

### a- Banker's Algorithm

This Alg. Could be used in a banking system to ensure that the bank never allocates its available cash in such a way that it can no longer satisfy the needs of all its customers. When a new process enters the system it must declare the maximum number of instances of each resource type that it may need.

- The maximum must be  $\leq$  total number of resources in the system.
- When a user requests a set of resources must be leave the system in a safe state if the resources are allocated otherwise the process must wait until some other process releases enough resources.

Several data structures must be maintained to implement banker's algorithm

Let  $n$  be the number of processes in the system and  $m$  be the number of resource types . We need the following data structures:

- Available : A vector of length  $m$  indicates the number of available resources of each type.

available . If available  $[j] = k$  these are  $k$  instances of resource type  $R_j$

- Max : An  $n \times m$  matrix defines the maximum demand of each process . If  $\max[i,j] = k$  , then process  $P_i$  may request at most  $k$  instances of resource type  $R_j$
- Allocation : An  $n \times m$  the resources currently allocated to each process . If allocation  $[i,j] = k$  then process  $p_i$  is currently allocated  $k$  instances of resources of resource type  $R_j$ .
- Need : An  $n \times m$  indicates the remaining resource need of each process . If  $\text{need}[i,j] = k$  then process  $p_i$  may need  $k$  more instances of resource type  $R_j$  to complete its task .

$\text{Need}[i,j] = \text{Max}[i,j] - \text{Allocation}[i,j]$

1- If request  $i \leq \text{Need}[i]$  go to step 2 otherwise raise an error since the process has exceeded its maximum claim.

2- If request  $i \leq \text{Available}$  go to step 3 . Otherwise  $p_i$  must wait since the resources are not available .

3- The system pretends to have allocated the requested resources to process  $p_i$  by modifying the state as follows:

$\text{Available} := \text{Available} - \text{Request}_i$  ,  
 $\text{Allocation}_i := \text{Allocation}_i + \text{Request}_i$  ,

$\text{Need}_i := \text{Need}_i - \text{Request}_i$ ,

If the resulting resource allocation state is safe the transaction is completed and process  $p_i$  is allocated its resources. If the new state is unsafe the  $p_i$  must wait for request  $i$  and the old resource allocation state is restored.

### c- Safety Algorithm

The algorithm for finding out whether or not a system is in a safe state can be described as follows:

- 1- Let work and finish be vectors of length m and n respectively.  
Initialize work := Available and Finish [i] := False for I = 1,2, ..., n
- 2- Find an i such that both
  - Finish [i] = false
  - Need i ≤ work
 If no such i exists, go to step 4
- 3- Work := work + allocation I Finish[i] := true go to step2
- 4- If Finish [i] = true for all I then the system is in a safe state

This algorithm may require an order of  $m \times n^2$  operations to decide whether a state is safe.

#### Example:

Consider a system with five processes  $\{p_0, p_1, p_2, \dots\}$  and three resource types  $\{A, B, C\}$ . Resource type A has 10 instances. Resource type B has 5 instances, and resource type c has 7 instance. Suppose that at time  $T_0$  the following snapshot of the system has been taken.

Allocation	Max	Available	
A B C	A B C	A B C	
0 1 0	7 5 3	3 3 2	P <sub>0</sub>
2 0 0	3 2 2		P <sub>1</sub>
3 0 2	9 0 2		P <sub>2</sub>
2 1 1	2 2 2		P <sub>3</sub>
0 0 2	4 3 3		P <sub>4</sub>

The content of the matrix Need is defined to be max-Allocation and is:

	Need
	A B C
P <sub>0</sub>	7 4 3
P <sub>1</sub>	1 2 2
P <sub>2</sub>	6 0 0
P <sub>3</sub>	0 1 1
P <sub>4</sub>	4 3 1

The system is in the safe state if the processes executed in the sequence  $(p_1, p_3, p_4, p_2, p_0)$ . Suppose now that process  $p_i$  requests one additional instance of resource type A and two instance of resources type C so request 1 =  $(1, 0, 2)$   
To decide whether this request can be immediately granted we first check that Request 1 ≤ Available ( that is ,  $(1,0,2) \leq (3,3,2)$ ) which is true we then pretend that this request has been fulfilled and we arrive at the following new state.

