Circle Drawing

The circle is a special kind of curves. The circle is a closed curve with same starting and ending point. Circles are probably the most used curves in elementary graphics.



- A circle is specified by the coordinates of its center (xc,yc) and its radius (r).
- The circle equation is : $(x-xc)^2 + (y yc)^2 = r^2$ (1)
- If the center of the circle is at the origin (0,0) then the equation is :

$$x^{2}+y^{2}=r^{2}$$
 (2)

Solving equation (1) for y :

$$y = yc \pm \sqrt{r^2 - (x - xc)^2}$$

Note: To draw a circle increment the x values by one unit from –r to +r and use the above equation to solve for the two y values at each step.

1. Direct (implicit) algorithm

In this method the first pixel of circle is at left side as equation x=xc-r

y=yc

to draw the circle we can increment x from –r to +r or from 0 to 2r by one unit at each step and solving for y

$$y = yc \pm \sqrt{r^2 - (x - xc)^2}$$
$$x = x + 1$$

This method of drawing a circle is inefficient because:

- 1. We are not taking advantages of the symmetry of the circle.
- 2. The amount of processing time required to perform the squaring and square root operations repeatedly.
- 3. X values are equally spaced (they differ by one unit) the y values are not. The circle is denes and flat near the y-axis and has large gaps and is steep near the x-axis.





H\W: Design implicit algorithm to draw circle if the first point is at right side.

2018-2019

H\W: design implicit algorithm to draw circle if the first point is x=xc, y=yc - r

H**W**: Find the point of a circle where xc=20, yc = 10 and r=8?

Example :Find the point of a circle where xc=10, yc= 10 and r=5 using direct algorithm?

```
xc=10
yc=10
x=xc-r x=10-5=5 3
For i=0:2*r
y=yc+sqrt((r^2)-(x-xc)^2)
Plot(x,round(y),'y')
y=yc-sqrt((r^2)-(x-xc)^2)
Plot(x,round(y),'y')
x=x+1
```

End

X	Y	Round(y)	Y	Round(y)	Plot(X,Y)
5	10	10	10	10	(5,10),(5,10)
6	13	13	7	7	(6,13),(6,7)
7	14	14	6	6	(7,14),(7,6)
8	14.5	15	5.4	5	(8,15),(8,5)
9	14.8	15	5.1	5	(9,15),(9,5)
10	15	15	5	5	(10,15),(10,5)
11	14.8	15	5.1	5	(11,15),(11,5)
12	14.5	15	5.4	5	(12,15),(12,5)
13	14	14	6	6	(13,14),(13,6)
14	13	13	7	7	(14,13),(14,7)



2. parametric (polar) algorithm

One method of eliminating the problem of plotting points evenly spaced around the circle is to use polar representation of a circle:

```
x = x_c + r \cos \theta,
```

$$y = y_c + r \sin \theta$$
.

Where: $\theta \ \rightarrow$ is measured in radians from 0 to 2π

arc length= $r \times \theta$, r=radius (constant)

in this method we depend on angles to draw the circle, since it propose the first angle th=0, and end angle is two_pi (360).

The change in angle (dth) must be small value dth=1/r.



Polar algorithm

```
Input : xc ,yc , r.
Output : Circle
{
    th=0; dth=1/r;
    while (th<=2*pi)
        {
            x = xc + r *cos (th)
            y = yc + r sin(th)
            plot (integer(x), integer(y), color)
            th = th + dth;
        }
}</pre>
```

Note: the algorithm use cos & sin operation and do not take the advantage of symmetric in circle

H\W: write Matlab program to draw circle using polar algorithm?

Example :Find the point of a circle where xc=10, yc= 10 and r=5 using polar algorithm ?

```
th=0
dth=1/r=1/5
While th <=2*pi
    x=xc+r*cos(th)
    y=yc+r*sin(th)
    Plot(round(x),round(y),'.k')
    th=th+dth</pre>
```

End

Х	Round(x)	У	Round(y)	th	Plot (x,y)
15	15	10	10	0.2	(15,10)
14.9	15	10.9	11	0.4	(15,11)
14.6	15	11.9	12	0.6	(15,12)
14.1	14	12.8	13	0.8	(14,13)
13.4	13	13.5	14	1	(13,14)
12.7	13	14.2	14	1.2	(13,14)
11.8	12	14.6	15	1.4	(12,15)
:	:	:	:	:	:
:				•	
14.9	15	9.5	10	6.4	(15,10)

