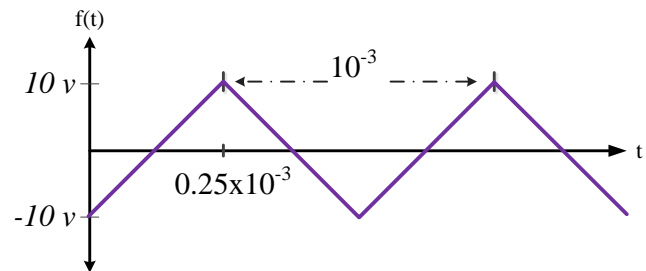


Q17: A modulating signal $f(t)$ shown

besides AM modulates a carrier with modulation index = 0.5, find:

- Total power.
- Sideband power.
- Carrier power.



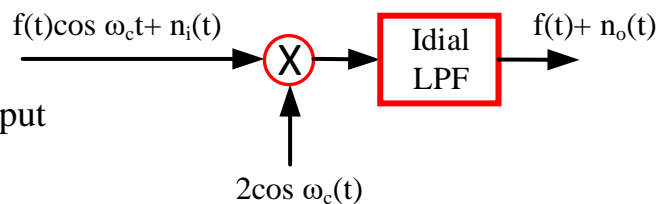
Q18: A certain message having $\frac{\overline{f^2(t)}}{|f(t)_{min}|^2} = 0.09$ is transmitted through a channel having PSD (10^{-7} w/Hz watt/Hz.

If the signal power at receiver input is 0.1 watt and the signal bandwidth is 3 kHz, find:

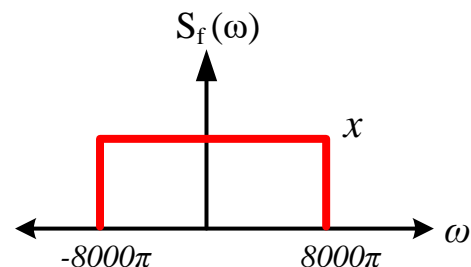
- SNR_{dB} at Rx input if AM/ DSB – SC Mod. Is used.
- $2-SNR_{dB}$ at Rx output if standard AM Mod. With $m = 0.5$ is used.

Ans: 28.23 dB, 11.66 dB.

Q19: A DSB – SC receiver shown in figure below. The channel noise PSD is $\eta/2$ with $\eta = 10^{-7}$. The PSD of the modulating signal $f(t)$ is shown in the other figure:



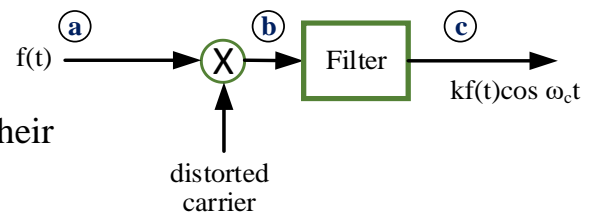
- Determine the receiver output noise power S .
- Determine the receiver noise output power N_o .
- If the output SNR is required to be at least 30dB, determine the minimum value of (x) and corresponding power of (t) .



Q20: For an AM channel with noise PSD $S_n(\omega) = 10^{-8} \text{ watt/Hz}$. (two- sided), if the receiver output SNR is required to be at least 33dB . Determine the transmitted power if the modulating signal is a single tone with peak amplitude of 0.1 volt and with frequency of 1 kHz .

Ans: 9.9 m watt .

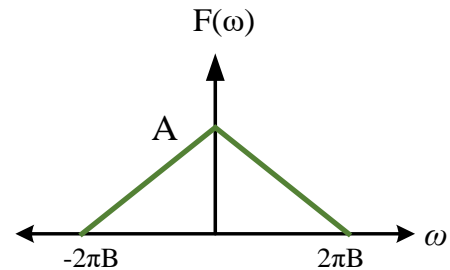
Q21: The figure below shows a DSB –SC modulator. The carrier available at the multiplier is a distorted sinusoid given by $a_1 \cos \omega_c t + a_2 \cos^2 \omega_c t$. The spectrum of $f(t)$ is shown in fig. shown:



(a) Determine the signals and sketch their spectra at points b&c.

