

**Example1 :** Consider the following four statements:

- (1) Ice floats in water **and**  $2 + 2 = 4$ . T T
- (2) Ice floats in water **and**  $2 + 2 = 5$ . T F
- (3) China is in Europe **and**  $2 + 2 = 4$ . F T
- (4) China is in Europe **and**  $2 + 2 = 5$ . F F

Only the first statement is true. Each of the others is false since at least one of its sub statements is false.

**Example2:** Consider the following four statements:

- (1) Ice floats in water **or**  $2 + 2 = 4$ .
- (2) Ice floats in water **or**  $2 + 2 = 5$ .
- (3) China is in Europe **or**  $2 + 2 = 4$ .
- (4) China is in Europe **or**  $2 + 2 = 5$ .

Only the last statement (iv) is false. Each of the others is true since at least one of its sub statements is true.

**Example3 :** Consider the following six statements:

- (a1) Ice floats in water.
- (a2) It is false that ice floats in water.
- (a3) Ice does not float in water.
- (b1)  $2 + 2 = 5$
- (b2) It is false that  $2 + 2 = 5$ .
- (b3)  $2 + 2 \neq 5$

Then (a2) and (a3) are each the negation of (a1); and (b2) and (b3) are each the negation of (b1).

Since (a1) is true, (a2) and (a3) are false; and since (b1) is false, (b2) and (b3) are true.

#### 4. Proposition AND Truth Tables

The truth table for the compound proposition  $\neg(p \wedge \neg q)$  is:

$p$	$q$	$\neg q$	$p \wedge \neg q$	$\neg(p \wedge \neg q)$
T	T	F	F	T
T	F	T	T	F
F	T	F	F	T
F	F	T	F	T

