

Lecture ONE : Number Systems

Number systems :

In general any number N can be represented in the base (radix) R as show below :

$$N_R = d_n R^n + d_{n-1} R^{n-1} + \dots\dots\dots d_1 R^1 + d_0 R^0$$

1-Decimal system (R= 10) :

This system uses (10) symbols (0 – 9)

$$Ex: N_{10} = 2^3 3^2 6^1 8^0 = 2 \times 10^3 + 3 \times 10^2 + 6 \times 10^1 + 8 \times 10^0 = 2000 + 300 + 60 + 8 = 2368$$

2-Binary system (R = 2) :

It uses only two basic symbol (0,1) . It is the most suitable number system for digital circuits.

$$Ex: N_2 = 1^4 1^3 0^2 0^1 1^0 = 1(2)^4 + 1(2)^3 + 0(2)^2 + 0(2)^1 + 1(2)^0 = 16 + 8 + 0 + 0 + 1 = (25)_D$$

$$Ex: 1^3 0^2 0^1 1^0 = 1(2)^3 + 0(2)^2 + 0(2)^1 + 1(2)^0 = 8 + 0 + 0 + 1 = (9)_D$$

3-Octal system (R= 8) :

It uses 8 symbols (0- 7)

$$Ex : 1^1 7^0 = 1(8)^1 + 7(8)^0 = 8 + 7 = (15)_D$$

$$Ex: 7^3 0^2 4^1 5^0 = 7(8)^3 + 0(8)^2 + 4(8)^1 + 5(8)^0 = 3584 + 0 + 32 + 5 = (3621)_D$$

4- Hexadecimal system (R =16)

It uses 16 symbol :

(0,1,2,.....,9,A,B,C,D,E,F)

$$Ex: 1^1 A^0 = 1(16)^1 + A(16)^0 = 16 + 10 = (26)_D$$

$$Ex: 3^2 9^1 5^0 = 3(16)^2 + 9(16)^1 + 5(16)^0 = 768 + 144 + 5 = (917)_D$$

The following table gives the correspondence between the four number system :

| Decimal | Binary | Octal | Hexadecimal |
|---------|--------|-------|-------------|
| 0 | 0 | 0 | 0 |
| 1 | 01 | 1 | 1 |
| 2 | 10 | 2 | 2 |
| 3 | 11 | 3 | 3 |
| 4 | 100 | 4 | 4 |
| 5 | 101 | 5 | 5 |
| 6 | 110 | 6 | 6 |
| 7 | 111 | 7 | 7 |
| 8 | 1000 | 10 | 8 |
| 9 | 1001 | 11 | 9 |
| 10 | 1010 | 12 | A |
| 11 | 1011 | 13 | B |
| 12 | 1100 | . | C |
| . | . | . | D |
| . | . | . | E |
| . | . | . | F |
| . | . | . | 10 |
| . | . | . | 11 |
| . | . | . | 12 |

Continue the above table.