



# Three-phase Rectifiers

## Lecture 12

Electrical Engineering Department  
Power Electronics and Special Machine

By

Dr. Mustafa Fadel

# Important Notice

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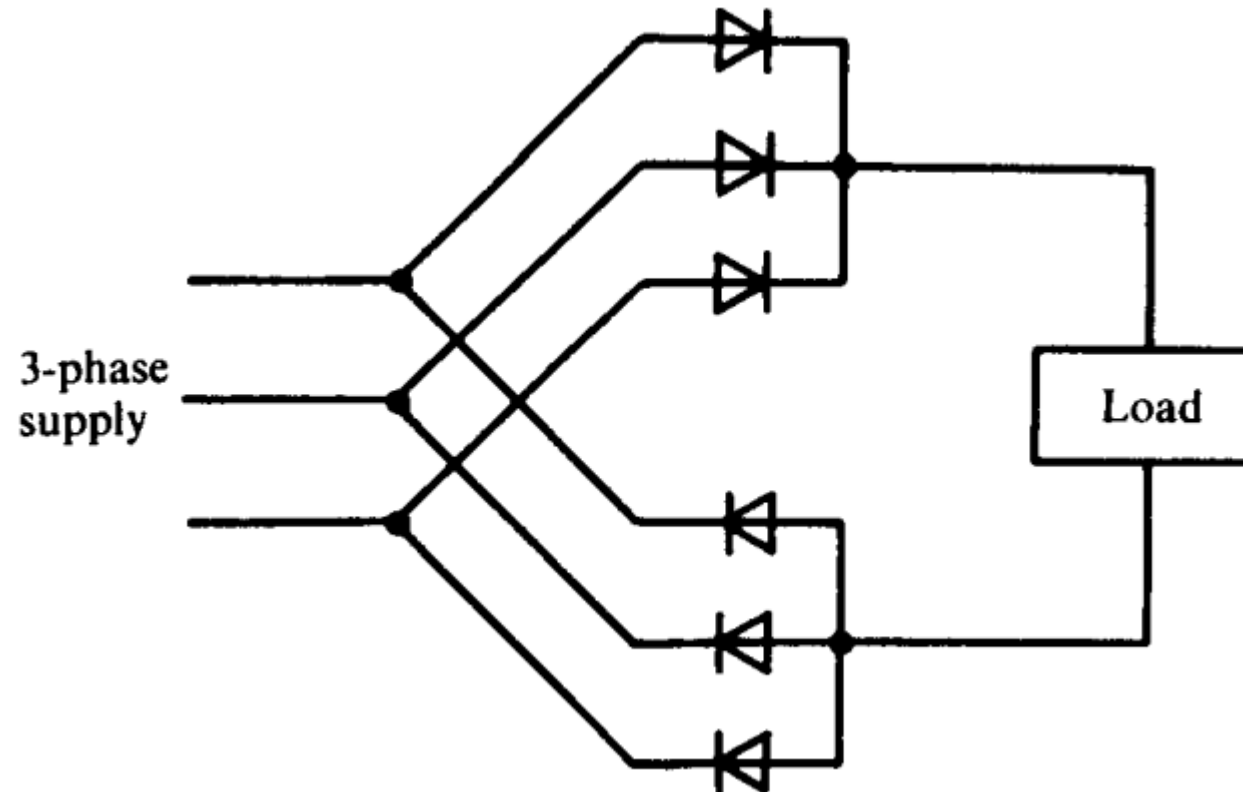
## Note to Students:

These lecture materials are provided as supplementary support to help clarify and reinforce the concepts discussed in the main course lectures. They are not a substitute for the official course materials or the primary references assigned. Students are encouraged to refer to the original sources and attend the main lectures to ensure full understanding of the subject.

# Uncontrolled Three-phase Bridge Rectifier(or Double-way)

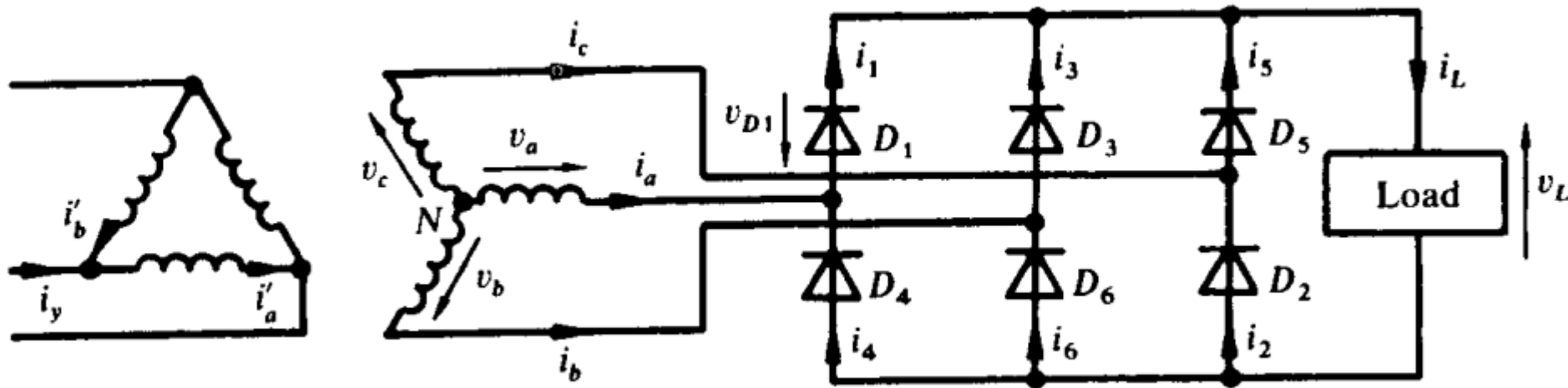
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The circuit of three-phase bridge rectifier feeding load is shown below



