

$$\underline{3} \quad (\vec{u} + \vec{0}) = (\vec{0} + \vec{u}) = \vec{u}$$

identity element

$$\underline{4} \quad \vec{u} + (-\vec{u}) = \vec{0}$$

inverse element

$$\underline{5} \quad l(m\vec{u}) = (lm)\vec{u}$$

$$\underline{6} \quad m(\vec{u} + \vec{v}) = m\vec{u} + m\vec{v}$$

$$\underline{7} \quad (l+m)\vec{u} = l\vec{u} + m\vec{u}$$

$$\underline{8} \quad (1)\vec{u} = \vec{u}$$

**Note:** a vector  $\vec{v}$  of length equals to 1 i.e.  $\|\vec{v}\| = 1$ , is called a **unit vector**.

**Definition:** For any vector  $\vec{v}$  such that  $\|\vec{v}\| \neq 0$ , (non-zero vector), it is possible to find the unit vector  $\vec{u}$  of the vector  $\vec{v}$  in the direction of  $\vec{v}$ , which is defined by:

$$\vec{u} = \frac{1}{\|\vec{v}\|} (\vec{v}) \quad \text{so that from}$$

the definition above

$$\|\vec{u}\| = \left\| \frac{1}{\|\vec{v}\|} (\vec{v}) \right\| \stackrel{\text{by } (*)}{=} \left( \frac{1}{\|\vec{v}\|} \right) (\|\vec{v}\|) = 1 \quad \text{unit vector}$$

$$\begin{aligned} (*) \quad \|\vec{v}\| &= \|m(v_1, v_2, v_3)\| \\ &= \|(mv_1, mv_2, mv_3)\| \\ &= \sqrt{(mv_1)^2 + (mv_2)^2 + (mv_3)^2} \end{aligned}$$