

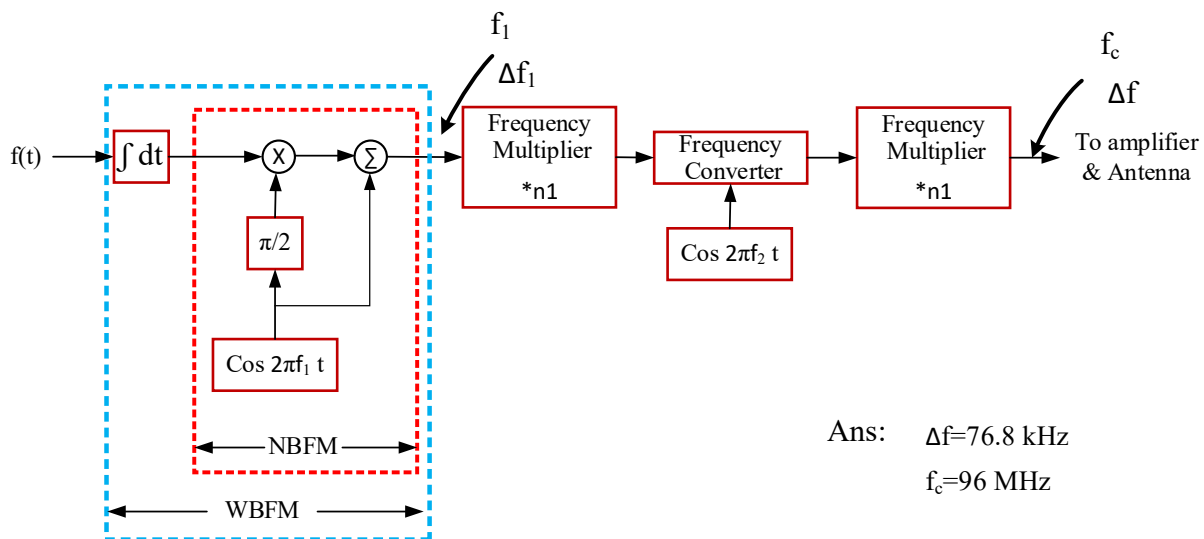
$\alpha = 1 \text{ v}, f_m = 1 \text{ kHz}$	2 kHz	40 kHz
$\alpha = 2 \text{ v}, f_m = 1 \text{ kHz}$	2 kHz	80 kHz
$\alpha = 1 \text{ v}, f_m = 2 \text{ kHz}$	4 kHz	80 kHz

Identify the type of angle modulation used (FM or PM Narrowband or wideband) for systems A and B.

**Ans:** system A: NBFM or NBPM  
System B: WBPM.

**Q17:** Design commercial FM transmitter using Armstrong's method. The final output is required to have carrier frequency of 91.2 MHz and  $\Delta f$  in the range of 75 kHz. Assume  $f_1 = 200 \text{ kHz}$  and  $\Delta f_1 = 25 \text{ Hz}$ .

**Q18:** Compute the carrier frequency  $f_c$  and the peak frequency deviation  $\Delta f$  of the output of the FM transmitter shown in fig. below [indirect (Armstrong) FM transmitter]. If:  $f_1 = 200 \text{ kHz}$ ,  $n_1 = 64$ ,  $f_2 = 10.8 \text{ MHz}$ ,  $n_2 = 48$ ,  $\Delta f_1 = 25 \text{ Hz}$



**Q19:** An angle modulated signal given by:

$$\phi(t) = A \cos[\omega_c t + 2 \cos 60 \pi t + 5 \cos 40 \pi t] \text{ with } f_c = \frac{\omega_c}{2\pi} \text{ Hz}$$

(a) Find the maximum phase deviation in radian.

(b) at  $t = \frac{1}{30} \text{ sec.}$ , find the instantaneous frequency deviation.

**Ans:** (a) 7 rad. (b) 86.6 Hz.

**Q20:** A communication system operates in the presence of white noise with two-sided power spectral density  $S_n(\omega) = 0.25 \times 10^{-14}$  watt/Hz and with total path losses (including Antennas) of 100 dB. The input bandwidth is 10 KHz. Calculate the minimum required carrier power of the transmitter for a 10 KHz sinusoidal input and a 40 dB output S/N ratio if the modulation is:

- (a) AM (DSB – LC), with  $m = 0.707$  and  $m = 1$ .
- (b) FM, with  $\Delta f = 10$  kHz and  $\Delta f = 50$  kHz
- (c) PM, with  $\Delta\theta = 1$  radian and  $\Delta\theta = \pi$  radian.

