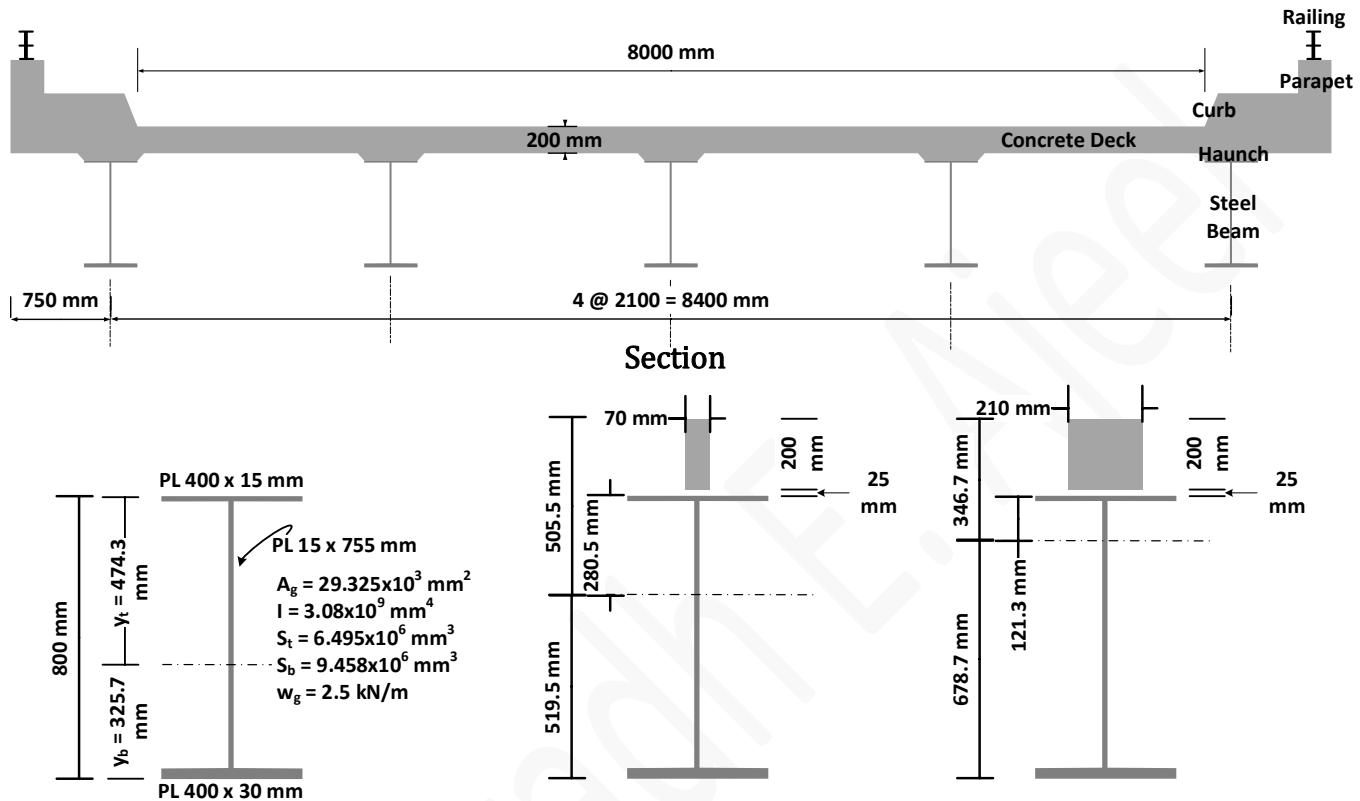




### Design of Composite Bridges

**Ex. 1:** Design the interior beams shown below for a single span bridge of ( $L$ ) = 20 m to carry standard HL-93 load and overlay layer of 50 mm thickness ( $h_{fws}$ ), curb, parapet with railing 0.4 kN/m each side on roadway width of 8 m. The compressive strength ( $f'_c$ ) = 30 MPa for all concrete sections. For steel section (A242); service stress ( $f_s$ ) = 162 MPa and yield strength ( $f_y$ ) = 295 MPa.



