

# MATLAB

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**المرحلة الثانية - صباحي**

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# **Lecture 13**

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Example (2):

$$\gg D = [2 \ 5 \ 4; 2 \ 4 \ 1] \leftarrow$$

$$\gg E = [1 \ 2; 3 \ 4; 7 \ 2] \leftarrow$$

$$\gg m3 = D * E \leftarrow$$

$$m3 = \begin{matrix} 45 & 32 \\ 21 & 22 \end{matrix}$$

$$\gg m4 = E * D \leftarrow$$

$$m4 = \begin{matrix} 6 & 13 & 6 \\ 14 & 31 & 16 \\ 18 & 43 & 30 \end{matrix}$$

15) To find the sum of the elements of one row or one column in a matrix :

Example :

$$\gg A = [2 \ 5 \ 4; 2 \ 4 \ 1] \leftarrow$$

$$A = \begin{matrix} 2 & 5 & 4 \\ 2 & 4 & 1 \end{matrix}$$

1)  $\gg S1 = \text{sum}(A(1,:)) \leftarrow$  لإيجاد مجموع عناصر الصف الأول في المصفوفة A  
 $S1 = 11$

2)  $\gg S2 = \text{sum}(A(2,:)) \leftarrow$  لإيجاد مجموع عناصر الصف الثاني في المصفوفة A  
 $S2 = 7$

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3)  $\rightarrow S_3 = \text{sum}(A(:, 2)) \leftarrow$  لإيجاد مجموع عناصر العمود الثاني في المصفوفة A  
 $S_3 = 9$

4)  $\rightarrow S_4 = \text{sum}(A(:, 3)) \leftarrow$  لإيجاد مجموع عناصر العمود الثالث في المصفوفة A  
 $S_4 = 5$

16) To find the transpose of a matrix :

Example :

$\rightarrow B = [1 \ 3 \ 5; 2 \ 6 \ 7; 4 \ 9 \ 8] \leftarrow$

$B =$   
1 3 5  
2 6 7  
4 9 8

$\rightarrow B'$   $\leftarrow$

ans =  
1 2 4  
3 6 9  
5 7 8

17) To find the determinant of a matrix :

Example :

$\rightarrow C = [2 \ 2; 7 \ 2] \leftarrow$

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$$C = \begin{bmatrix} 2 & 2 \\ 7 & 2 \end{bmatrix}$$

$\gg \det(C) \ll$

$$\text{ans} = -10$$

18) To find the inverse of a matrix :

Example :

$\gg C = [2 \ 2; 7 \ 2] \ll$

$$C = \begin{bmatrix} 2 & 2 \\ 7 & 2 \end{bmatrix}$$

$\gg \text{inv}(C) \ll$

$$\text{ans} = \begin{bmatrix} -0.2000 & 0.2000 \\ 0.7000 & -0.2000 \end{bmatrix}$$

19) To find the size of a matrix :

Example :

$\gg B = [2 \ 5 \ 3 \ 1; 4 \ 6 \ 2 \ 9]; \ll$

$\gg \text{size}(B) \ll$

$$\text{ans} = 2 \ 4$$

# **Lecture 14**

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## Solving a System of Linear Equations:

1) Solving a system of linear equations by using inverse matrix method in MATLAB prog.

Example: Solve the following system of linear equations by using inverse matrix method in MATLAB prog. :

$$x + y + z = 2$$

$$2x + 3y - z = 9$$

$$x + 3y + 2z = 5$$

Answer:

$$\gg A = [1 \ 1 \ 1; 2 \ 3 \ -1; 1 \ 3 \ 2]; \downarrow$$

$$\gg A1 = \text{inv}(A); \downarrow$$

$$\gg B = [2; 9; 5]; \downarrow$$

$$\gg X = A1 * B \downarrow$$

$$X = \begin{matrix} 1 \\ 2 \\ -1 \end{matrix}$$

$\therefore x = 1, y = 2$  and  $z = -1$

Exercise: Solve the following system of linear equations by using inverse matrix method in MATLAB prog. :

$$x + 8y + 2z = -1$$

$$x + 3y + z = 4$$

$$x + 3y + 2z = 3$$

(ans.  $x = 7.4, y = -0.8,$  and  $z = -1$ )

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2) Solving a system of linear equations by using Cramer's rule in MATLAB prog. .