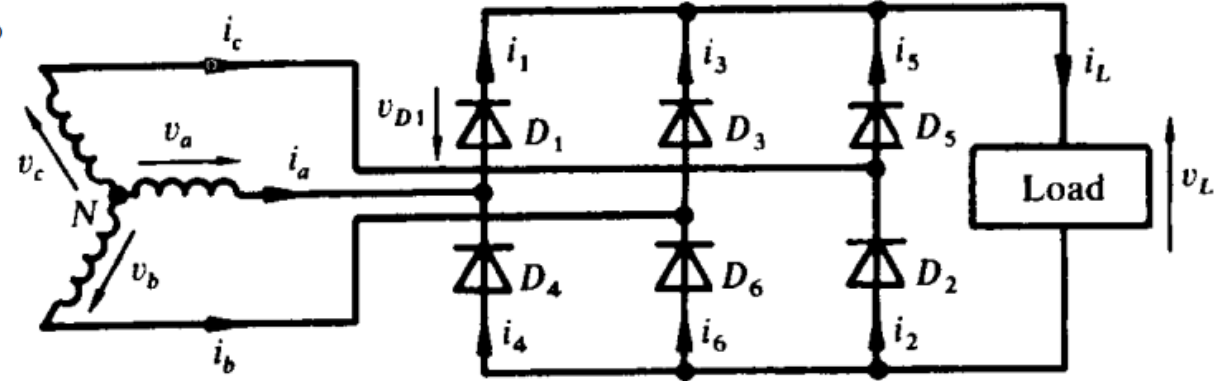
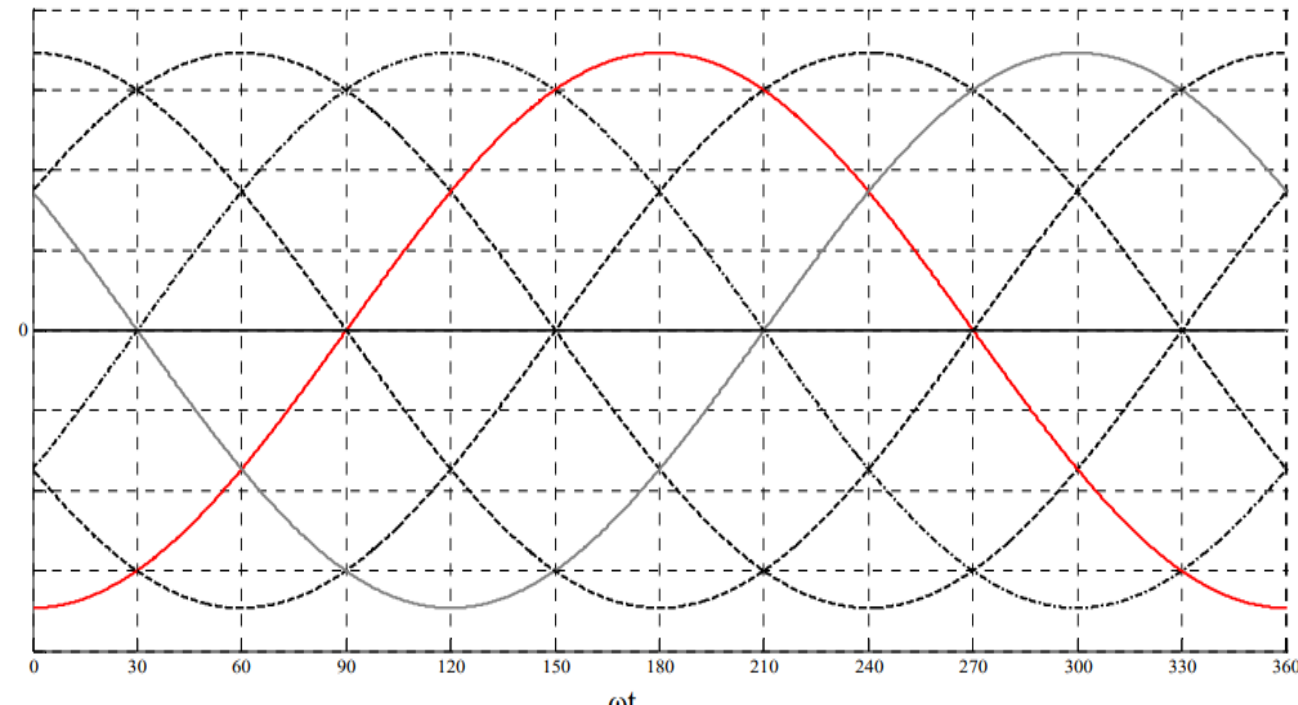
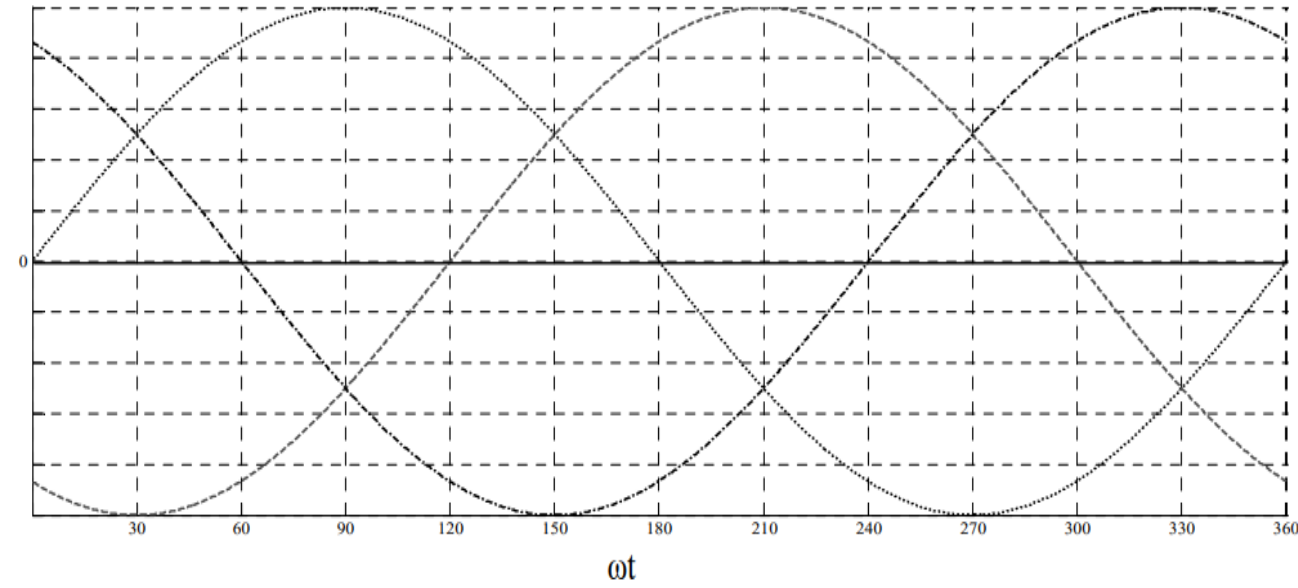
# Uncontrolled Three-phase Bridge Rectifier(or Double-way)

