

Cojil Minimization of makespan with precedence  
Pm/ Prc/ Cmax

(\*) In first step, forward pass calculations are made to find out earliest completion times of jobs as under,

Let  $C_j^1 =$  earliest completion time of job  $j$

$$C_j^1 = \max_{i \in Y} (C_i^1) + P_j$$

where  $C_i^1$  is the earliest completion time of job  $i$  that belongs to set  $Y$ . set  $Y$  contains predecessor jobs for job  $j$

(\*) To find critical path on the precedence network, latest completion times of all jobs are calculated as follows:

Let  $C_j^2 =$  latest completion time of job  $j$

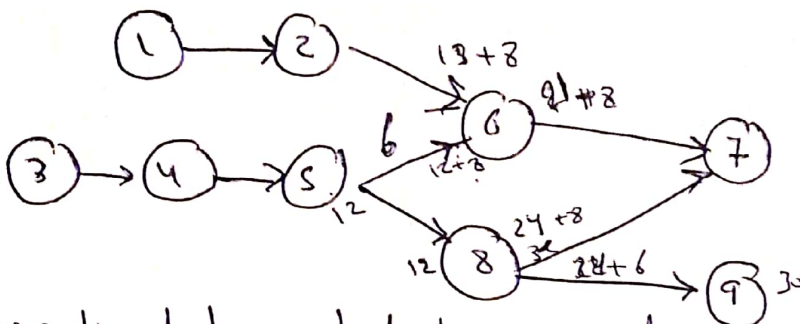
$$C_j^2 = \min_{k \in \Omega} (C_k^2 - P_k)$$

where  $C_k^2 =$  latest completion time of job  $k$  that belongs to set  $\Omega$   
set  $\Omega$  contains successor jobs for job  $j$ . All the jobs without any successor are assigned a value equal to  $C_{max}$  for backward pass calculations.

(1)

Q10 A parallel shop has nine jobs with process times as follows

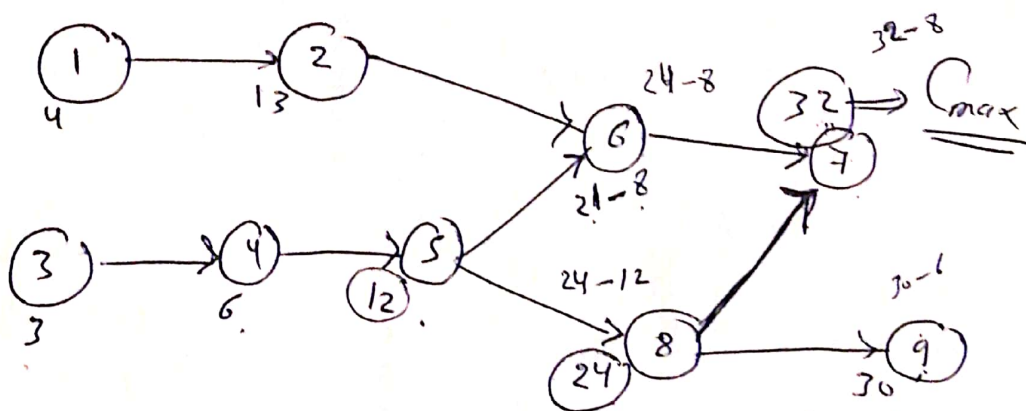
Job	1	2	3	4	5	6	7	8	9
$P_j$	4	9	3	3	6	8	8	12	6



use directed graph technique and find ① makespan ② critical path

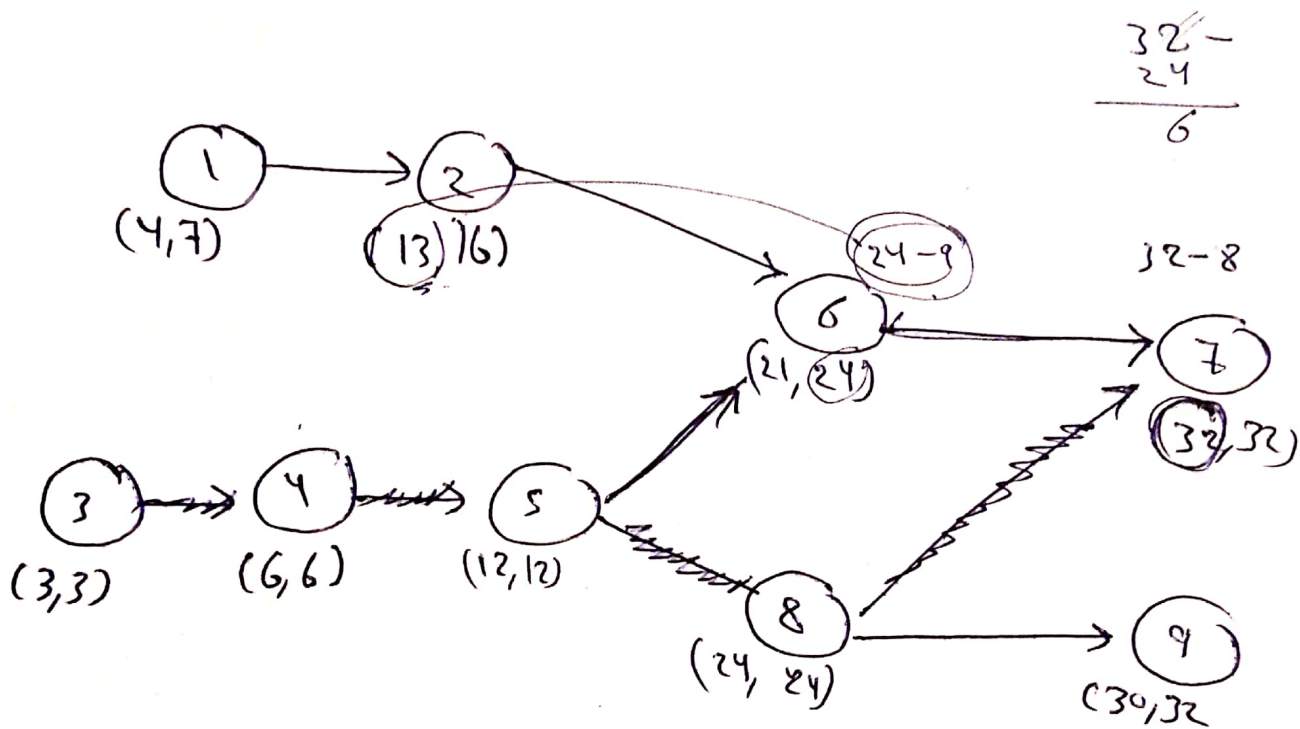
Solution The earliest completion time  $C_j'$  of all jobs are shown below in table

Job	1	2	3	4	5	6	7	8	9
$P_j$	4	9	3	3	6	8	8	12	6
$C_j'$	4	13	3	6	12	21	32	24	30



Precedence diagram showing earliest completion times

$$C_8'' = \min \{ C_7'' - P_7, C_9'' - P_9 \} = \min \{ 32 - 8, 32 - 6 \} = \min \{ 24, 26 \} = 24$$



$$\frac{32 - 24}{6}$$

$$32 - 8$$

critical path (J<sub>3</sub>-J<sub>4</sub>-J<sub>5</sub>-J<sub>8</sub>-J<sub>7</sub>) for the precedence diagram