

**Exercises(2-12):**

- Let  $P$  and  $Q$  be two normal  $p$ -subgroups of a finite group  $G$ . Show that  $PQ$  is a normal  $p$ -subgroup of  $G$ .
- Determine whether  $(\mathbb{Z}_{125}, +_{125})$  is a  $p$ -group.
- Determine whether  $(\mathbb{Z}_{121}, +_{121})$  is a  $p$ -group.
- Determine whether  $(\mathbb{Z}_{41}, +_{41})$  is a  $p$ -group.
- Determine whether  $(\mathbb{Z}_{16}, +_{16})$  is a  $p$ -group.
- Determine whether  $(\mathbb{Z}_{625}, +_{625})$  is a  $p$ -group.
- Determine whether  $(\mathbb{Z}_{185}, +_{185})$  is a  $p$ -group.
- Determine whether  $(\mathbb{Z}_{128}, +_{128})$  is a  $p$ -group.
- Determine whether  $(\mathbb{Z}_{256}, +_{256})$  is a  $p$ -group.
- Determine whether  $(\mathbb{Z}_{100}, +_{100})$  is a  $p$ -group.
- Show that  $G_\ell = \{\pm 1, \pm i, \pm j, \pm k\}, \cdot$  is a  $p$ -group.