**Q21:** A FDM system uses SSB – SC modulation and FM main carrier modulation. There are forty (40) equal bandwidth voice input channels, each bandlimited to 3.3 kHz. A 0.7 kHz guard band is allowed between channels and below the first channel:

- (a) Determine the final transmission bandwidth if the peak frequency deviation is 800KHz.
- (b) Compute the degradation in signal to noise of nput No.40 when compared to the input No.1 (Assume a white main spectral density to the discriminator and no deemphasis).

**Ans: (a) 1.92 MHz (b) 36 dB.**

**Q22:** Prove that NBFM requires the same transmission bandwidth as the AM.

# Chapter 6

## Pulse and Digital Modulation

### Sampling Theorem:

A signal band limited to B Hz by regularly-spaced samples, provided sampling rate is at least 2B sample per second.

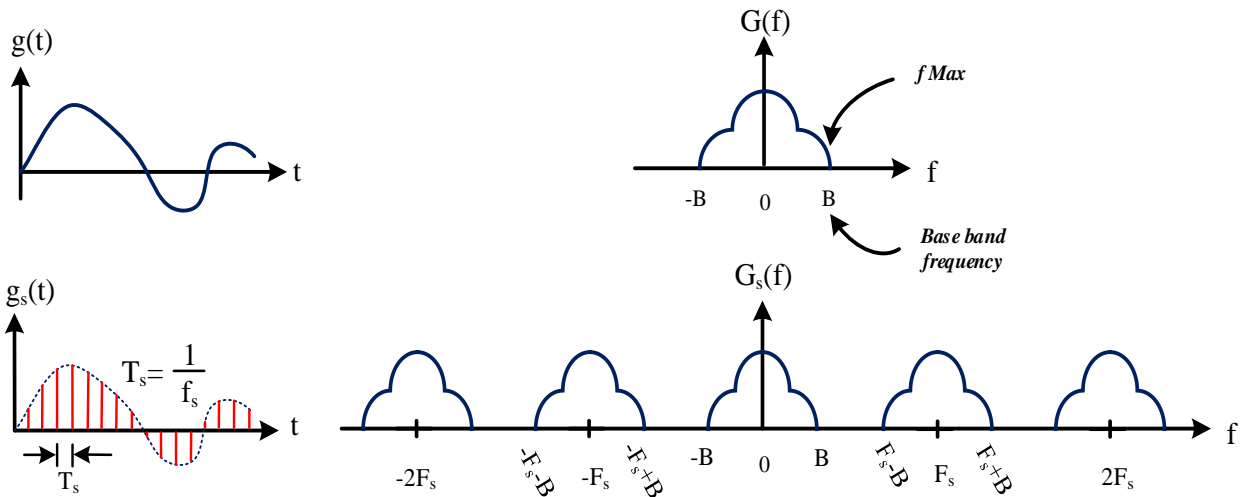
$$F_s \geq 2B$$

$$F_s \geq 2f_{max}$$

Or ... (6-1)