Allocation	Max	Available	
A B C	A B C	A B C	
0 1 0	7 4 3	3 3 2	P <sub>0</sub>
3 0 2	0 2 0		P <sub>1</sub>
3 0 2	6 0 0		P <sub>2</sub>
2 1 1	0 1 1		P <sub>3</sub>
0 0 2	4 3 1		P <sub>4</sub>

By execute the safety Alg. We find the sequence ( p<sub>1</sub> , p<sub>3</sub> , p<sub>4</sub> , p<sub>0</sub> , p<sub>2</sub>) satisfies our safety requirements . Hence we can immediately grant the request of process p<sub>1</sub>

If p<sub>4</sub> request for ( 3 , 3 , 0) . The request can not granted since the resources are not available . Request 1 > Available . If p<sub>0</sub> request ( 0 , 2 , 0) can not granted even though the resources are available since the resulting state is unsafe.

## Deadlock Detection

If a system does not employ some protocol that ensures that no deadlock will never occur. Then a detection and recovery scheme must be implemented . The system can use an algorithm to examines the state of the system periodically to determine whether has occurred . If so the system must recover from the deadlock by providing :

- Maintain information about the current allocation of resources to processes and outstanding request.
- Provide an Alg. That use the above information to determine whether the system has entered the deadlock state.

The detection Alg. Employs several time – varying data structures that are very similar to those used in the Banker’s Algorithm :

- **Available**
- **Allocation**
- **Request** . An n<sub>x</sub>m matrix indicating the current request of each process.  
If Request [i,j] = k then p<sub>i</sub> is requesting k more instances of resource type r<sub>j</sub> .

The detection Alg. Simply investigates every possible allocation sequence for the processes that remain to be completed.

The detection Alg . as follows:

- Let work and finish be vectors of length m and n respectively . Initialize  
Work := Available , for i = 1 ,2 ,3, ... , n. If allocation ≠ 0 the Finish [i] := false.  
Otherwise , Finish[i] := false.

- Find an index i such that :

- Finish [i] = false , and
- Request i ≤ work .

If no such I exits go to step 4.

- Work := work +Allocation i

Finish [i] := true

Go to step2

- If Finish [i] = false , for some i , 1 ≤ i ≤ n then the system is in a deadlock state. More over , if Finish [i] = false then process p<sub>i</sub> is deadlocked.

### Example

Consider a system with five processes  $\{p_0, p_1, \dots, p_4\}$  and three resources types  $\{A=7 \text{ instance}, B=2, C=6 \text{ instance}\}$  suppose that at time  $T_0$  we the following resource allocation state.

Allocation	Max	Available	
A B C	A B C	A B C	
0 1 0	0 0 0	0 0 0	$P_0$
2 0 0	2 0 2		$P_1$
3 0 3	0 0 0		$P_2$
2 1 1	1 0 0		$P_3$
0 0 2	0 0 2		$P_4$

If we execute the detection Alg. We find the system is not in a deadlock state and the sequence  $\langle p_0, p_2, p_3, p_1, p_4 \rangle$  will result in finish  $[i] = \text{true}$  for all  $i$ .

Suppose now that process  $p_2$  makes one additional request for an instance of type C. the Request matrix is modified as follows :

	Need
	A B C
$P_0$	0 0 0
$P_1$	2 0 2
$P_2$	0 0 1
$P_3$	1 0 0
$P_4$	0 0 2

We claim that the system is now deadlocked . Although we can reclaim the resources held by process  $p_0$  the number of available resources is not sufficient to fulfill the requests of the other processes . Thus a deadlock exist , consisting of processes  $\langle p_1, p_2, p_3 \text{ and } p_4 \rangle$ .

- Single Instance of each resource type

The detection Alg. is of order  $m \times n^2$  . If all resources have only a single instance we can define a faster Alg. we will use a variant of the resource allocation graph called a wait – for graph . This graph is obtained from the resource allocation graph by removing the nodes of type resource and collapsing the appropriate edges. Where the edge from  $p_i$  is waiting for process  $p_j$  to release a resource that it needs.

An edge  $(p_i, p_j)$  exists in a wait – for graph if and only if the resource RAG contains two edges  $(p_i, r_q)$  and  $(r_q, p_j)$  for some resource , see fig bellow

