

Lemma :-

———— If  $r \in \mathbb{Q}$  and  $s \in \mathbb{Q}'$ , then

1.  $r + s \in \mathbb{Q}'$
2.  $r \cdot s \in \mathbb{Q}'$ .

Proof ①

Suppose that  $r + s \notin \mathbb{Q}'$   
 $\Rightarrow r + s \in \mathbb{Q}$ .

Since  $\mathbb{Q}$  is field and  $r \in \mathbb{Q}$ .

$\Rightarrow (r + s) - r = s \in \mathbb{Q}$  c! with hypothesis  
 $s \in \mathbb{Q}'$ .  
 $\therefore r + s \in \mathbb{Q}'$ .

Proof ② (Exc).

Definition =- A complex number is an order pair  
where  $a, b \in \mathbb{R}$ , and we denoted by the  
Set of all complex number by  $\mathbb{C}$ .

Definition =- let  $(a, b), (c, d)$  be two complex  
numbers. then

1.  $(a, b) = (c, d)$  iff  $a = c, b = d$ .
2.  $(a, b) + (c, d) = (a + c, b + d)$ .
3.  $(a, b) \cdot (c, d) = (ac - bd, ad + bc)$