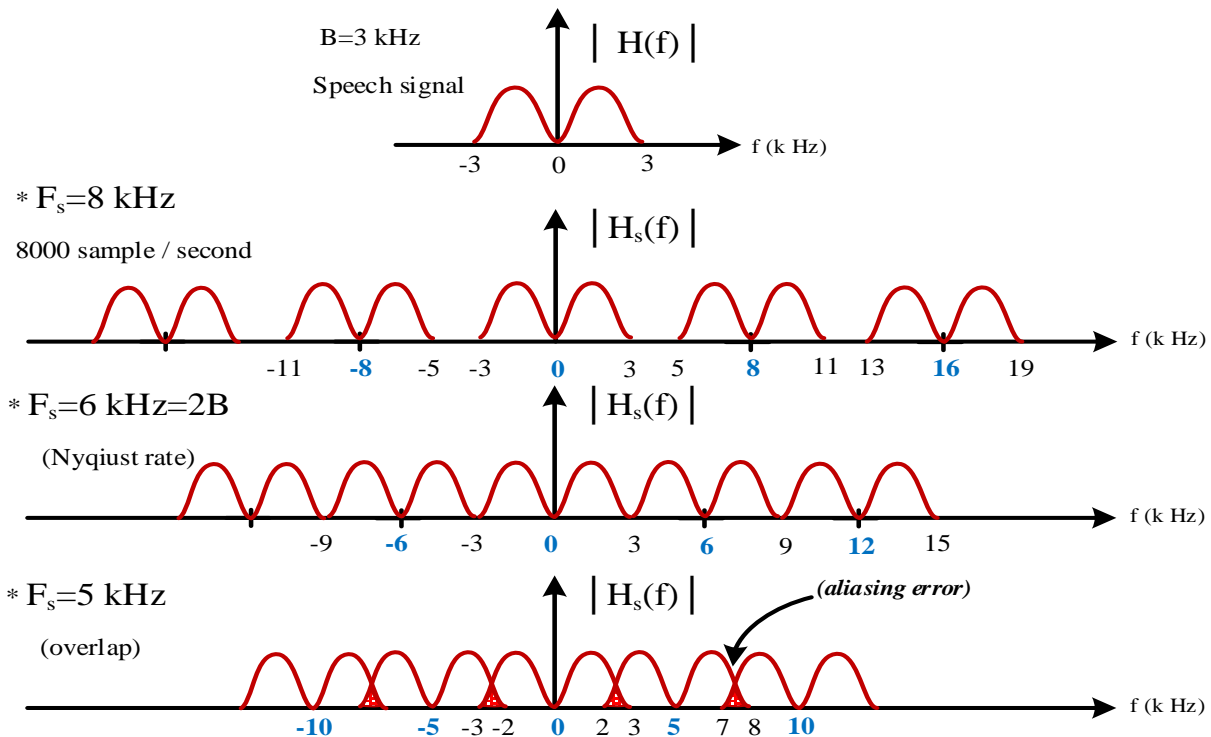
$$F_s = 2f_{max}$$

Minimum sampling rate or Nyquist sampling rate ... (6-2)



$$g_s(t) = g(t) \sum_{n=-\infty}^{\infty} \delta(t - nT_s) = \frac{1}{T_s} \sum_{n=-\infty}^{\infty} g(t) e^{jn\omega_s t}$$

$$G_s(\omega) = \frac{1}{T_s} \sum_{n=-\infty}^{\infty} G(\omega - n\omega_s)$$

**Effect of sampling on a signal spectrum:**

**Ex 6-1:** Determine the Nyquist rate of the sampling for the signal:

$$g(t) = 10 \cos 100\pi t + 15 \cos 150\pi t + 5 \cos 300\pi t$$

**Solution:**

$$f_{max} = \frac{300\pi}{2\pi} = 150 \text{ Hz}$$

$$\text{Nyquist rate} = 2f_{max} = 2 \times 150 = 300 \text{ Hz}$$

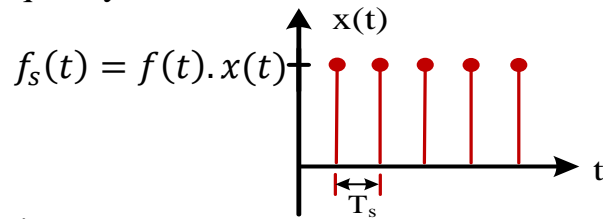
**H.W:**

Determine the Nyquist rate of sampling required for

a)  $g(t) = 10 \cos 100\pi t \cos 200\pi t$

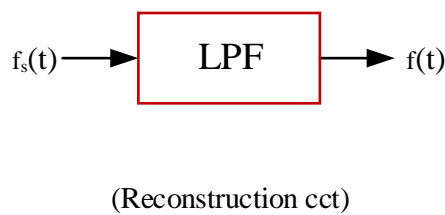
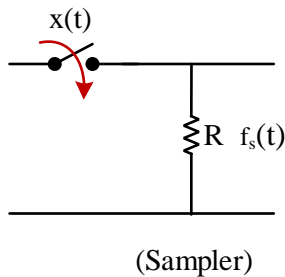
b)  $g(t) = e^{-2|t|}$  (approximate the BW where  $|G(\omega)|$  drops to value less than 0.1)

The sampler behaves exactly as a multiplier. It multiplies  $f(t)$  by a gating function  $x(t)$  which is a train of impulses with frequency  $f_s$  then,



