

المطلوب

ex ① $X^3 P^3 + y^3 q^3 = 27 Z$

Sol $(XP)^3 + (yq)^3 = 27 Z$

$X = \ln x$, $Y = \ln y$ الفرميه

$XP = \frac{\partial Z}{\partial X} = p_1$

$yq = \frac{\partial Z}{\partial y} = q_1$

عوضا الفرمة بالمعادلة الاصلية

$\Rightarrow p_1^3 + q_1^3 = 27 Z$

حلول الشكل الكا اكاالة الشانبة (Case 2)

$Z = f(u)$

$u = X + ay$

$p_1 = \frac{\partial Z}{\partial u}$

$q_1 = a \frac{\partial Z}{\partial u}$

$(\frac{\partial Z}{\partial u})^3 + (a \frac{\partial Z}{\partial u})^3 = 27 Z$

$(\frac{\partial Z}{\partial u})^3 + a^3 (\frac{\partial Z}{\partial u})^3 = 27 Z$

$(\frac{\partial Z}{\partial u})^3 [1 + a^3] = 27 Z$] $\times (1 + a^3)$

$(\frac{\partial Z}{\partial u})^3 = \frac{27 Z}{1 + a^3}$ الجذر التكعيبي

$\frac{\partial Z}{\partial u} = \frac{3 \sqrt[3]{Z}}{\sqrt[3]{1 + a^3}}$



Subject _____

موضوع الدرس _____

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الموافق _____

التاريخ _____

$$\int \frac{\partial z}{3z^{1/3}} = \int \frac{\partial u}{3\sqrt[3]{1+a^3}}$$

$$\int \frac{1}{3} z^{-1/3} dz = \frac{u}{3\sqrt[3]{1+a^3}} + C$$

$$\frac{1}{3} z^{2/3} = \frac{x+ay}{3\sqrt[3]{1+a^3}} + C$$

$$\frac{1}{2} \sqrt[3]{z^2} - \frac{\ln x + a \ln y}{3\sqrt[3]{1+a^3}} + C$$