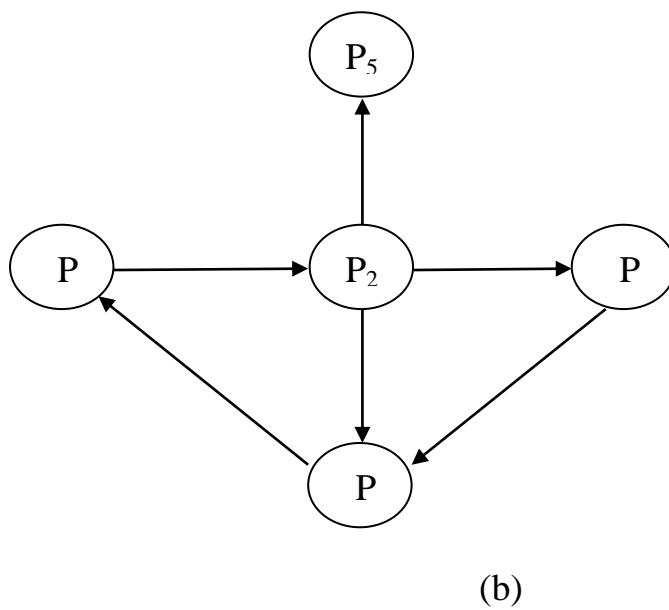
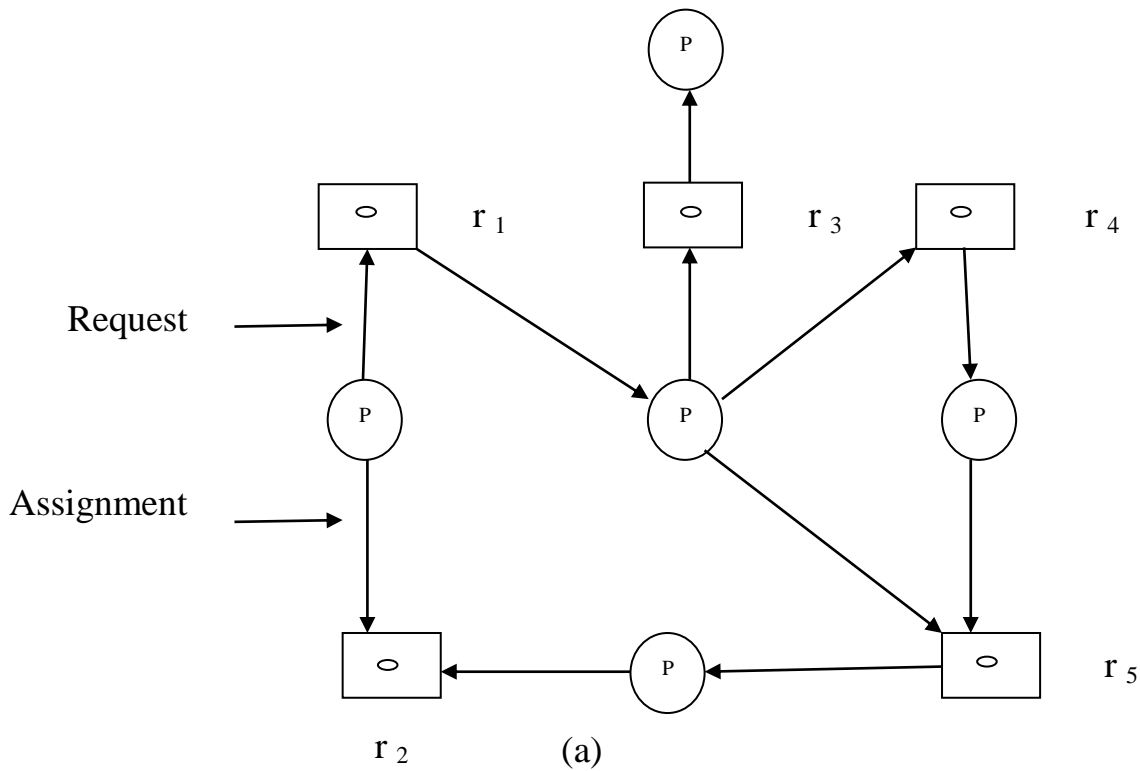


Fig: RAG (a) and its wait – for graph (b)

A deadlock exists in the system if and only if the wait – for graph contains a cycle.

- **Recovery from deadlock**

When a detection Alg. determines that a deadlock exists the system must recover from the deadlock .

There are two options for breaking a deadlock

a- **Process termination** by killing a process , two methods:

- Kill all deadlocked processes.
- Kill one process at a time until the deadlock cycle is eliminated.

b- **Resource preemption**, to eliminate deadlocks using resource preemption we can preempt some resources from processes and give them to other processes until the deadlock cycle is broken .

If preemption is required in order to deal with deadlocks then three issues need to be addressed:

- Selecting a victim: which process and which resources .
- Rollback : if we preempt a resource from a process what should be done with that process?
- Starvation : How do we ensure that Starvation will not occur?  
That is how can we guarantee that resources will not always be preempted from the some process?