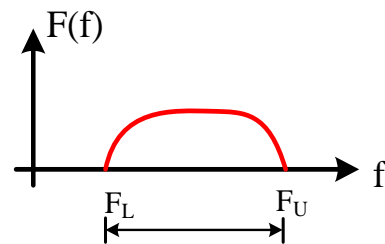
Reconstruction of  $f(t)$  from  $f_s(t)$  is

done using LPF with cutoff  $f_{max}$



**Note:**

If  $f(t)$  is a baseband signal over a frequency range  $f_L$  to  $f_u$  such that  $B=f_u - f_L$  then sampling theorem of such signals states that  $f(t)$  can be completely recovered from  $f_s(t)$  if:



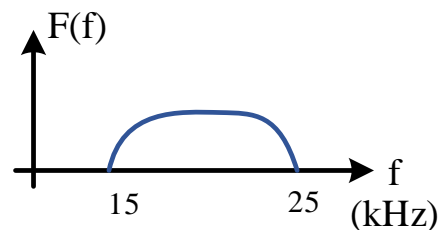
$$f_s = \frac{2f_u}{k}, \text{ where } k \text{ is the largest integer not exceeding } \frac{f_u}{B}$$

**Ex 6-2:**

For the signal shown besides,  $F_s = \frac{2 \cdot (25)}{k}$  where  $k =$

$$\text{int} \left( \frac{25}{10} \right) = 2$$

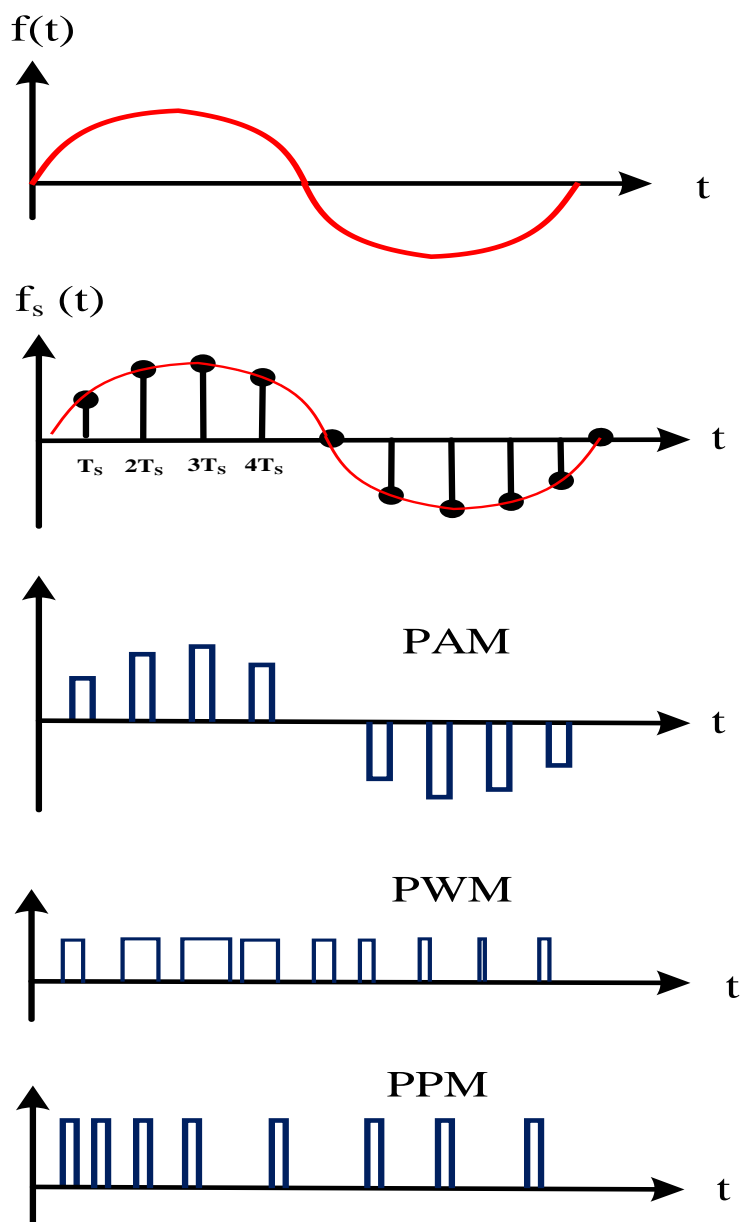
$$f_s = \frac{2 \times (25)}{2} \text{ or } f_s = 25 \text{ kHz}$$



