6\text{k} \\ &= 3\text{k}\Omega \end{aligned}$$

$$I_1 = \frac{12\text{V}}{9\text{k} + 3\text{k}} = 1\text{mA} \quad \Rightarrow V_a = R_{\text{eq}} I_1 = 3\text{V}$$

$$\therefore I_2 = \frac{V_a}{6\text{k}\Omega} = \frac{3}{6\text{k}} = \frac{1}{2}\text{mA}$$

$$I_3 = I_1 - I_2 \quad \Rightarrow I_3 = 1\text{mA} - \frac{1}{2}\text{mA} = \frac{1}{2}\text{mA}$$