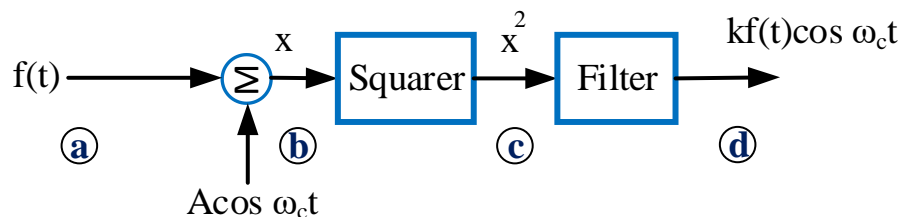
(b) What kind of filter is required in fig?

(c) What is minimum value of ω_c required for this scheme to work



Ans: $4\pi B \text{ rad/sec}$.

Q22: Show that the scheme shown in fig. Below can be used to generate DSB-SC signal. Assuming that $f(t)$ is a signal bandlimited to $B \text{ Hz}$, find the signals and sketch their spectra at points a, b, c and d. Explain the nature of filter in this figure.



Q23: An Am communication system with $m = 0.707$ operates in the presence of white noise with two- sided power spectral density $0.25 \times 10^{-14} \text{ watt/Hz}$,

and with total path losses of 90 dB . The input bandwidth is 10 kHz . Calculate the minimum required carrier amplitude of the transmitter for a 10 kHz sinusoidal input and 40 dB output SNR . Assume that resistance level is one ohm.

Ans: 63.254 volt.

Q24: A signal $f(t)$ is bandlimited to ω_m . If it is frequency translated by multiplying it by the signal $\cos\omega_c t$. Find ω_c so that the bandwidth of the transmitted signal is 1 percent of the carrier frequency ω_c .

Chapter 5

Angle Modulation

Introduction:

It is a type of CW modulation in which the angle of a sinusoidal signal (either frequency or phase) in proportion to the message where amplitude is constant. It gives a high degree of noise immunity by band expansion; it is also wide use in high fidelity music broadcast, also having a constant envelope.

$$\phi(t) = A \cos \theta(t) \quad \text{“Angle Modulation”}$$

$$\phi(t) = f(t) \cos (\omega_c t + \theta_o) \quad \text{“Amplitude Modulation”}$$

Where $(\omega_c t + \theta_o)$ represents the angle of carrier frequency

For PM

$$\theta(t) = \omega_c t + \theta_o + k_p f(t)$$

Where k_p is constant (rad/volt)

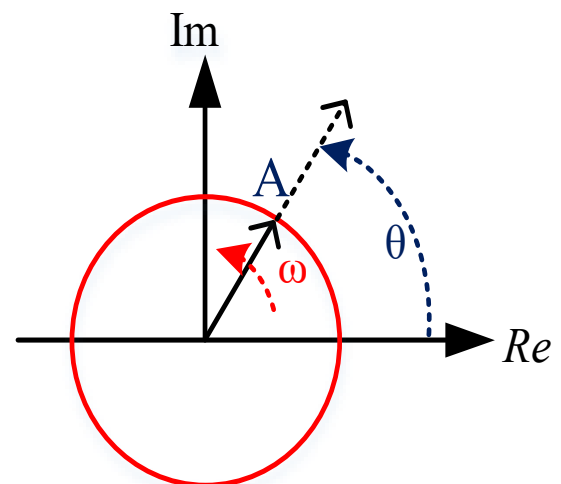
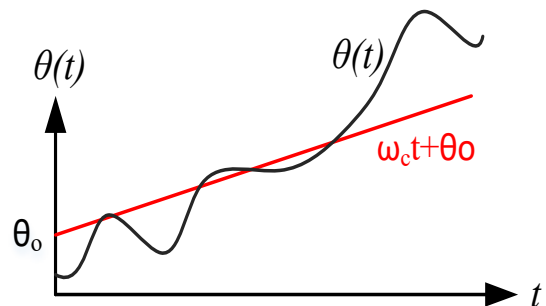
If $\theta_o = 0$

$$\theta(t) = \omega_c t + k_p f(t) \quad \dots(5-1)$$

$$\phi_{PM}(t) = A_c \cos[\omega_c t + k_p f(t)] \quad \dots(5-2)$$

The instantaneous frequency $\omega_i(t)$ is:

$$\omega_i(t) = \frac{d\theta(t)}{dt} = \omega_c + k_p f'(t) \quad \dots(5-3)$$



For FM

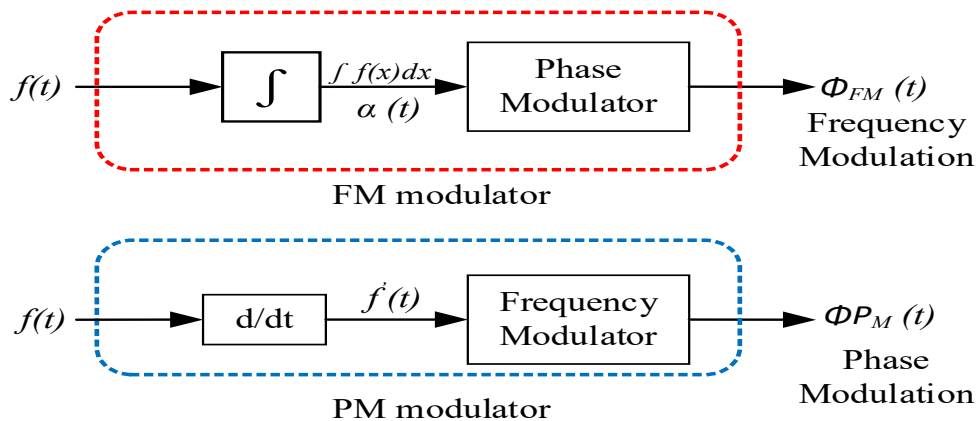
$$\omega_i(t) = \frac{d\theta(i)}{dt} = \omega_c + k_f f(t) \quad \dots(5-4)$$

Where k_f is constant ($\frac{\text{rad/sec}}{\text{volt}}$) modulation constant

$$\theta(t) = \omega_c t + k_f \int_{-\infty}^t f(\alpha) d\alpha \quad \dots(5-5)$$

$$\Phi_{FM}(t) = A_c \cos \left[\omega_c t + k_f \int_{-\infty}^t f(\alpha) d\alpha \right] \quad \dots(5-6)$$

We note from $\Phi_{PM}(t)$ and $\Phi_{FM}(t)$ that FM and PM are similar [PM corresponds to $f(t)$ and FM corresponds to $f'(t)$]. Where the frequency is the derivative of the phase, or it represents the rate of change in phase.