**Sol:**

#### Determination of Composite Section Properties

$$b_f = S = 2100 \text{ mm}$$

$$n_A = E_d / 3E_g = 0.033 \quad [\text{long-time loading}]$$

$$n_B = E_d / E_g = 0.1 \quad [\text{short-time loading}]$$

#### Long-Time Loading

$$b_e = n_A \cdot b_f = 0.033 \times 2100 = 70 \text{ mm}$$

$$A_{d,tr} = b_e \cdot h_d = 70 \times 200 = 14 \times 10^3 \text{ mm}^2$$

$$I_{d,tr} = b_e \cdot h^3 / 12 = 70 \times 200^3 / 12 = 46.67 \times 10^6 \text{ mm}^4$$

$$h = h_d + h_h + h_g = 200 + 25 + 800 = 1025 \text{ mm}$$

Component	$A$ $\text{mm}^2$	$y_t$ $\text{mm}$	$A \cdot y_t$ $\text{mm}^3$	$y_{tc}$ $\text{mm}$	$I_o$ $\text{mm}^4$	$d$ $\text{mm}$	$A \cdot d^2$ $\text{mm}^4$	$I_o + A \cdot d^2$ $\text{mm}^4$
Deck	$14 \times 10^3$	100	$1.4 \times 10^6$	505.5	$0.05 \times 10^9$	-405.5	$2.3 \times 10^9$	$2.35 \times 10^9$
Girder	$29.325 \times 10^3$	699.3	$20.5 \times 10^6$		$3.08 \times 10^9$	193.8	$1.1 \times 10^9$	$4.18 \times 10^9$
$\Sigma$	$43.325 \times 10^3$		$21.9 \times 10^6$					$6.53 \times 10^9$

$$y_{tcd} = \sum(A \cdot y_t) / \sum A = 21.9 \times 10^6 / 43.325 \times 10^3 = 505.5 \text{ mm}$$



$$y_{tcg} = y_{tcd} - h_d - h_h = 505.5 - 200 - 25 = 280.5 \text{ mm}$$

$$y_{bcg} = h - y_{tcd} = 1025 - 505.5 = 519.5 \text{ mm}$$

$$I_c = \sum(I_o + A \cdot d^2) = 6.53 \times 10^9 \text{ mm}^4$$

$$S_{tcdA} = I_c / (n_A \cdot y_{tcd}) = 6.53 \times 10^9 / (0.033 \times 505.5) = 391.45 \times 10^6 \text{ mm}^3$$

$$S_{tcgA} = I_c / y_{tcg} = 6.53 \times 10^9 / 280.5 = 23.28 \times 10^6 \text{ mm}^3$$

$$S_{bcgA} = 6.53 \times 10^9 / 519.5 = 12.57 \times 10^6 \text{ mm}^3$$

### Short-Time Loading

$$b_e = n_B \cdot b_f = 0.1 \times 2100 = 210 \text{ mm}$$

$$A_{d,tr} = b_e \cdot h_d = 210 \times 200 = 42 \times 10^3 \text{ mm}^2$$

$$I_{d,tr} = b_e \cdot h^3 / 12 = 210 \times 200^3 / 12 = 140 \times 10^6 \text{ mm}^4$$

$$h = 1025 \text{ mm}$$

Component	A mm <sup>2</sup>	y <sub>t</sub> mm	A · y <sub>t</sub> mm <sup>3</sup>	y <sub>tc</sub> mm	I <sub>o</sub> mm <sup>4</sup>	d mm	A · d <sup>2</sup> mm <sup>4</sup>	I <sub>o</sub> + A · d <sup>2</sup> mm <sup>4</sup>
Deck	42x10 <sup>3</sup>	100	4.2x10 <sup>6</sup>	346.3	0.14x10 <sup>9</sup>	-246.3	2.55x10 <sup>9</sup>	2.69x10 <sup>9</sup>
Girder	29.33x10 <sup>3</sup>	699.3	20.5x10 <sup>6</sup>		3.08x10 <sup>9</sup>	353	3.65x10 <sup>9</sup>	6.73x10 <sup>9</sup>
$\Sigma$	71.33x10 <sup>3</sup>		24.7x10 <sup>6</sup>					9.42x10 <sup>9</sup>

$$y_{tcd} = \sum(A \cdot y_t) / \sum A = 24.7 \times 10^6 / 71.325 \times 10^3 = 346.3 \text{ mm}$$

$$y_{tcg} = 346.3 - 225 = 121.3 \text{ mm}$$

$$y_{bcg} = h - y_{tcd} = 1025 - 346.3 = 678.7 \text{ mm}$$

$$I_c = \sum(I_o + A \cdot d^2) = 9.42 \times 10^9 \text{ mm}^4$$

$$S_{tcdB} = I_c / (n_B \cdot y_{tcd}) = 9.42 \times 10^9 / (0.1 \times 346.3) = 272.02 \times 10^6 \text{ mm}^3$$