Another representation for circuit of three-phase uncontrolled bridge rectifier feeding load is shown below:



# Uncontrolled Three-phase Bridge Rectifier(or Double-way)

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## Uncontrolled Three-phase Bridge Rectifier(or Double-way)

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The six voltages of three-phase bridge rectifier can be written as:

$$V_{ab} = V_a - V_b = \sqrt{3} V_m \sin(\omega t + 30^\circ)$$

$$V_{ac} = V_a - V_c = \sqrt{3} V_m \sin(\omega t - 30^\circ)$$

$$V_{bc} = V_b - V_c = \sqrt{3} V_m \sin(\omega t - 90^\circ)$$

$$V_{ba} = V_b - V_a = \sqrt{3} V_m \sin(\omega t - 150^\circ)$$

$$V_{ca} = V_c - V_a = \sqrt{3} V_m \sin(\omega t - 210^\circ)$$

$$V_{cb} = V_c - V_b = \sqrt{3} V_m \sin(\omega t + 270^\circ)$$

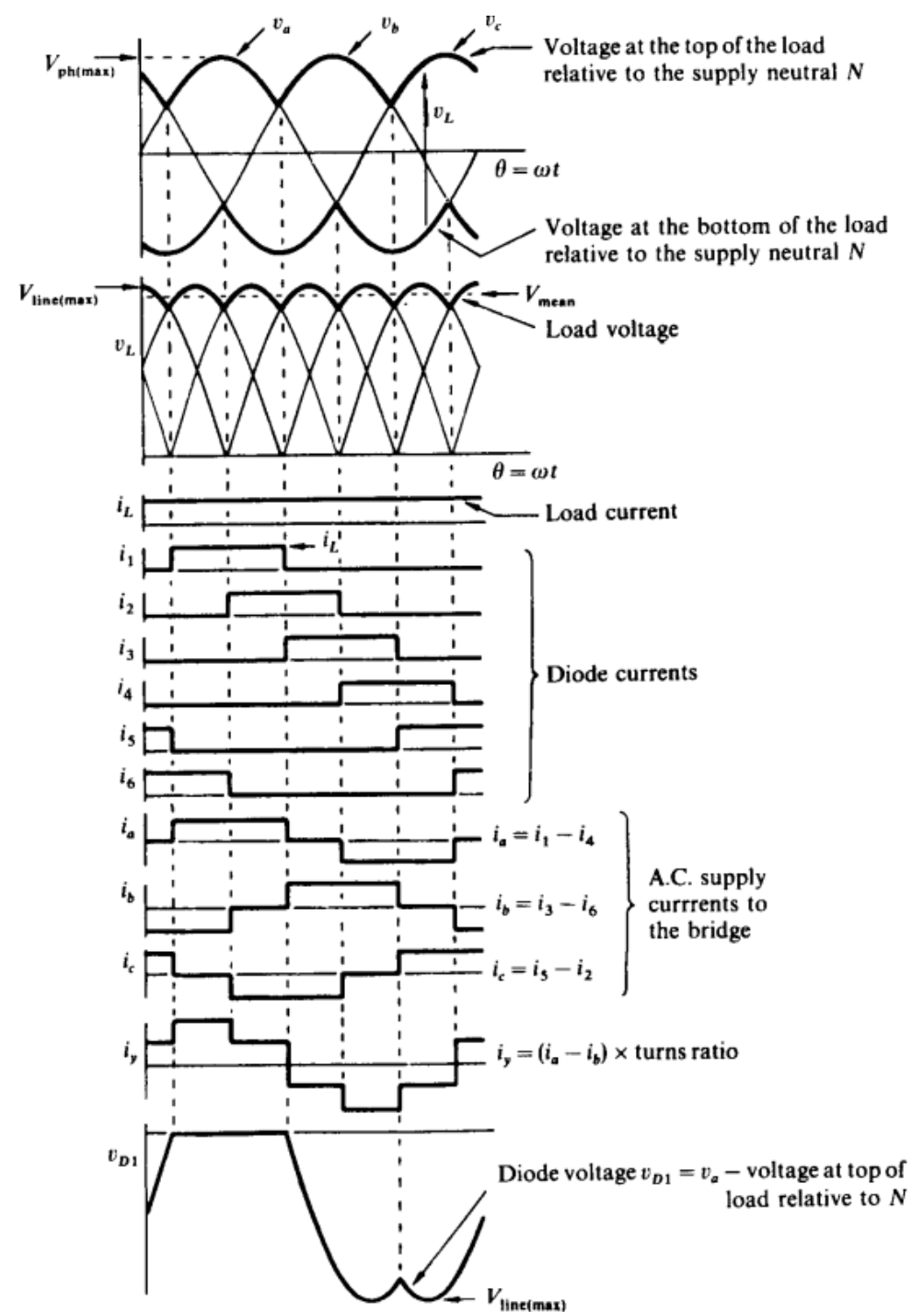
# Uncontrolled Three-phase Bridge Rectifier(or Double-way)