Example: Solve the following system of linear equations by using Cramer's rule in MATLAB prog. :

$$x + y + z = 2$$

$$2x + 3y - z = 9$$

$$x + 3y + 2z = 5$$

Answer:

$$\gg A2 = [1 \ 1 \ 1; 2 \ 3 \ -1; 1 \ 3 \ 2]; \leftarrow$$

$$\gg A21 = [2 \ 1 \ 1; 9 \ 3 \ -1; 5 \ 3 \ 2]; \leftarrow$$

$$\gg A22 = [1 \ 2 \ 1; 2 \ 9 \ -1; 1 \ 5 \ 2]; \leftarrow$$

$$\gg A23 = [1 \ 1 \ 2; 2 \ 3 \ 9; 1 \ 3 \ 5]; \leftarrow$$

$$\gg x = \det(A21) / \det(A2) \leftarrow$$

$$x = 1.0000$$

$$\gg y = \det(A22) / \det(A2) \leftarrow$$

$$y = 2.0000$$

$$\gg z = \det(A23) / \det(A2) \leftarrow$$

$$z = -1.0000$$

Exercise: Solve the following system of linear equations by using Cramer's rule in MATLAB prog. :

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$$x + 8y + 2z = -1$$

$$x + 3y + z = 4$$

$$x + 3y + 2z = 3$$

(ans.  $x = 7.4$ ,  $y = -0.8$ , and  $z = -1$ )

3) Solving a system of linear equations by using the Gauss-Jordan elimination method in MATLAB prog.

Example: Solve the following system of linear equations by using the Gauss-Jordan elimination method in MATLAB prog.:

$$x + y + z = 2$$

$$2x + 3y - z = 9$$

$$x + 3y + 2z = 5$$

Answer:

$$\gg A = [1 \ 1 \ 1; 2 \ 3 \ -1; 1 \ 3 \ 2]; \leftarrow$$

$$\gg b = [2; 9; 5]; \leftarrow$$

$$\gg X = [A \ b] \leftarrow$$

$$X = \begin{array}{cccc} 1 & 1 & 1 & 2 \\ 2 & 3 & -1 & 9 \\ 1 & 3 & 2 & 5 \end{array}$$

$$\gg rref(X) \leftarrow$$

$$\text{ans} = \begin{array}{cccc} 1 & 0 & 0 & 1 \\ 0 & 1 & 0 & 2 \\ 0 & 0 & 1 & -1 \end{array}$$

$\therefore x = 1$ ,  $y = 2$  and  $z = -1$

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Exercise : Solve the following system of linear equations by using the Gauss-Jordan elimination method in MATLAB prog. :

$$X + 8y + 2Z = -1$$

$$X + 3y + Z = 4$$

$$X + 3y + 2Z = 3$$

(ans.  $X = 7.4$ ,  $y = -0.8$ , and  $Z = -1$ )

Solved Problem :

Solve the following system of linear equations in MATLAB prog. :

$$X + y + 2Z = 14$$

$$X - 3y + 2Z = 10$$

$$2X - y + 2Z = 15$$

- 1) by using inverse matrix method.
- 2) by using Cramer's rule.
- 3) by using Gauss-Jordan elimination method.

Solution :

$$1) \gg A = [1 \ 1 \ 2; 1 \ -3 \ 2; 2 \ -1 \ 2]; \leftarrow$$

$$\gg B = [14; 10; 15]; \leftarrow$$

$$\gg A1 = \text{inv}(A); \leftarrow$$

$$\gg X = A1 * B \leftarrow$$

$$X = \begin{matrix} 3 \\ 1 \\ 5 \end{matrix}$$

$\therefore X = 3, y = 1, \text{ and } Z = 5$

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$$2) \gg A1 = [1 \ 1 \ 2; 1 \ -3 \ 2; 2 \ -1 \ 2]; \leftarrow$$

$$\gg A11 = [14 \ 1 \ 2; 10 \ -3 \ 2; 15 \ -1 \ 2]; \leftarrow$$

$$\gg A12 = [1 \ 14 \ 2; 1 \ 10 \ 2; 2 \ 15 \ 2]; \leftarrow$$

$$\gg A13 = [1 \ 1 \ 14; 1 \ -3 \ 10; 2 \ -1 \ 15]; \leftarrow$$

$$\gg X = \det(A11) / \det(A1) \leftarrow$$

$$X = 3$$

$$\gg y = \det(A12) / \det(A1) \leftarrow$$

$$y = 1$$

$$\gg z = \det(A13) / \det(A1) \leftarrow$$

$$z = 5$$

$\therefore x = 3, y = 1, \text{ and } z = 5$

$$3) \gg A = [1 \ 1 \ 2; 1 \ -3 \ 2; 2 \ -1 \ 2]; \leftarrow$$

$$\gg b = [14; 10; 15]; \leftarrow$$

$$\gg X = [A \ b] \leftarrow$$

$$X = \begin{array}{cccc} 1 & 1 & 2 & 14 \\ 1 & -3 & 2 & 10 \\ 2 & -1 & 2 & 15 \end{array}$$

$$\gg \text{rref}(X) \leftarrow$$

$$\text{ans} = \begin{array}{cccc} 1 & 0 & 0 & 3 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 5 \end{array}$$

$\therefore x = 3, y = 1, \text{ and } z = 5$  .