

①

Definition:- let  $(X, d)$  be a metric space let  $E \subseteq X$   
 a point  $p \in E$  is called an interior point  
 of  $E$  if  $\exists N_r(p) \ni N_r(p) \subseteq E$ . The set of all  
 interior point of  $E$  denoted by  $E^\circ$  or  $\text{int } E$ .

Example:- Let  $(\mathbb{R}, d)$  be a usual metric space.  
 $E = [0, 1)$  ? Find  $E^\circ$

Solution:- let  $p \in [0, 1)$

$$r = \frac{1}{2} \min \{ |p-0|, |p-1| \}$$

$\therefore p$  is interior point of  $[0, 1)$

Let  $p=0$

it is not possible to find  $N_r(p) \ni$

$$N_r(p) \subseteq E$$

$$\therefore \text{int } E = (0, 1)$$

Example:- let  $(\mathbb{R}, d)$  be a usual metric space,  
 $E = \{4, 5, 6\}$  ? Find  $E^\circ$

Solution:- Since there is no neighbourhood of any  
 point of  $E$  which is subset of  $E$  then  
 $E^\circ = \emptyset$ .

Definition:- let  $(X, d)$  be a metric space a subset  $E$   
 of  $X$  is called open set if every point of  
 $E$  is an interior point of  $E$ .

Example:- ①  $E = (0, 1)$  ,  $E = \{x : 0 < x < 1\}$   
 Since every point of  $(0, 1)$  is an interior point  
 $\therefore (0, 1)$  is open

② -  $A = [0, 1]$  ,  $A = \{x : 0 \leq x \leq 1\}$

Since  $(0)$  and  $(1)$  are in  $A$  and not interior