

$$\Rightarrow \mp \frac{\partial u}{\sqrt{1+a^2}} = \frac{\partial z}{\sqrt{z}}$$

$$\Rightarrow \mp \int \frac{\partial u}{\sqrt{1+a^2}} = \int \frac{\partial z}{z^{\frac{1}{2}}}$$

$$\Rightarrow \mp \int \frac{\partial u}{\sqrt{1+a^2}} = \int z^{-\frac{1}{2}} \partial z$$

$$\Rightarrow \mp \frac{u}{\sqrt{1+a^2}} = 2 \frac{z^{\frac{1}{2}}}{\frac{1}{2}} + C$$

$$\Rightarrow \mp \frac{x+ay}{\sqrt{1+a^2}} = 2\sqrt{z} + C$$

Subject _____

موضوع الدرس

Date: / /

الموافق

التاريخ / /

ex 2 Solve $q(z-q) = p$

let $u = x + ay$

$$p = \frac{\partial z}{\partial u}, \quad q = a \frac{\partial z}{\partial u}$$

$$a \frac{\partial z}{\partial u} \cdot \left(z - a \frac{\partial z}{\partial u} \right) = \frac{\partial z}{\partial u}$$

$$\Rightarrow a \left(z - a \frac{\partial z}{\partial u} \right) = 1$$

$$\Rightarrow az - a^2 \frac{\partial z}{\partial u} = 1$$

$$\Rightarrow az - 1 = a^2 \frac{\partial z}{\partial u}$$

$$\Rightarrow \int \frac{\partial u}{a^2} = \int \frac{\partial z}{az-1}$$

$$\Rightarrow \frac{u}{a^2} = \frac{1}{a} \int \frac{a \partial z}{az-1}$$

كتابنا بالمقام
والجزء ونقسم
بـ (a)

$$\Rightarrow \frac{u}{a^2} = \frac{1}{a} \ln |az-1| + C$$

$$\Rightarrow \frac{x+ay}{a^2} = \frac{1}{a} \ln |az-1| + C$$