$$S_{tcgB} = I_c / y_{tcg} = 9.42 \times 10^9 / 121.3 = 77.66 \times 10^6 \text{ mm}^3$$

$$S_{bcgB} = 9.42 \times 10^9 / 678.7 = 13.88 \times 10^6 \text{ mm}^3$$

### **Determination of Unfactored Loads**

Force effects from unfactored composite (dead) loads:

$$w_d = h_d \times b_f \times Y_c = 0.2 \times 2.1 \times 24 = 10.08 \text{ kN/m}$$

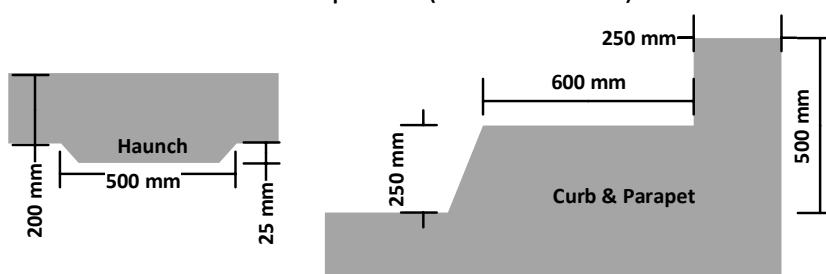
$$w_h = h_h \times b_h \times Y_c = 0.025 \times 0.45 \times 24 = 0.27 \text{ kN/m}$$

$$w_g = 2.5 \text{ kN/m} \text{ [with diaphragms]}$$

$$w_{DC1} = w_{D,nc} = 10.08 + 0.27 + 2.5 = 12.85 \text{ kN/m}$$

$$M_{DC1} = w_{DC1} L^2 / 8 = 12.85 \times 20^2 / 8 = 642.5 \text{ kN.m}$$

Force effects from unfactored composite (dead and live) loads:



$$w_{cu} = h_{cu} \times b_{cu} \times Y_c \times N_{cu} / N_g = 0.25 \times 0.6 \times 24 \times 2/5 = 1.44 \text{ kN/m}$$



$$w_{pa} = h_{pa} \times b_{pa} \times Y_c \times N_{pa}/N_g = 0.50 \times 0.25 \times 24 \times 2/5 = 1.2 \text{ kN/m}$$

$$w_{ra} = w_{ra} \times N_{ra}/N_g = 0.4 \times 2/5 = 0.16 \text{ kN/m}$$

$$w_{DC2} = w_{D,c} = 1.44 + 1.2 + 0.16 = 2.8 \text{ kN/m}$$

$$M_{DC2} = w_{DC2} L^2/8 = 2.8 \times 20^2/8 = 140 \text{ kN.m}$$

$$w_{fws} = h_{fws} \times w \times Y_{as}/N_g = 0.05 \times 8 \times 22.5/5 = 1.8 \text{ kN/m}$$

$$M_{DW} = w_{DW} L^2/8 = 1.8 \times 20^2/8 = 90 \text{ kN.m}$$

$$w_{Ln} = 9.3 \text{ kN/m}$$

$$M_{Ln} = w_{Ln} \cdot L^2/8 = 9.3 \times 20^2/8 = 465 \text{ kN.m}$$

$$M_{Tr} = 1246.6 \text{ kN.m}$$

Live load distribution factors:

$$N_g \geq 4 \quad N_g = 5 \therefore \text{OK}$$

$$6 \leq L \leq 73 \quad L = 20 \text{ m} \therefore \text{OK}$$

$$1.1 \leq S \leq 4.9 \quad S = 2.1 \text{ m} \therefore \text{OK}$$

$$110 \leq h_d \leq 300 \quad h_d = 200 \text{ mm} \therefore \text{OK}$$

$$n_B = 10$$

$$I_g = 3.08 \times 10^9 \text{ mm}^4$$

$$A_g = 29.325 \times 10^3 \text{ mm}^2$$

$$e_g = y_{tg} + h_h + h_d/2 = 474.3 + 25 + 100 = 599.3 \text{ mm}$$

$$\begin{aligned} K_g &= n(I_g + A_g \cdot e_g^2) = 10(3.08 \times 10^9 + 29.325 \times 10^3 \times 599.3^2) \\ &= 136.124 \times 10^9 \text{ mm}^4 \end{aligned}$$

$$4 \times 10^9 \leq K_g \leq 3 \times 10^{12} \quad K_g = 136.124 \times 10^9 \text{ mm}^4 \therefore \text{OK}$$