The waveforms of three-phase full-wave rectifier feeding load is shown:

The mean load voltage is

$$V_{mean} = \frac{1}{2\pi/6} \int_{\pi/3}^{\frac{2\pi}{3}} V_{line} \sin(\omega t) d\omega t$$

$$V_{mean} = \frac{3V_{line}}{\pi} \text{ OR } \frac{3\sqrt{3}V_{phase}}{\pi}$$



## **Uncontrolled Three-phase Bridge Rectifier(or Double-way)**

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Example: A three-phase bridge uncontrolled rectifier supplies a DC load of 300 V, 60 A from a 415 V, 3-phase AC supply via a delta-star transformer. Determine the required diode and transformer specification. Assume a diode voltage drop of 0.7 V and continuous load current.

# Uncontrolled Three-phase Bridge Rectifier(or Double-way)

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Solution:

$$V_{mean} = \frac{3V_{line}}{\pi} - (2 \times 0.7) \qquad V_{phase,rms} = \frac{V_{phase}}{\sqrt{2}} = 128.9 V$$

$$300 = \frac{3V_{line}}{\pi} - 1.4$$

$$V_{line} = 315.6 V$$

$$V_{phase} = \frac{V_{line}}{\sqrt{3}} = 182.211 V$$

# Uncontrolled Three-phase Bridge Rectifier(or Double-way)

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Solution:

Diode rating, P.R.V=  $V_{\text{line}}=315.6 \text{ V}$

$$I_{\text{rms}} = \frac{60}{\sqrt{3}} = 34.6 \text{ A}$$

Secondary phase current RMS value  $\left(\frac{60^2+60^2}{3}\right)^{1/2} = 49 \text{ A}$

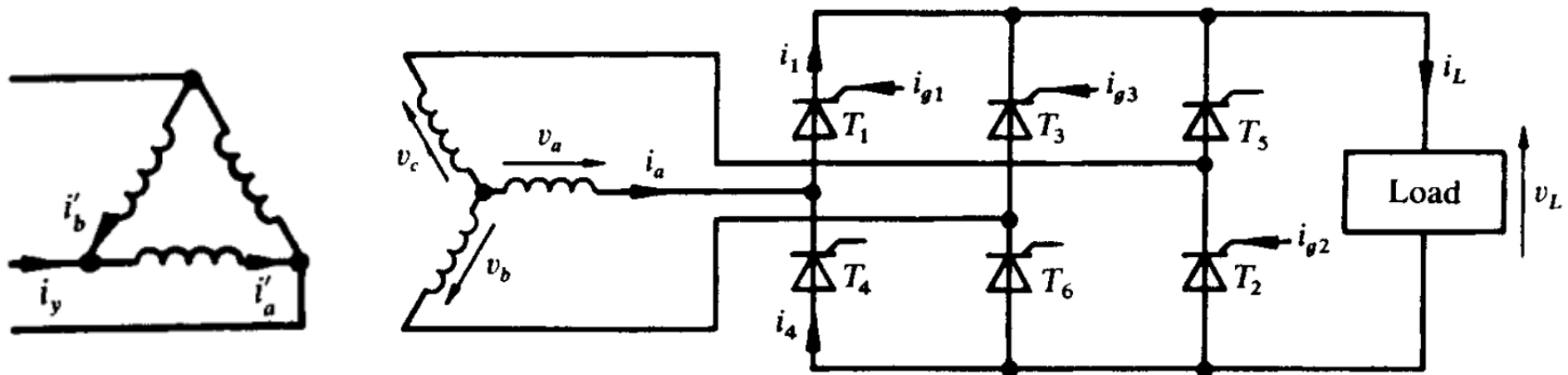
Transformer rating= $3 \times 315.6 \times 49= 18.9 \text{ kVA}$