Reconstruction in such case has done using BPF

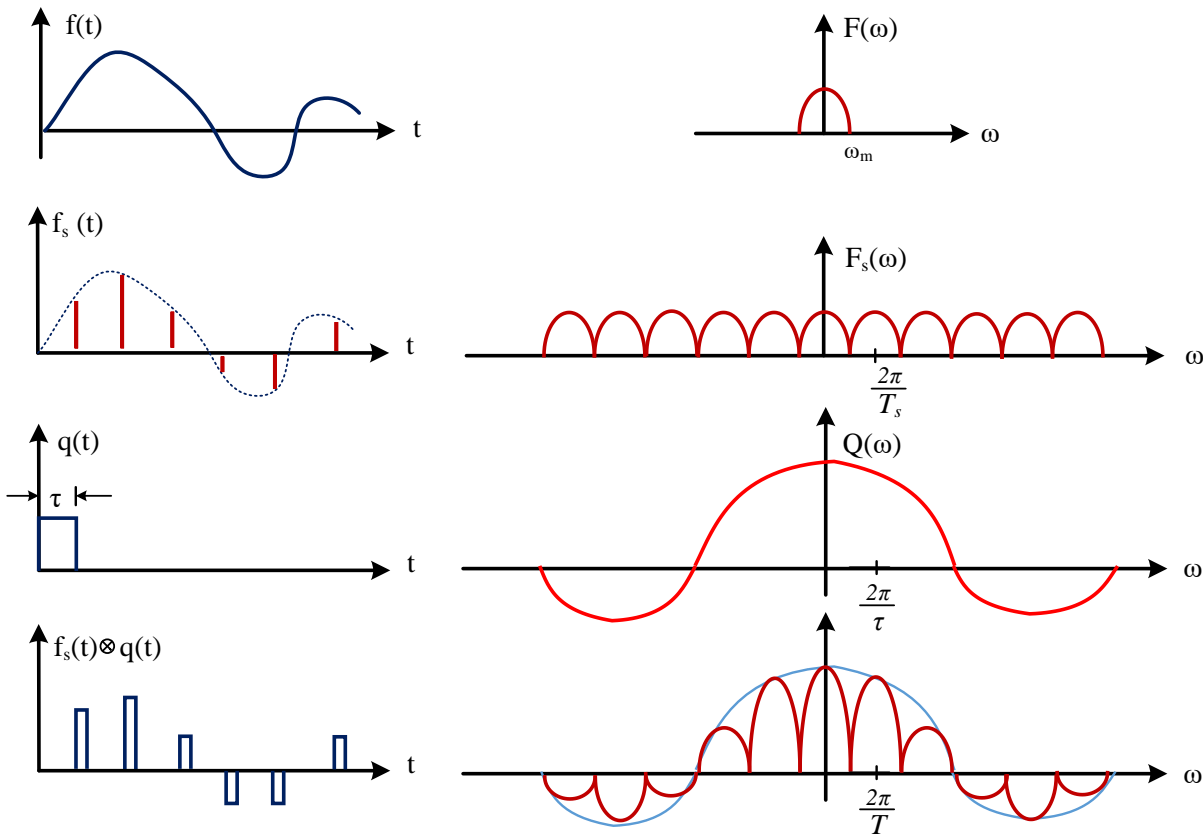
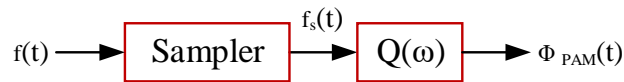
### Pulse Modulation Techniques:

If an analog signal is sampled, the sampled values may be used to modify certain parameter of a periodic train pulses (amplitude, width or position). Accordingly, we have Pulse Amplitude Modulation (PAM), Pulse Width Modulation (PWM) or Pulse Position Modulation (PPM).



### 1- PAM

#### Generation:



Pulse Amplitude modulation the same as the output of the sampled at rate  $f_s$  ( $f_s \geq 2f_{max}$  for baseband signals).

$$\Phi_{PAM}(nT_s) = \sum_{n=-\infty}^{\infty} f(nT_s) q(t - nT_s) \quad \dots (6-3)$$

PAM is usually used as TDM-PAM (TDM=Time Division Multiplexing) to transmit more than one message at the same channel.

#### Detection:

