

Depending on the figure below; use the following data for all Questions:

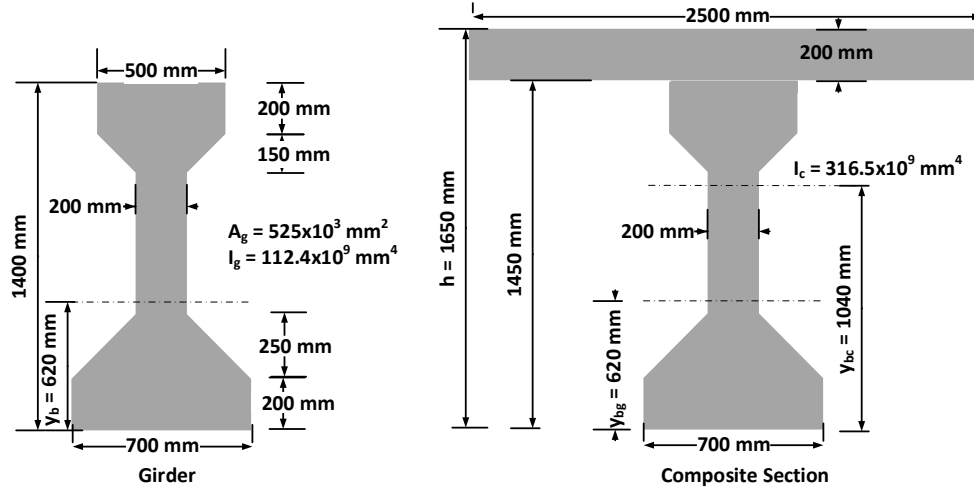
Effective length (L) = 27 m

Concrete deck: (f'_c) = 28 MPa

Concrete beam: (f'_{ci}) = 35 MPa and (f'_c) = 42 MPa

Prestressing steel: (ϕ_p) = 12.7 mm, (A_p) = 98.7 mm², (f_{py}) = 1674 MPa and (f_{pu}) = 1860 MPa

Losses expected in prestressing = 0.2



Q.1: Determine the required number of strands for the girder to carry (M_{LL+IM}) = 2400 kN.m, (M_{DC1}) = 2700 kN.m, (M_{DC2}) = 275 kN.m, overlay weight (w_{DW}) = 1.6 kN/m and (y_{bp}) = 0.12 m.

Q.2: Check the allowability of stresses in girder section in-service stage of the bridge life.

Q.3: Check the flexural strength of the girder during the bridge life.

Q.1 Sol:

$$M_{DW} = w_{DW} \cdot L^2 / 8 = 1.6 \times 27^2 / 8 = 145.8 \text{ kN.m}$$

$$S_{bg} = I_g / y_{bg} = 112.4 \times 10^9 / 620 = 180.13 \times 10^6 \text{ mm}^3$$

$$S_{bcg} = I_c / y_{bcg} = 316.5 \times 10^9 / 1040.6 = 304.15 \times 10^6 \text{ mm}^3$$

$$f_{bot} = \frac{M_{DC1}}{S_{bg}} + \frac{M_{DC2} + M_{DW} + 0.8M_{(LL+IM)}}{S_{bcg}}$$

$$= \frac{2700}{180.13} + \frac{275 + 145.8 + 0.8 \times 2400}{304.15} = 22.69 \text{ MPa}$$

$$f_t = 0.50 \sqrt{f'_c} = 0.5 \times \sqrt{42} = 3.24 \text{ MPa}$$

$$f_{c,pe} = f_{bot} - f_t = 22.69 - 3.24 = 19.45 \text{ MPa}$$

$$e = y_{bg} - y_{bp} = 620 - 120 = 500 \text{ mm}$$

$$f_{c,pe} = \frac{P_e}{A_g} + \frac{P_e \cdot e_c}{S_{bg}}$$

$$19.45 = \frac{P_e}{525 \times 10^3} + \frac{P_e \times 0.5}{180.13 \times 10^3} \rightarrow P_e = 4155.51 \text{ kN}$$

$$f_{pi} = 0.75 f_{pu} = 0.75 \times 1860 = 1395 \text{ MPa}$$

$$P_{i,p} = A_p \cdot f_{pi} = 98.7 \times 1395 = 137.68 \text{ kN}$$

$$R = 1 - \text{losses} = 1 - 0.2 = 0.8$$

$$P_{e,p} = R \cdot P_{i,p} = 0.8 \times 137.86 = 110.29 \text{ kN}$$

$$N_p = P_e / P_{e,p} = 4155.51 / 110.29 = 38 \text{ strands}$$

Q.2 Sol:

$$f_c = 0.45f'_c = 0.45 \times 42 = 18.9 \text{ MPa}$$

$$f_t = 3.24 \text{ MPa}$$

At midspan P_e , $M_{D,nc}$, $M_{D,c}$, M_{DW} and $M_{(LL+IM)}$.

