

Q. 1:

صباحي (٢٠)

$$W_{DC} = 0.6 \times 24 = 14.4 \text{ kN/m}^2$$

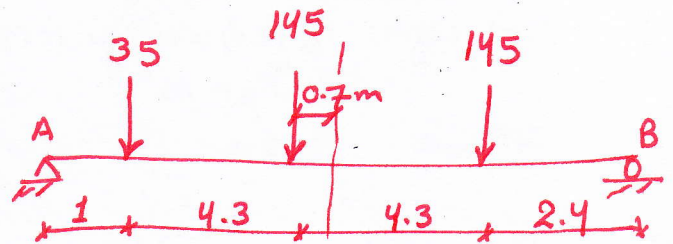
$$\rightarrow M_{DC} = 259.2 \text{ kN.m}$$

$$W_{DW} = 2 \text{ kN/m}^2$$

$$\rightarrow M_{DW} = 36 \text{ kN.m}$$

$$M_{Ln} = 167.4 \text{ kN.m}$$

$$V_A = \frac{145[2 \times 2.4 + 4.3] + 35 \times 11}{12} = 142 \text{ kN.}$$



$$M_{Tr} = 142 \times 5.3 - 35 \times 4.3 = 602.1 \text{ kN.m}$$

$$\text{Net } W = 10 - 2 \times 1.8 = 6.4 \text{ m} \rightarrow N_L = 2$$

$$E_{si} = 250 + 0.42 \times \sqrt{L_1 \times W_1} = 250 + 0.42 \times \sqrt{12 \times 10^7} = 4.85 \text{ m}$$

$$L_1 = 12 \text{ m} < 18 \text{ m} \therefore \text{OK}$$

$$W_1 = 10 \text{ m} < 18 \text{ m} \therefore \text{OK}$$

$$E_{mi} = 2100 + 0.12 \times \sqrt{12 \times 10^7} = 3.41 \text{ m} \leq \frac{10}{2} = 5 \text{ m} \therefore \text{OK}$$

$$\therefore E_{int} = 3.41 \text{ m}$$

$$\therefore M_{LL+IM} = [1.33 M_{Tr} + M_{Ln}] / E_{int}$$

$$= [1.33 \times 602.1 + 167.4] / 3.41 = 283.9$$

$$\therefore M_u = 1.25 \times 259.2 + 1.5 \times 36 + 1.75 \times 283.9$$

$$= 874.87 \simeq \underline{875 \text{ kN.m}}$$

Q. 2 :

$$W_{DC} = 0.6 \times 24 = 14.4 \text{ kN/m}^2$$

$$\longrightarrow M_{DC} = 259.2 \text{ kN.m}$$

$$W_{DW} = 2 \text{ kN/m}^2$$

$$\longrightarrow M_{DW} = 36 \text{ kN.m}$$

$$W_{Ln} = 9.3 \text{ kN/m}^2$$

$$\longrightarrow M_{Ln} = 167.4 \text{ kN.m}$$

$$V_A = \frac{110[2 \times 5.1 + 1.2]}{12} = 104.5 \text{ kN}$$

$$M_{Ta} = 104.5 \times 5.7 = 595.7 \text{ kN.m}$$

$$W = 10 - 2 \times 1.8 = 6.4 \text{ m}$$

$$\longrightarrow N_L = 2$$

$$L_1 = 12 \text{ m} < 18 \text{ m} \therefore \text{OK}$$

$$W_1 = 10 \text{ m} < 18 \text{ m} \therefore \text{OK}$$

$$E_{si} = 0.25 + 0.42 \times \sqrt{12 \times 10} = 4.85 \text{ m}$$

$$E_{mi} = 2.1 + 0.12 \times \sqrt{12 \times 10} = 3.41 \text{ m} \leq \frac{10}{2} = 5 \text{ m} \therefore \text{OK}$$

$$\therefore E_{int.} = 3.41 \text{ m}$$

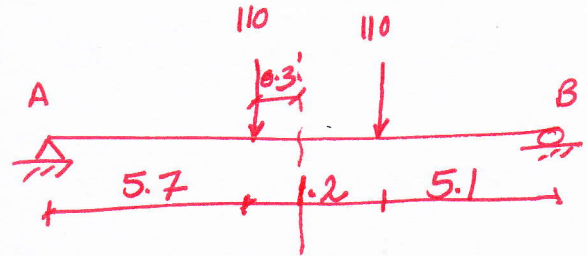
$$\longrightarrow M_{LL+IM} = [1.33 M_{Ta} + M_{Ln}] / E_{int.}$$

$$= [1.33 \times 595.7 + 167.4] / 3.41$$

$$= 281.4 \text{ kN.m}$$

$$\therefore M_u = 1.25 \times 259.2 + 1.5 \times 36 + 1.75 \times 281.4$$

$$= 870.45 \simeq 870.5 \text{ kN.m}$$



Q.3.

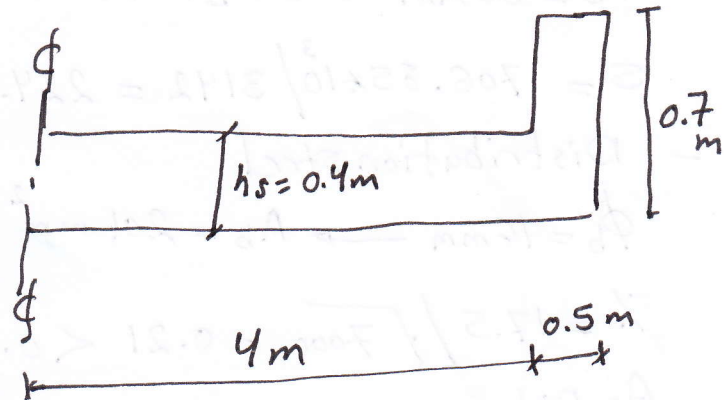
Design the required reinforcement for the interior strip of the slab-bridge section shown below if:

$$M_u = 380 \text{ kN.m}$$

$$f'_c/f_y = 42/420 \text{ MPa}$$

$$S = 7 \text{ m}$$

Then sketch the reinforcement



Solution.

$$\text{Take } C_b = 25 \text{ mm}, \phi_b = 30 \text{ mm}$$

$$d_s = 400 - 25 - 30/2 = 360 \text{ mm}$$

$$A_s = 1.25 \times 380 \times 10^6 / (420 \times 360) = 3142 \text{ mm}^2/\text{m}$$

$$B_1 = 0.85 - 0.05(42 - 28)/7 = 0.75$$

$$C = \cancel{0.85} 3142 \times 420 / (0.85 \times 42 \times 0.75 \times 1000) = 49.29 \text{ mm}$$

$$\epsilon_s = [(360 - 49.29) / 49.29] \times 0.003 = 0.0189 > 0.005 \therefore \underline{\text{OK}}$$

$$a = 0.75 \times 49.29 \text{ mm} = 37 \text{ mm}$$

$$M_r = 0.9 \times 3142 \times 420 (360 - \frac{37}{2}) = 405.6 \text{ kN.m} > 380 \text{ kN.m} \therefore \underline{\text{OK}}$$

$$f_r = 0.63 \sqrt{42} = 4.08 \text{ MPa}$$

$$\bar{y} = 200 \text{ mm}, I_g = 1000 \times 400^3 / 12 = 5.33 \times 10^9 \text{ mm}^4$$

$$S_{xc} = 5.33 \times 10^9 / 200 = 26.67 \times 10^6 \text{ mm}^3$$

$$M_{cr} = 4.08 \times 26.67 = 108.88 \text{ kN.m}$$

$$1.2 M_{cr} = 130.7 \text{ kN.m}$$

$$< 1.33 \times 380 = 505.4 \text{ kN.m} \quad \underline{\text{OK}}$$

$$< 405.6 \text{ kN.m} \quad \underline{\text{OK}}$$

$$S_{\min} = 45 \text{ mm}$$

$$S_{\max} = 450 \text{ mm}$$

- Main steel

$$\phi_b = 30 \text{ mm} \rightarrow A_b = 706.85 \text{ mm}^2$$

$$S = 706.85 \times 10^3 / 3142 = 224.96 \text{ mm} \quad \text{Say } 200 \text{ mm}$$