Transformer ratio = (Primary/ Secondary) =  $415/128.9$

Primary phase RMS current= $49 \times (128.9/415)=15.2 \text{ A}$

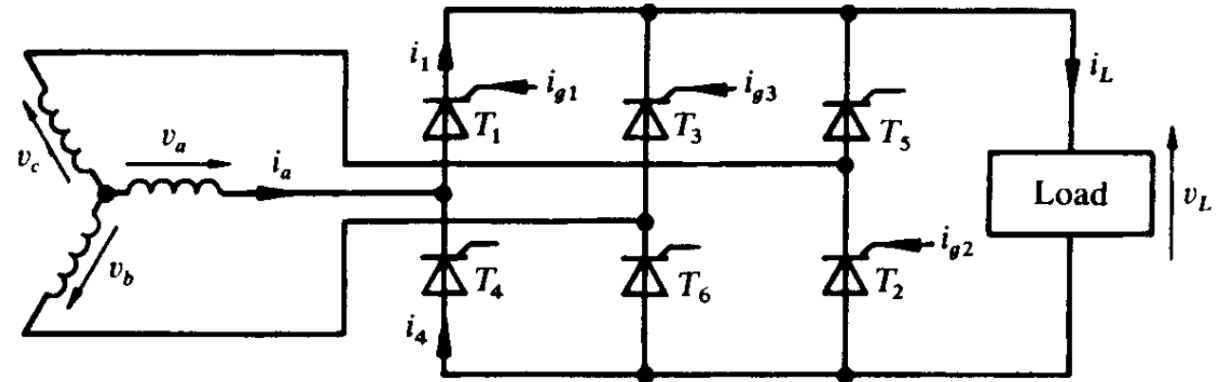
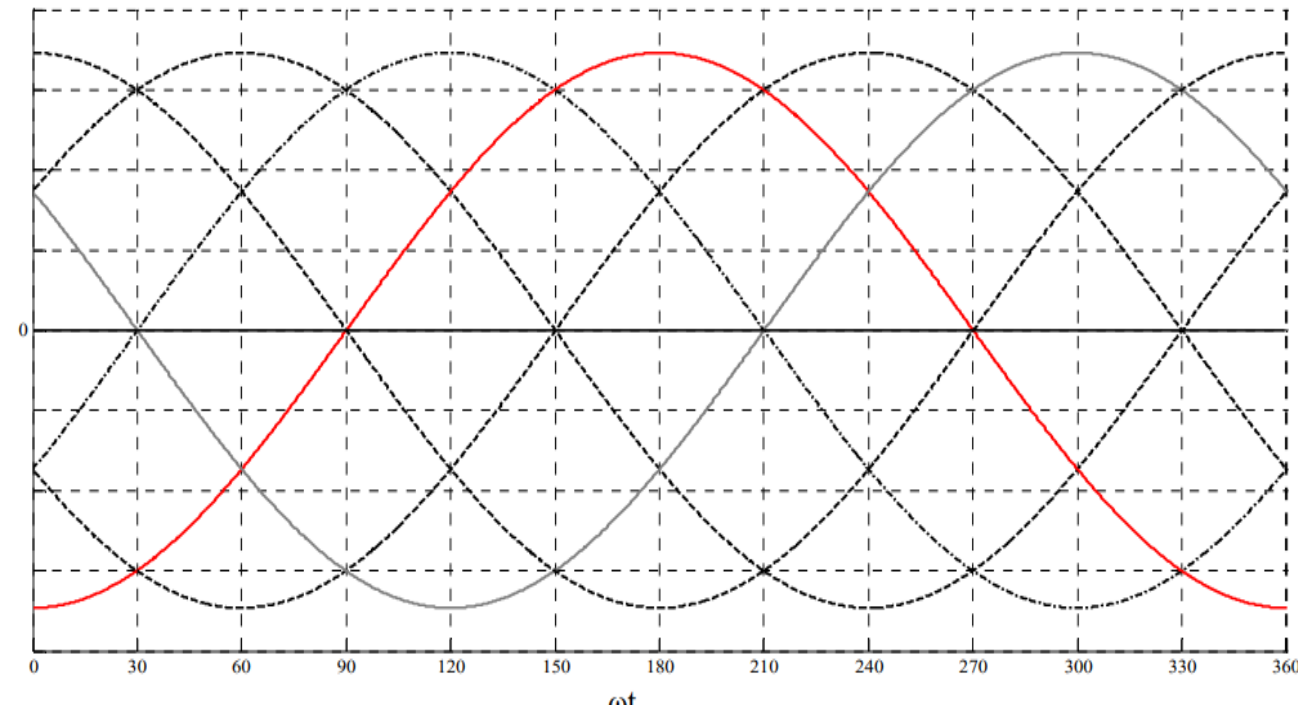
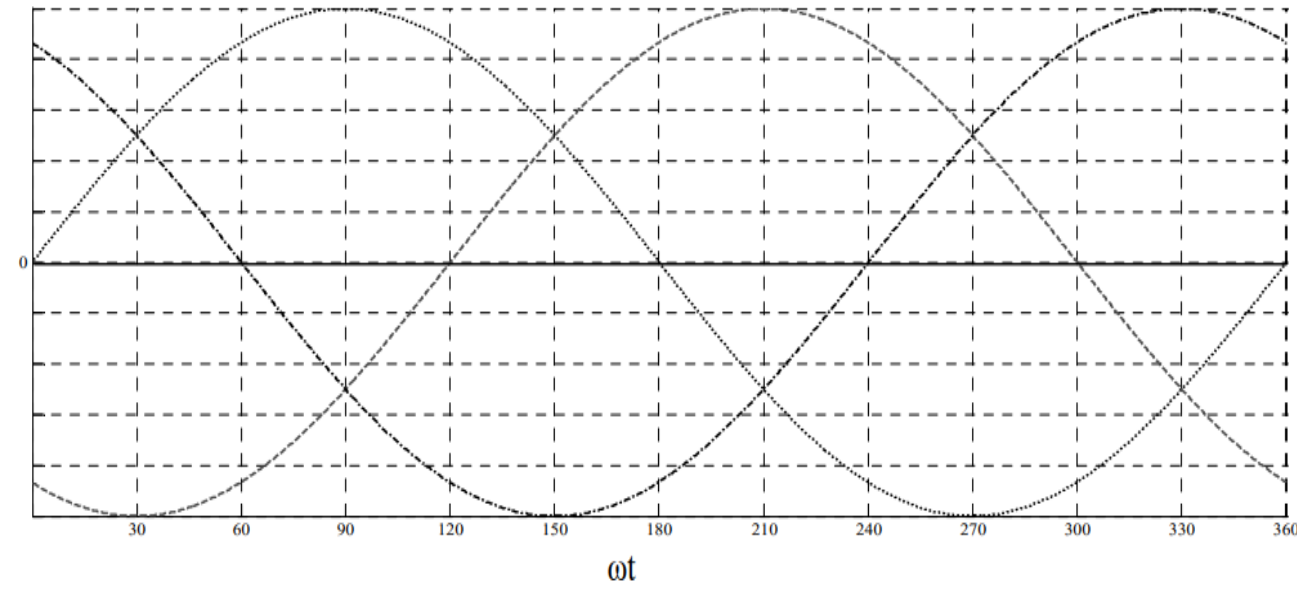
# Fully Controlled Three-phase Bridge Rectifier