$$P_i = N_p \cdot P_{i,p} = 38 \times 137.68 = 5231.84 \text{ kN}$$

$$P_e = R \cdot P_i = 0.8 \times 5231.84 = 4185.47 \text{ kN}$$

$$S_{tg} = I_g/y_{tg} = 112.4 \times 10^9 / 780 = 144.1 \times 10^6 \text{ mm}^3$$

$$S_{tcg} = I_c/y_{tcg} = 316.5 \times 10^9 / 360 = 879.17 \times 10^6 \text{ mm}^3$$

$$\begin{aligned} f_{top} &= -\frac{P_e}{A_g} + \frac{P_e \cdot e}{S_{tg}} - \frac{M_{DC1}}{S_{tg}} - \frac{M_{DC2} + M_{DW} + 0.8M_{(LL+IM)}}{S_{tcg}} \\ &= -\frac{4185.47}{525} + \frac{4185.47 \times 0.5}{144.1} - \frac{2700}{144.1} - \frac{275 + 145.8 + 0.8 \times 2400}{879.17} \\ &= -7.97 + 14.52 - 18.74 - 2.66 = -14.85 \text{ MPa} < 18.9 \text{ MPa} \therefore \text{OK} \end{aligned}$$

$$\begin{aligned} f_{bot} &= -\frac{P_e}{A_g} - \frac{P_e \cdot e}{S_{bg}} + \frac{M_{DC1}}{S_{bg}} + \frac{M_{DC2} + M_{DW} + 0.8M_{(LL+IM)}}{S_{bcg}} \\ &= -\frac{4185.47}{525} - \frac{4185.47 \times 0.5}{180.13} + \frac{2700}{180.13} + \frac{275 + 145.8 + 0.8 \times 2400}{304.15} \\ &= -7.97 - 11.62 + 14.99 + 7.7 = 3.1 \text{ MPa} < 3.24 \text{ MPa} \therefore \text{OK} \end{aligned}$$

At ends P_e load only.

$$f_{top} = -\frac{P_e}{A_g} + \frac{P_e \cdot e}{S_{tg}} = -7.97 + 14.52 = 6.55 \text{ MPa} > 3.24 \text{ MPa} \therefore \text{NOK}$$

$$f_{bot} = -\frac{P_e}{A_g} - \frac{P_e \cdot e}{S_{bg}} = -7.97 - 11.62 = -19.59 \text{ MPa} > 18.9 \text{ MPa} \therefore \text{NOK}$$

Q.3 Sol:

$$M_{DC} = M_{DC1} + M_{DC2} = 2700 + 275 = 2975 \text{ kN.m}$$

$$\begin{aligned} M_u &= \eta_i [1.25M_{DC} + 1.50M_{DW} + 1.75M_{LL+IM}] \\ &= 1.0 [1.25 \times 2975 + 1.50 \times 145.8 + 1.75 \times 2400] = 8137.45 \text{ kN.m} \end{aligned}$$

$$A_{ps} = N_p \cdot A_p = 38 \times 98.7 = 3750.6 \text{ mm}^2$$

$$0.5f_{pu} = 0.5 \times 1860 = 930 \text{ MPa}$$

$$f_{pe} = R \cdot f_{pi} = 0.8 \times 1395 = 1116 \text{ MPa} > 0.5f_{pu} = 930 \text{ MPa} \therefore \text{OK}$$

$$d_{ps} = h - y_{bp} = 1650 - 120 = 1530 \text{ mm}$$

$$\beta_1 = 0.85 - 0.05(f'_c - 28)/7 = 0.85 - 0.05(42 - 28)/7 = 0.75$$

$$k = 2(1.04 - f_{py}/f_{pu}) = 2(1.04 - 0.9) = 0.28$$

$$\begin{aligned} c &= \frac{A_{ps} \cdot f_{pu}}{0.85f'_c \cdot \beta_1 \cdot b_e + k \cdot A_{ps} \cdot f_{pu}/d_{ps}} \\ &= \frac{3750.6 \times 1860}{0.85 \times 42 \times 0.75 \times 2500 + 0.28 \times 3750.6 \times 1860 / 1530} \end{aligned}$$

$$c = 102.27 \text{ mm} < 200 \text{ mm} \rightarrow \text{rectangular section}$$

$$f_{ps} = f_{pu}(1 - k \cdot c/d_{ps}) = 1860(1 - 0.28 \times 102.27/1530) = 1825.19 \text{ MPa}$$

$$a = \beta_1 \cdot c = 0.75 \times 102.27 = 76.7 \text{ mm}$$

$$M_n = A_{ps} \cdot f_{ps}(d_{ps} - a/2) = 3750.6 \times 1825.19(1530 - 76.7/2) = 10210.9 \text{ kN.m}$$

$$\phi = 1.0 \rightarrow M_r = 10210.9 \text{ kN.m} > M_u = 8137.45 \text{ kN.m} \therefore \text{OK}$$