- Distribution steel

$$\phi_b = 16 \text{ mm} \rightarrow A_b = 201 \text{ mm}^2$$

$$\% = 17.5 / \sqrt{7000} = 0.21 < 0.5 \quad \text{ok}$$

$$A_{s, \text{Dist.}} = 0.21 \times 3142 = 658 \text{ mm}^2/\text{m}$$

$$S = 201 \times 10^3 / 658 = 305.47 \text{ mm} \quad \text{Say } 300 \text{ mm}$$

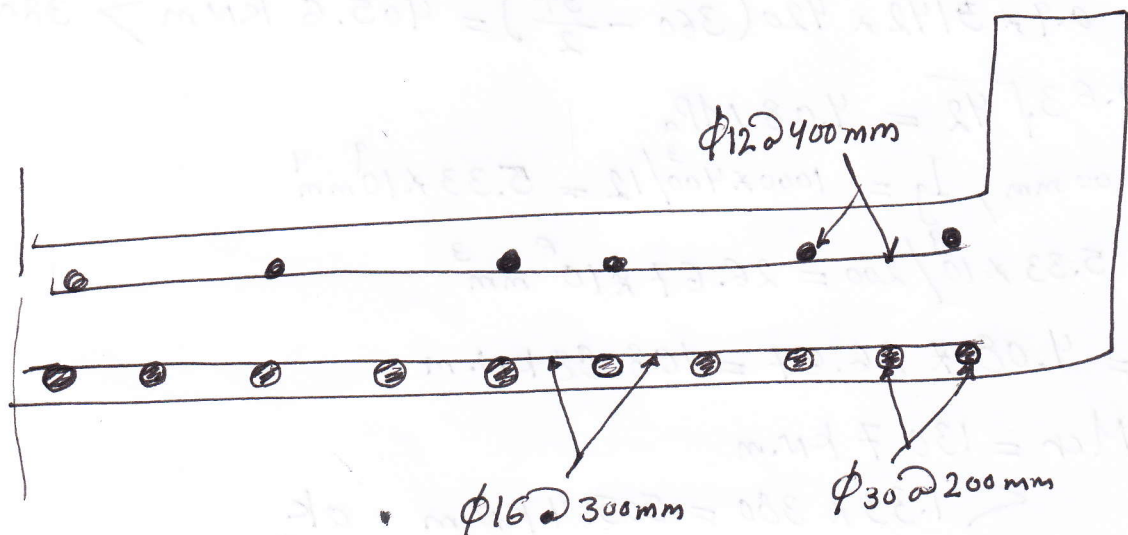
- Shrinkage & Temp. steel

$$\phi_b \pm 12 \text{ mm} \rightarrow A_b = 113 \text{ mm}^2$$

$$A_{s, S+T} = 750 \times 400 \times 10^3 / [2(1000 + 400) \times 420] = 255.1 \text{ mm}^2/\text{m}$$

$$233 < A_{s, S+T} < 1270 \text{ mm}^2/\text{m} \quad \text{ok}$$

$$S = 113 \times 10^3 / 255.1 = 442.96 \text{ mm} \quad \text{Say } 400 \text{ mm.}$$



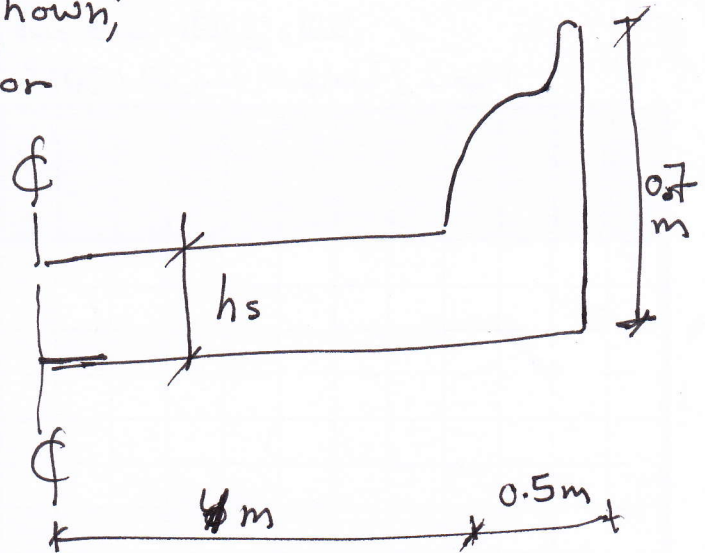
Q. 4.

