

**Q1)** Suppose that you do a binary search for the key **39** in the following sorted array: 10 ,11, 25 ,31, 36, 39, 53, 55, 56, 64, 68, 75, 78, 82, 87 Give the sequence of keys in the array that are compared with 39.

<b>0</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>	<b>10</b>	<b>11</b>	<b>12</b>	<b>13</b>	<b>14</b>
<b>10</b>	<b>11</b>	<b>25</b>	<b>31</b>	<b>36</b>	<b>39</b>	<b>53</b>	<b>55</b>	<b>56</b>	<b>64</b>	<b>68</b>	<b>75</b>	<b>78</b>	<b>82</b>	<b>87</b>
<b>low</b>							<b>Mid</b>							<b>high</b>
<b>low</b>			<b>Mid</b>			<b>high</b>								
				<b>low</b>	<b>found</b>	<b>high</b>								

### ◆ Step 1

- Middle index =  $\lfloor(0+14)/2\rfloor=7$
- Element = **55**
- Compare:  $39 < 55 \rightarrow$  go **left**

### ◆ Step 2

- New range: index 0 to 6
- Middle index =  $\lfloor(0+6)/2\rfloor=3$
- Element = **31**
- Compare:  $39 > 31 \rightarrow$  go **right**

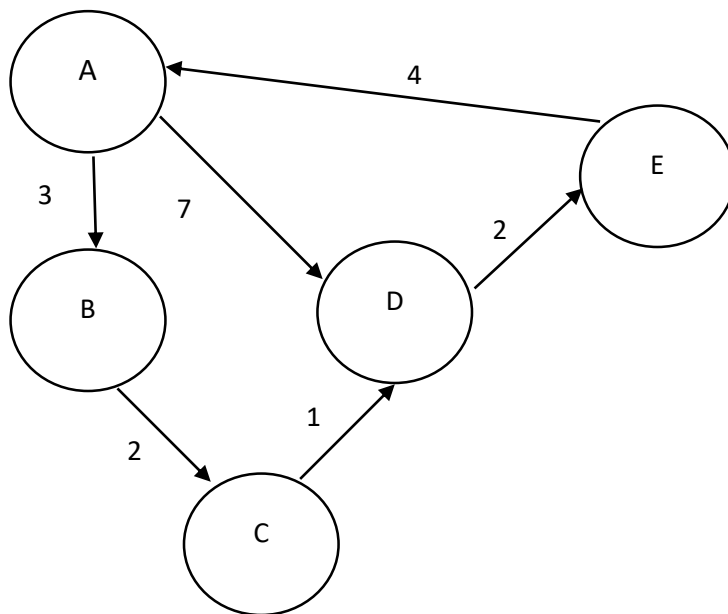
### ◆ Step 3

- New range: index 4 to 6
- Middle index =  $\lfloor(4+6)/2\rfloor=5$
- Element = **39**
- Match found ✓

**Q2)** Consider the following **graph**, represented as an **adjacency matrix**:

	<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>	<i>E</i>
<i>A</i>	$\infty$	3	$\infty$	7	$\infty$
<i>B</i>	$\infty$	$\infty$	2	$\infty$	$\infty$
<i>C</i>	$\infty$	$\infty$	$\infty$	1	8
<i>D</i>	$\infty$	$\infty$	$\infty$	$\infty$	2
<i>E</i>	4	$\infty$	$\infty$	$\infty$	$\infty$

1. Draw the corresponding graph.
2. What is the graph type?
3. Does the graph contain a cycle?



2. Directed, weighted, cyclic

3. yes  $A \rightarrow B \rightarrow C \rightarrow D \rightarrow E \rightarrow A$

**Q1)** Suppose that you do a binary search for the key **75** in the following sorted array: 10 ,11, 25 ,31, 36, 39, 53, 55, 56, 64, 68, 75, 78, 82, 87 Give the sequence of keys in the array that are compared with 75.

