

Simple Harmonic Motion

A particle undergoes harmonic motion if it experiences a restoring force proportional to its displacement

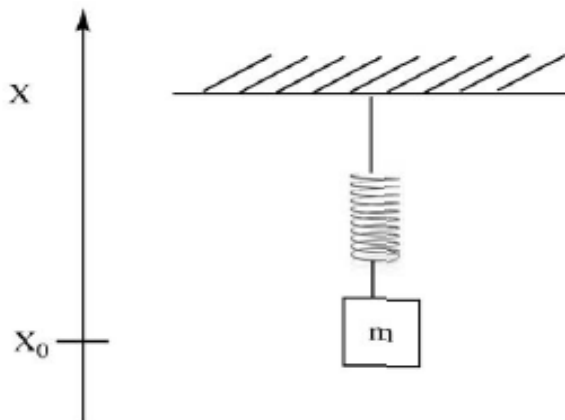
$$F = -kx$$

Where k is the force constant, the stiffer the spring the greater the value of k .

F = force, k = force constant, x = displacement.

The negative sign in F signifies that the direction of the force is opposite to that of the displacement.

Let's first focus on a simple harmonic oscillator in classical mechanics.



Hooke's Law

$$F = -k(X - X_0)$$

force is - gradient
of potential

$$F = -\frac{dV}{dX}$$

When $X > X_0$

Force pushes mass back down toward X_0

When $X < X_0$

Force pulls mass back up toward X_0

Newton Equation

$$F = ma = m \frac{d^2x}{dt^2} = -kx$$

Substitute and rearrange

$$\frac{d^2x}{dt^2} = -\frac{k}{m}x$$

$$x = A \sin \omega t$$

$$\frac{dx}{dt} = A \omega \cos \omega t$$

$$\frac{d^2x}{dt^2} = -A \omega^2 \sin \omega t \quad \dots \dots \dots A \sin \omega t = X$$

$$\frac{d^2x}{dt^2} = -\omega^2 X$$

$$\frac{k}{m} X = -\omega^2 X$$

$$x = A \sin \sqrt{\frac{k}{m}} t$$

$$t = \hat{j}$$

$$X = A \sin \sqrt{\frac{k}{m}} t$$

$$\sqrt{k/m} \hat{j} = 2\pi$$

$$1/\hat{j} = \sqrt{\frac{k}{m}} \frac{1}{2\pi}$$

$$1/\hat{j} = v \quad \dots \quad v = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$$

$$V=c/\lambda = c \bar{\nu} \quad \dots \quad \bar{\nu} = V/c = \frac{1}{2\pi c} \sqrt{k/m}$$

$$m = m_1 m_2 / m_1 + m_2 \quad \dots m = \text{mass reduce}$$

K= force constant (N/m) , V=frequency (s⁻¹),

$\bar{\nu}$ = wave number (cm⁻¹)