The circuit of three-phase fully controlled bridge rectifier feeding load is shown below:



# Fully Controlled Three-phase Bridge Rectifier

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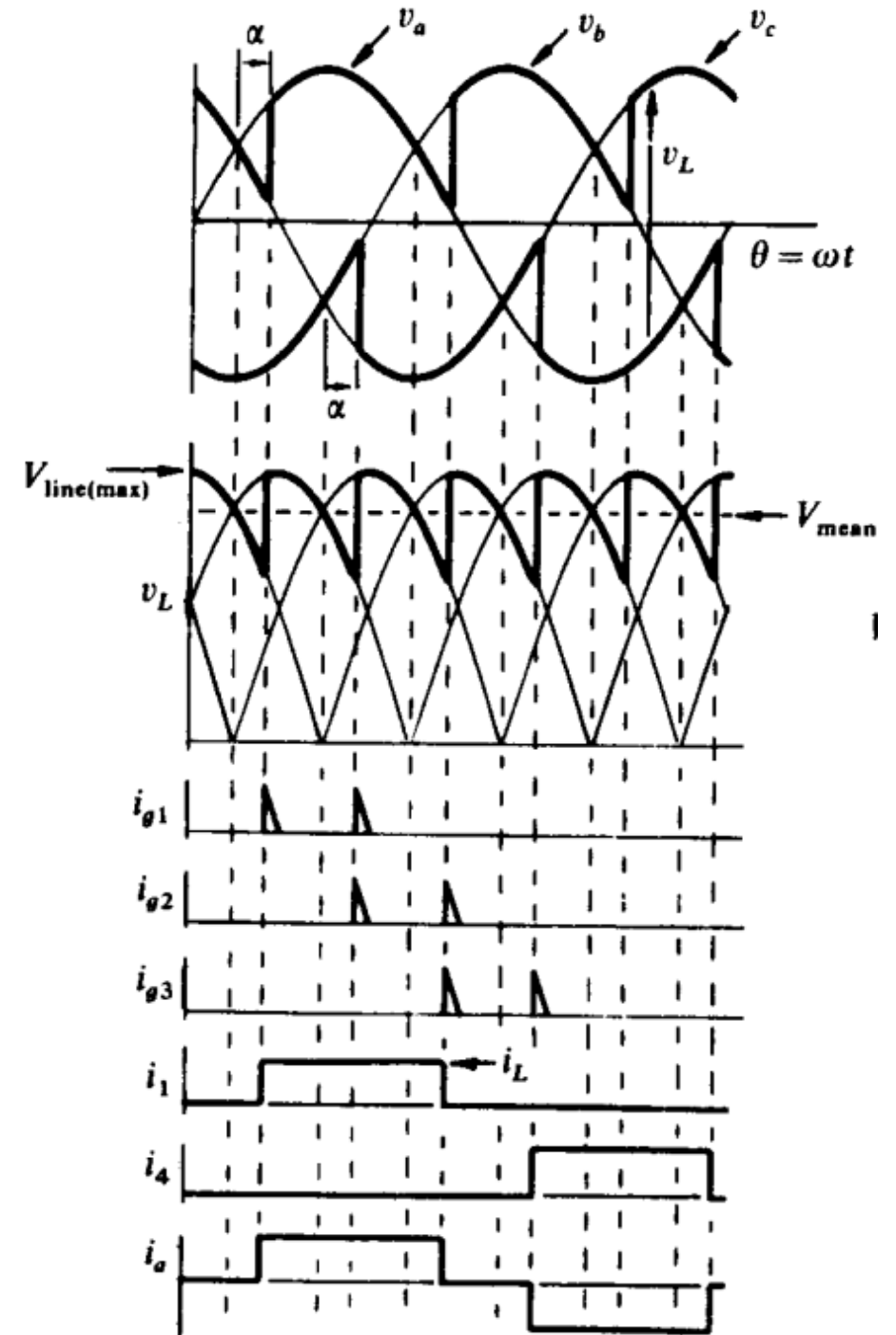
# Fully Controlled Three-phase Bridge Rectifier

