

$$+ (-1)^{1+2} (u_1 v_3 - v_1 u_3) \mathbf{j} + (-1)^{1+3} (u_1 v_2 - v_1 u_2) \mathbf{k}$$

Note: \perp the definition of cross product is defined depending on the determinate of matrix and since the determinate of matrix is defined for only the square matrices then cross product is defined for \mathbb{R}^n when $n=3$ only no less no more.

2. If the Question is mentioned the cross product then this means that the question is about \mathbb{R}^3 space.

Example: Let $\vec{u} = (1, 2, -2)$ and $\vec{v} = (3, 0, 1)$, find $\vec{u} \times \vec{v}$ and $\vec{v} \times \vec{u}$

Sol: $\vec{u} \times \vec{v} = \begin{vmatrix} \mathbf{i} & \mathbf{j} & \mathbf{k} \\ 1 & 2 & -2 \\ 3 & 0 & 1 \end{vmatrix} = 2\mathbf{i} - 7\mathbf{j} - 6\mathbf{k}$