

Definition :-

 An order set S is called well-order if every non-empty subset of S has a smallest (or first) element.

Examples. ① $S = \mathbb{N}$, $(\mathbb{N}, <)$ is an order set

Let $E = \{7, 8, 9, 10\}$.

$G = \{2, 3, 4\}$.

since $G \subseteq \mathbb{N}$ has smallest element.

$E \subseteq \mathbb{N}$ has smallest element.

$\therefore \mathbb{N}$ is well-order.

② $S = \mathbb{Z}$, $(\mathbb{Z}, <)$ an order set.

Let $E = \{\dots, -3, -2, -1, 0\}$

$E \subseteq \mathbb{Z}$, but E has no smallest element.

$\therefore \mathbb{Z}$ is not well-order.