The waveforms of three-phase full-wave rectifier feeding load is shown:

The mean load voltage is

$$V_{mean} = \frac{1}{2\pi/6} \int_{\frac{\pi}{3} + \alpha}^{\frac{2\pi}{3} + \alpha} V_{line} \sin(\omega t) d\omega t$$

$$V_{mean} = \frac{3V_{line}}{\pi} \cos \alpha \quad \text{or} \quad \frac{3\sqrt{3}V_{phase}}{\pi} \cos \alpha$$



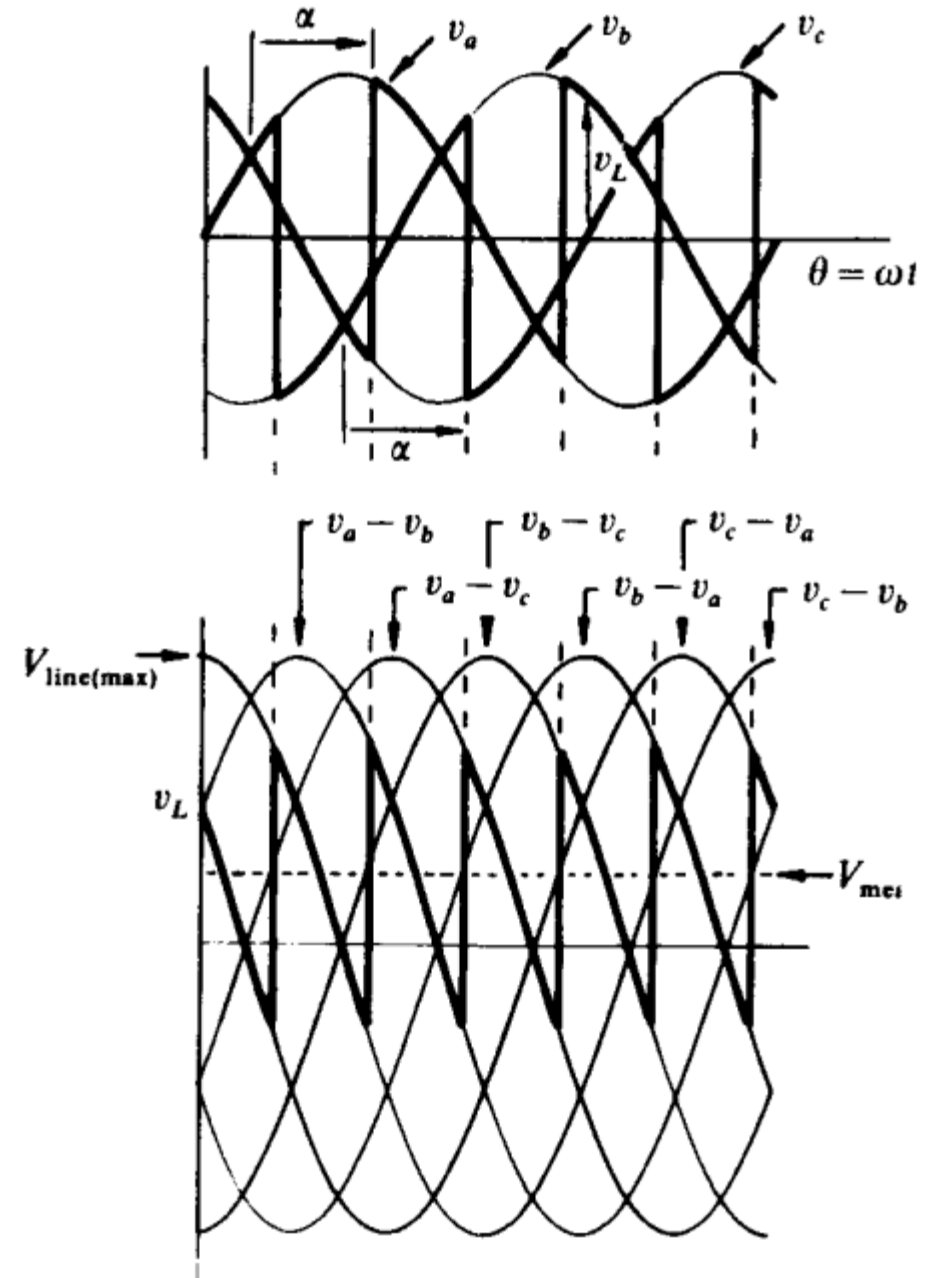
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$$V_{mean} = \frac{3V_{line}}{\pi} \cos \alpha \quad \text{or} \quad \frac{3\sqrt{3}V_{phase}}{\pi} \cos \alpha$$



# Fully Controlled Three-phase Bridge Rectifier

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Example: A fully-controlled three-phase rectifier bridge circuit is supplied by line voltage of 220 V. Assuming continuous load current and a thyristor voltage drop of 1.5 V, determine the mean load voltage at firing delay angles of  $0^\circ$ ,  $30^\circ$ ,  $45^\circ$ ,  $60^\circ$ , and  $90^\circ$ . Plot the waveform of the thyristor voltage at a firing delay angle of  $75^\circ$ .