Thus, the cross section satisfies the design stipulations

$$w = 8 \text{ m} \rightarrow N_L = 2$$

$\therefore$  check both  $DF_{si}$  and  $DF_{mi}$

Live load distribution factor for moment:

$$\begin{aligned} DF_{Mi} &= 0.06 + (S/4300)^{0.4} \cdot (S/L)^{0.3} \cdot (K_g/L \cdot h_d^3)^{0.1} \\ &= 0.06 + (2.1/4.3)^{0.4} \cdot (2.1/20)^{0.3} \cdot (0.136124/20 \times 0.2^3)^{0.1} = 0.436 \end{aligned}$$

$$\begin{aligned} DF_{Mi} &= 0.075 + (S/2900)^{0.6} \cdot (S/L)^{0.2} \cdot (K_g/L \cdot h_d^3)^{0.1} \\ &= 0.075 + (2.1/2.9)^{0.6} \cdot (2.1/20)^{0.2} \cdot (0.136124/20 \times 0.2^3)^{0.1} = 0.592 \end{aligned}$$

$$\rightarrow DF_{int} = 0.592$$

$$IM = 0.33$$

$$\begin{aligned} M_{LL+IM} &= DF_{int} [(1 + IM)M_{Tr} + M_{Ln}] \\ &= 0.592 [1.33 \times 1246.6 + 465] = 1256.8 \text{ kN.m} \end{aligned}$$

### Check Stresses on Steel Girder

$$f_s = 162 \text{ MPa}$$

#### At midspan

$$f_{top} = \frac{M_{DC1}}{S_{tg}} + \frac{M_{DC2} + M_{DW}}{S_{tcgA}} + \frac{M_{(LL+IM)}}{S_{tcgB}}$$



$$\begin{aligned}
 &= \frac{642.5 \times 10^6}{6.5 \times 10^6} + \frac{(140 + 90) \times 10^6}{23.28 \times 10^6} + \frac{1256.8 \times 10^6}{77.66 \times 10^6} \\
 &= 98.85 + 9.88 + 16.18 = 124.91 \text{ MPa} < f_s = 162 \text{ MPa} \therefore \text{OK} \\
 f_{bot} &= \frac{M_{DC1}}{S_{bg}} + \frac{M_{DC2} + M_{DW}}{S_{bcgA}} + \frac{M_{(LL+IM)}}{S_{bcgB}} \\
 &= \frac{642.5 \times 10^6}{9.46 \times 10^6} + \frac{(140 + 90) \times 10^6}{12.57 \times 10^6} + \frac{1256.8 \times 10^6}{13.88 \times 10^6} \\
 &= 67.92 + 18.3 + 90.55 = 176.77 \text{ MPa} > f_s = 162 \text{ MPa} \therefore \text{NOK}
 \end{aligned}$$

### Check Stresses on Concrete Deck

$$\begin{aligned}
 f_c &= 0.45 f'_c = 0.45 \times 30 = 13.5 \text{ MPa} \\
 f_{top} &= \frac{M_{DC2} + M_{DW}}{S_{tcdA}} + \frac{M_{(LL+IM)}}{S_{tcdB}} \\
 &= \frac{(140 + 90) \times 10^6}{391.45 \times 10^6} + \frac{1256.8 \times 10^6}{272.02 \times 10^6} \\
 &= 0.59 + 4.62 = 5.21 \text{ MPa} < f_c = 13.5 \text{ MPa} \therefore \text{OK}
 \end{aligned}$$

### If Dimensions of Steel Beam Are Not Designed

$$h_g = L/25$$

$$t_w = h_g/170 \geq 15 \text{ mm} \quad [\text{to avoid needing to stiffeners}]$$

$$t_{f,upper} = t_w$$

$$A_{f,upper} = M_{DC1}/(150h_g)$$

$$b_{f,upper} = A_{f,upper}/t_{f,upper}$$

$$b_{f,lower} = b_{f,upper}$$

$$t_{f,lower} = 2t_{f,upper}$$

$$h_w = h_g - (t_{f,lower} + t_{f,upper})$$