# LAB. METEOROLOGICAL DATA ANALYSIS ........ FOURTH STAGE 

(The second Semester)

## Department of Atmospheric Sciences

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## Lecturers :

Assist. Prof. Zahra salah , L. Ruaa mazin
L. Farah Haseeb , L. Luma Mahdi
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## ((The First Lecture))

## correlation coefficient

It is the relationship between two variables representing each of the two variables or phenomena (linear relationship).

If one of the two phenomena changes in a certain direction, the second changes in the direction of the first or in an opposite direction to the first,
*If the two changes appear in the same direction, meaning an increase in the first, corresponding to an increase in the second, or a decrease in the first, corresponding to a decrease in the second, then the relationship is direct increasing (positive).

* If the increase in the first is offset by a decrease in the second, or vice versa, the correlation is inverse or decreasing (negative).
* acrrelation of zero means there is no relationship( dis corrrlation) between the two variables.


## Correlation scale :

1-pearson correlation $(r)$ :is astatisical formula that measures linear correlation between two variables Xand Y.

The strength of the correlation between two variables ( $r$ ) is measured and denoted by the correlation coefficient, It is a numerical measure that measures the strength of the correlation between two variables, where its value ranges between ( +1 and -1 ).

$$
\mathrm{r}=\frac{n\left(\sum x y\right)-\left(\sum x\right)\left(\sum y\right)}{\sqrt{\left.\left[n \sum x^{2}-\left(\sum x\right)^{2}\right]\left[n \sum y^{2}-\left(\sum y\right)^{2}\right)\right]}}
$$

## where :

r = Pearson Coefficient
$\mathrm{n}=$ Data number
$\Sigma \mathrm{xy}=$ sum of products of the paired stocks
$\Sigma \mathrm{x}=$ sum of the x scores
$\Sigma y=$ sum of the $y$ scores
$\Sigma \mathrm{x} 2=$ sum of the squared x scores
$\Sigma \mathrm{y} 2=$ sum of the squared y scores

- To calculate the correlation , the excel program is done using a function
= correl
the following table shows the types of correlation and the direction of the relationship for each type:

| Type of correlation and relationship | positive value |
| :--- | :---: |
| dis correlation | $\mathbf{0}$ |
| Weak direct correlation | $>+\mathbf{0 . 5}$ |
| Direct correlation is acceptable | $\mathbf{+ 0 . 5}$ |
| Medium direct correlation | $\mathbf{+ 0 . 6}$ |
| good direct correlation | $\mathbf{+ 0 . 7}$ |
| Very good correlation | $\mathbf{+ 0 . 8}$ |
| Excellent or strong direct correlation | $\mathbf{+ 0 . 9}$ |
| perfect connection | $\mathbf{+ 1}$ |


| Type of correlation and relationship | Negative value |
| :--- | :---: |
| Weak reverse correlation | $\mathbf{> - 0 . 5}$ |
| Acceptable reverse correlation | $\mathbf{- 0 . 5}$ |
| Medium reverse correlation | $\mathbf{- 0 . 6}$ |
| Good reverse correlation | $\mathbf{- 0 . 7}$ |
| Very good reverse correlation | $\mathbf{- 0 . 8}$ |
| strong reverse correlation | $\mathbf{- 0 . 9} \mathbf{- 1}$ |

Example (1) // The following data represents temperature and relative humidity, Find is the pearson coefficient (low, function).

| $\mathbf{T}$ | $\mathbf{3 3}$ | $\mathbf{3 5}$ | $\mathbf{3 4}$ | $\mathbf{3 3}$ | $\mathbf{3 3 . 5}$ | $\mathbf{3 6}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| RH | $\mathbf{5 5}$ | $\mathbf{5 6}$ | $\mathbf{6 0}$ | $\mathbf{5 4}$ | $\mathbf{5 0}$ | $\mathbf{4 5}$ |

Solue\

$$
\mathrm{r}=\frac{n\left(\sum x y\right)-\left(\sum x\right)\left(\sum y\right)}{\sqrt{\left.\left[n \sum x^{2}-\left(\sum x\right)^{2}\right]\left[n \sum y^{2}-\left(\sum y\right)^{2}\right)\right]}} \quad \mathrm{n}=6
$$