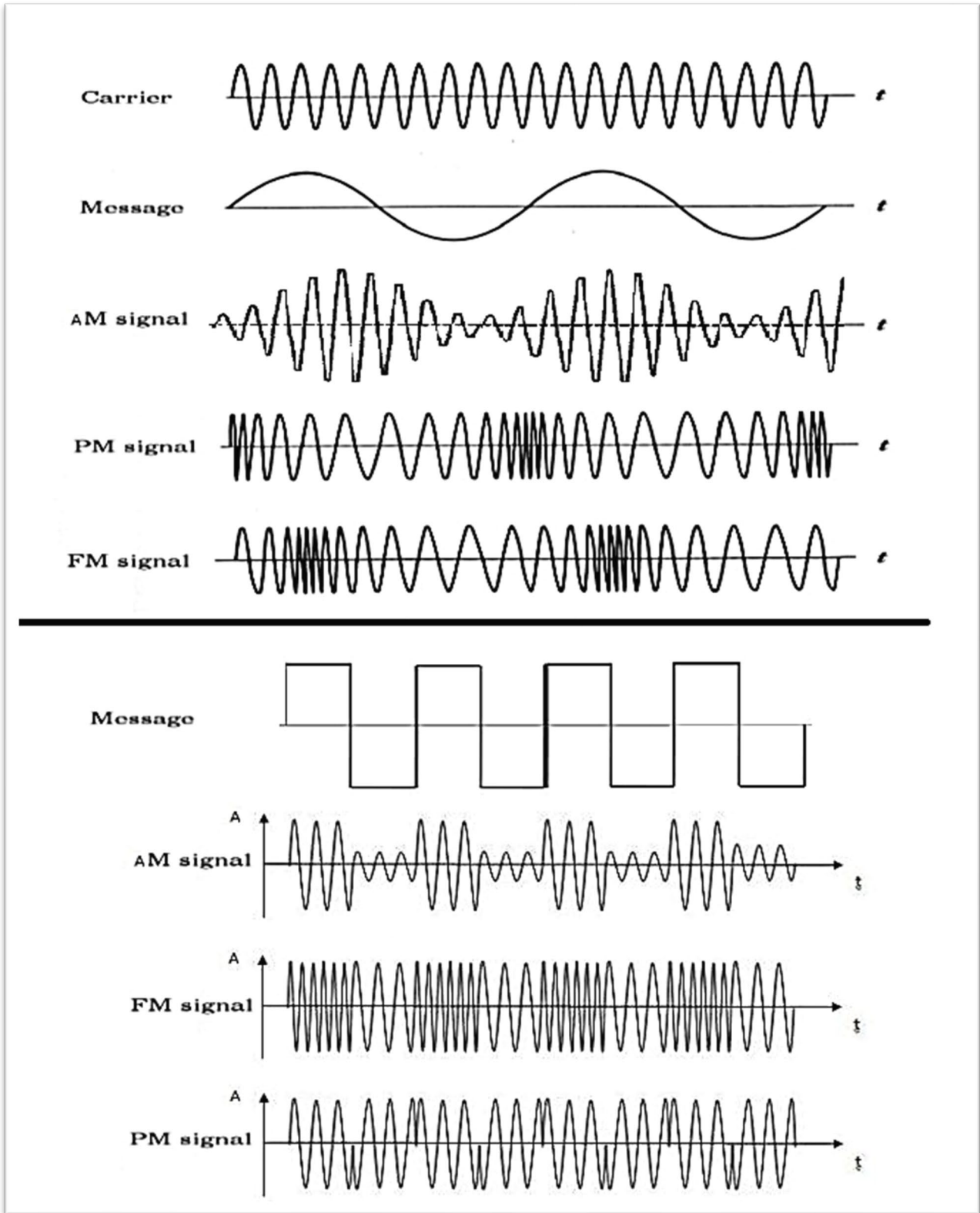
**H.W**

Write the equation for $\Phi_{AM}(t)$, $\Phi_{FM}(t)$ and $\Phi_{PM}(t)$, if the modulating signal is;

$$1-f(t) = 2\cos 300\pi t + 4\cos 600\pi t$$

$$2-f(t) = 2t, \text{ at } 0 < t < 1 \text{ msec}$$

Comparison of time waveforms



Ex 5-1

Find maximum and minimum instantaneous frequencies resulting from modulating a carrier signal with carrier frequency of $f_c=100$ MHz by $f(t)$ shown if:

1-FM with $k_f = 2\pi * 10^5 \frac{\text{rad/sec}}{\text{volt}}$ is used

2- PM with $k_p = 10\pi \frac{\text{rad}}{\text{volt}}$ is used

Solution:

For FM

$$\omega_i(t) = \omega_c + k_f f(t)$$

$$f_i(t) = f_c + \frac{k_f}{2\pi} f(t)$$

$$= 10^8 + 10^5 f(t)$$

$$f_{i \min} = 10^8 - 10^5 |f(t)|_{\min} = 99.9 \text{ MHz}$$

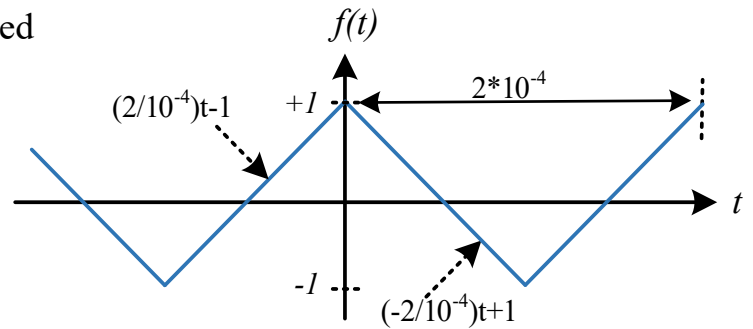
$$f_{i \max} = 10^8 + 10^5 |f(t)|_{\max} = 100.1 \text{ MHz}$$

For PM

$$f_i(t) = f_c + \frac{k_p}{2\pi} f'(t)$$

$$f_{i \min} = 10^8 - 5 * |f'(t)|_{\min} = 10^8 - 10^5 = 99.5 \text{ MHz}$$

$$f_{i \max} = 10^8 + 5 * |f'(t)|_{\max} = 10^8 + 10^5 = 100.5 \text{ MHz}$$

**Power of Angle Modulated waves:**

Simply from equations:

$$Pt_{FM} = Pt_{PM} = \frac{A_c^2}{2}$$

Watt ... (5-7)

(assuming $R=1\Omega$, if R is given then $Pt = \frac{A_c^2}{2R}$)