# Fully Controlled Three-phase Bridge Rectifier

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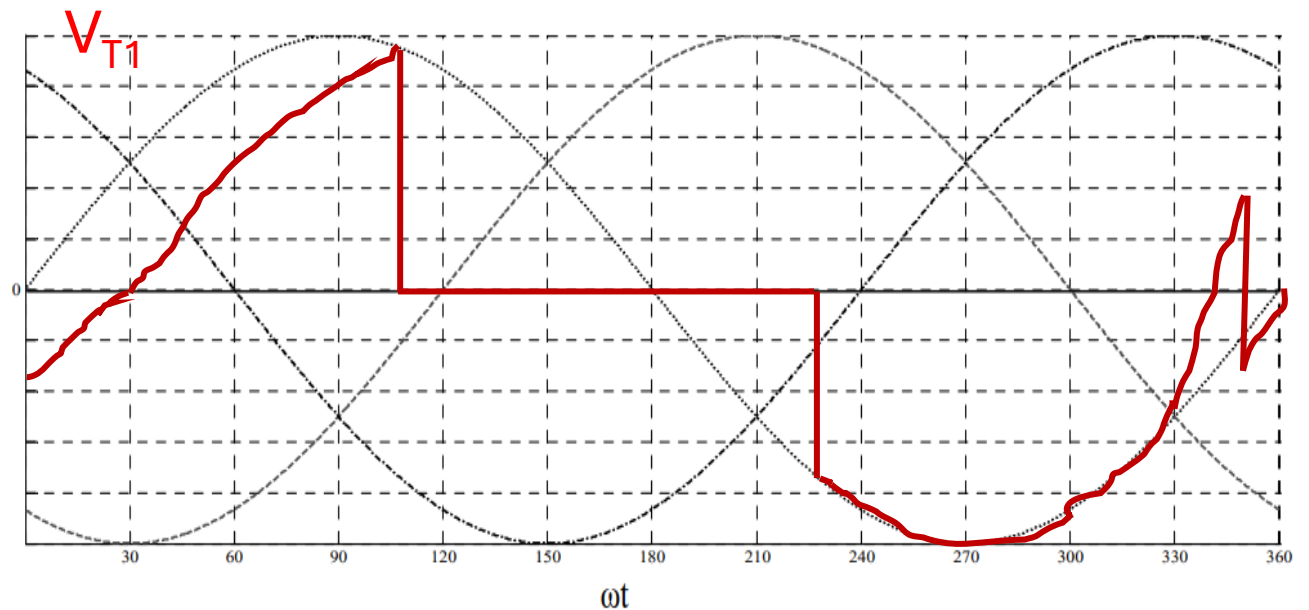
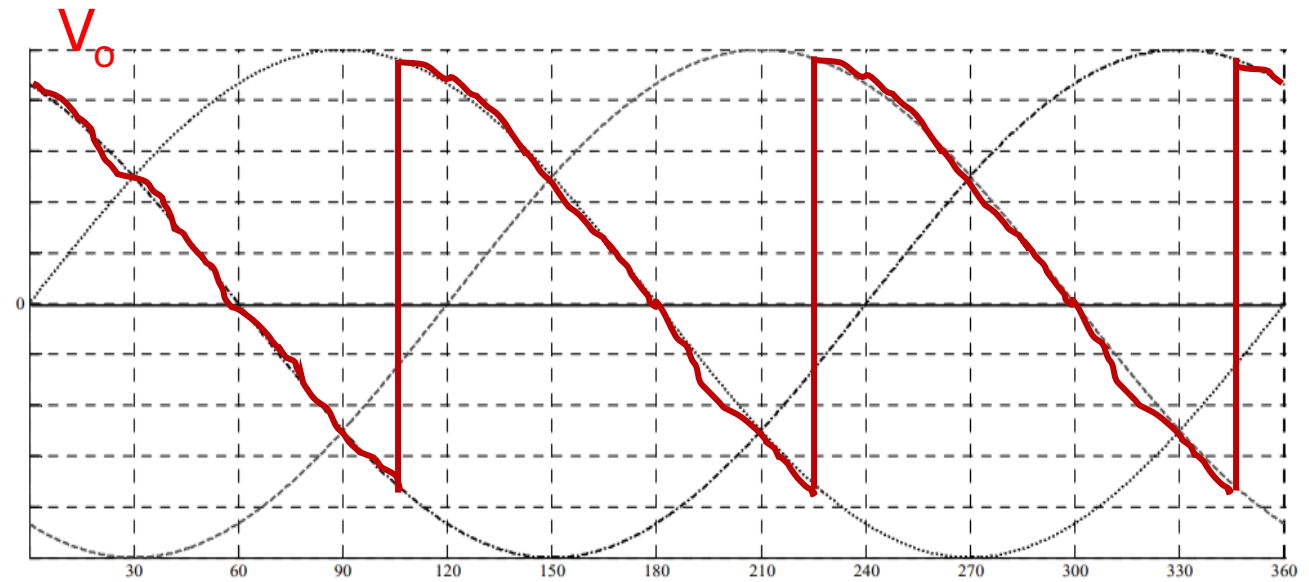
Solution:

$$V_{mean} = \frac{3V_{line}}{2\pi} \cos \alpha - (2 \times 1.5) = \frac{3 \times 220\sqrt{2}}{2\pi} \cos \alpha - (2 \times 1.5)$$

| $\alpha$   | $0^\circ$ | $30^\circ$ | $45^\circ$ | $60^\circ$ | $90^\circ$ |
|------------|-----------|------------|------------|------------|------------|
| $V_{mean}$ | 294 V     | 254 V      | 207V       | 146 V      | 0 V        |

# Fully Controlled Three-phase Bridge Rectifier

Solution: The voltage across thyristor  $T_1$  is given by the phase-A source voltage  $V_a$  minus the load voltage  $V_o$ , i.e.,  $V_{T1} = V_a - V_o$





**Thanks for listening!**