<b>0</b>	<b>1</b>	<b>2</b>	<b>3</b>	<b>4</b>	<b>5</b>	<b>6</b>	<b>7</b>	<b>8</b>	<b>9</b>	<b>10</b>	<b>11</b>	<b>12</b>	<b>13</b>	<b>14</b>
10	11	25	31	36	39	53	55	56	64	68	75	78	82	87
low							Mid							high
								low			found			high

◆ Step 1

- Middle index =  $\lfloor (0+14)/2 \rfloor = 7$
- Element = **55**
- Compare:  $75 > 55 \rightarrow$  go **right**

### ◆ Step 2

- New range: index 8 to 14
- Middle index =  $\lfloor (8+14)/2 \rfloor = 11$
- Element = **75**
- Match found ✓

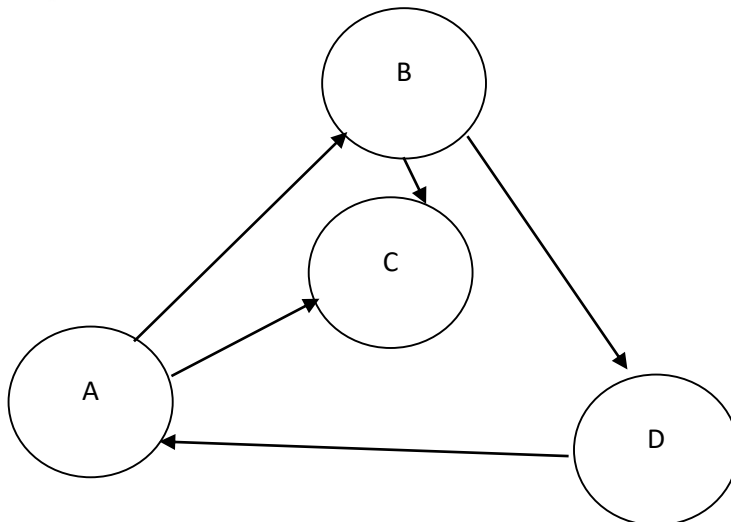
✓ Sequence of comparisons:

55  $\rightarrow$  75

**Q2)** Consider the following **graph** represented as an **adjacency matrix**:

	<i>A</i>	<i>B</i>	<i>C</i>	<i>D</i>
<i>A</i>	0	1	1	0
<i>B</i>	0	0	1	1
<i>C</i>	0	0	0	1
<i>D</i>	1	0	0	0

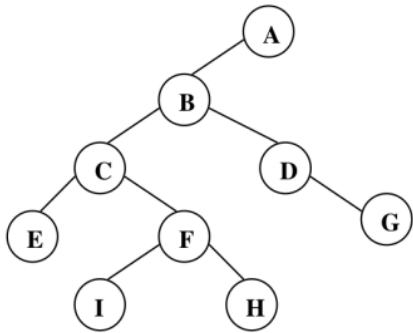
1. **Draw the corresponding graph.**
2. **What is the graph type?**
3. **Does the graph contain a cycle?**



## 2. directed, unweighted, cyclic

Yes  $A \rightarrow B \rightarrow D \rightarrow A$ 

Q1) Consider the following graph:

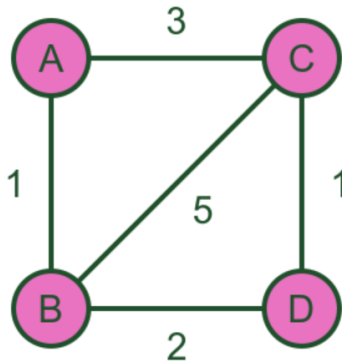


1. Represented its **adjacency matrix** (A).
2. What is the type of the graph?

	A	B	C	D	E	F	G	H	I
A	0	1	0	0	0	0	0	0	0
B	1	0	1	1	0	0	0	0	0
C	0	1	0	0	1	1	0	0	0
D	0	1	0	0	0	0	1	0	0
E	0	0	1	0	0	0	0	0	0
F	0	0	1	0	0	0	0	1	1
G	0	0	0	1	0	0	0	0	0
H	0	0	0	0	0	1	0	0	0
I	0	0	0	0	0	1	0	0	0

Undirected, unweighted, Acyclic

Q1) Consider the following **graph**:



1. Represented its **adjacency matrix (A)**.
2. What is the type of the graph?

	A	B	C	D
A	inf	1	3	inf
B	1	inf	5	2
C	3	5	inf	1
D	2	inf	1	inf

**Weighted, undirected, cyclic**