For the section of Slab-bridge shown;
Sketch the required reinforcement for
the interior strips. if:

$$S = 8\text{ m}$$

$$f_c'/f_y = 37/420 \text{ MPa}$$

$$M_u = 420 \text{ kN.m}$$



Solution:

$$h_{min} = 0.04 [8000 + 3000] = 440 \text{ mm}$$

$$\text{Use } h_s = 450 \text{ mm}$$

$$\text{Take } C_b = 25 \text{ mm and } \phi_b = 30 \text{ mm}$$

$$d_s = 450 - 25 - 30/2 = 410 \text{ mm}$$

$$A_s = 1.25 \times 10^6 \times 420 / (420 \times 410) = 3048.7 \text{ mm}^2/\text{m}$$

$$\beta_1 = 0.85 - 0.05(37 - 28)/7 = 0.786$$

$$C = 3048.7 \times 420 / (0.85 \times 37 \times 0.786 \times 1000) = 51.82 \text{ mm}$$

$$E_s = [(410 - 51.82) / 51.82] \times 0.003 = 0.0207 > 0.005 \quad \text{OK}$$

$$\rightarrow \phi = 0.9$$

$$a = 0.786 \times 51.82 = 40.8 \text{ mm}$$

$$M_r = 0.9 \times 3048.7 \times 420 (410 - \frac{40.8}{2}) = 449 \text{ kN.m} > 420 \text{ kN.m} \quad \text{OK}$$

$$f_r = 0.63 \sqrt{37} = 3.83 \text{ MPa}$$

$$\bar{y} = 225 \text{ mm} \rightarrow I_g = 10^3 \times 450^3 / 12 = 7.59 \times 10^9 \text{ mm}^4$$

$$S_{nc} = 33.75 \times 10^6 \text{ mm}^3$$

$$M_{cr} = 3.83 \times 33.75 \times 10^6 = 129.3 \text{ kN.m}$$

$$1.2 M_{cr} = 155.2 \text{ kN.m}$$

$$< 1.33 \times 420 = 558.6 \text{ kN.m} \quad \text{OK}$$

$$< 449 \text{ kN.m} \quad \text{OK}$$

$$S_{min} = 45 \text{ mm}$$

$$S_{max.} = 450 \text{ mm}$$

- Main Steel

$$A_b = 706.85 \text{ mm}^2$$

$$S = 706.85 \times 10^3 / 3048.7 = 231.8 \text{ mm}$$

Say 200 mm.

- Distribution Steel

$$\phi_b = 16 \text{ mm} \rightarrow A_b = 201 \text{ mm}^2$$

$$\% = 17.5 / \sqrt{8000} = 0.195 < 0.5 \text{ ok}$$

$$A_{s, \text{Dist}} = 0.195 \times 3048.7 = 596.5 \text{ mm}^2/\text{m}$$

$$S = 201 \times 10^3 / 596.5 = 337 \text{ mm}$$

Say 300 mm

- Shrinkage & Temp. Steel

$$\phi_b = 12 \text{ mm} \rightarrow A_s = 113 \text{ mm}^2$$

$$A_{s, S+T} = 750 \times 450 \times 10^3 / (2 \times 1450 \times 420) = 277.1 \text{ mm}^2/\text{m}$$

$$233 < 277.1 < 1270 \text{ mm}^2/\text{m} \text{ ok}$$

$$S = 113 \times 10^3 / 277.1 = 407.8 \text{ mm}$$

Say 400 mm