| NO | $\mathbf{X}$ | $\mathbf{Y}$ | $\mathbf{X Y}$ | $\mathbf{X}^{\mathbf{2}}$ | $\mathbf{Y}^{\mathbf{2}}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $\mathbf{3 3}$ | $\mathbf{5 5}$ | $\mathbf{1 8 1 5}$ | $\mathbf{1 0 8 9}$ | $\mathbf{3 0 2 5}$ |
| $\mathbf{2}$ | $\mathbf{3 5}$ | $\mathbf{5 6}$ | $\mathbf{1 9 6 0}$ | $\mathbf{1 2 2 5}$ | $\mathbf{3 1 3 6}$ |
| $\mathbf{3}$ | $\mathbf{3 4}$ | $\mathbf{6 0}$ | $\mathbf{2 0 4 0}$ | $\mathbf{1 1 5 6}$ | $\mathbf{3 6 0 0}$ |
| $\mathbf{4}$ | $\mathbf{3 3}$ | $\mathbf{5 4}$ | $\mathbf{1 7 8 2}$ | $\mathbf{1 0 8 9}$ | $\mathbf{2 9 1 6}$ |
| $\mathbf{5}$ | $\mathbf{3 3 . 5}$ | $\mathbf{5 0}$ | $\mathbf{1 6 7 5}$ | $\mathbf{1 1 2 2 . 2 5}$ | $\mathbf{2 5 0 0}$ |
| $\mathbf{6}$ | $\mathbf{3 6}$ | $\mathbf{4 5}$ | $\mathbf{1 6 2 0}$ | $\mathbf{1 2 9 6}$ | $\mathbf{2 0 2 5}$ |
| $\mathbf{n}=\mathbf{6}$ | $\sum \mathbf{x}=\mathbf{2 0 4 . 5}$ <br> $\sum \mathbf{x}^{2}=\mathbf{4 1 8 2 0 . 2 5}$ | $\sum \mathbf{y}=\mathbf{3 2 0}$ <br> $\sum \mathbf{y}^{\mathbf{2}}=\mathbf{1 0 2 4 0 0}$ | $\sum=\mathbf{1 0 8 9 2}$ | $\sum=\mathbf{6 9 7 7 . 2 5}$ | $\sum=\mathbf{1 7 2 0 2}$ |

$\mathbf{r}=\frac{6(10892)-(204.5)(320)}{\sqrt{[6(6977.25)-(41820.25)][6(17202)-(102400)]}} \rightarrow \mathbf{r}=\quad \rightarrow \mathbf{r}=$
relationship is
Example (2) // Find is the pearson coefficient (low, function ) for the following table:

| NO | X | Y |
| :---: | :---: | :---: |
| 1 | 40 | 78 |
| 2 | 21 | 70 |
| 3 | 25 | 60 |
| 4 | 31 | 55 |
| 5 | 38 | $\mathbf{8 0}$ |
| $\mathbf{6}$ | $\mathbf{4 7}$ | $\mathbf{6 6}$ |

Multiple correlation coefficient:
This coefficient, which is symbolized by the symbol $R$, also measures the strength of the relationship between more than two variables, which are continuous random variables (multivariate distribution), and calculating the value of $R$ is an extension of the value of the simple correlation coefficient ( $r$ ) with the replacement of $X, Y$ with $X 1-X k, Y$ and taking three variables $X 1, X 2$, $X 3$ we get the following formulas:

$$
\begin{aligned}
& \mathrm{Y}, \mathrm{X}_{1}, \mathrm{X}_{2} \\
& r_{Y X_{1}}=\frac{n \sum Y X_{1}-\sum Y \sum X_{1}}{\sqrt{N \sum Y_{I}^{2}-\left(\sum Y_{I}\right)^{2}} \sqrt{n \sum X_{1}^{2}-\left(\sum X_{1}\right)^{2}}} \\
& r_{Y X_{2}}=\frac{n \sum Y X_{2}-\sum Y \sum X_{2}}{\sqrt{n \sum Y_{1}^{2}-\left(\sum Y_{1}\right)^{2}} \sqrt{n \sum X_{2}^{2}-\left(\sum X_{2}\right)^{2}}} \\
& r_{X_{1} X_{2}}=\frac{n \sum X_{1} X_{2}-\sum X_{1} \sum X_{2}}{\sqrt{n \sum X_{1}^{2}-\left(\sum X_{1}\right)^{2}} \sqrt{n \sum X_{2}^{2}-\left(\sum X_{2}\right)^{2}}} \\
& R_{Y X_{1} X_{2}}=\sqrt{\frac{r^{2}{ }_{Y X_{1}+r^{2}{ }_{Y X_{2}}}-2 r_{Y X_{1}} r_{Y X_{2}} r_{X_{1} X_{2}}}{1-r^{2} X_{1} X_{2}}}
\end{aligned}
$$

